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1 **Title: Forces acting on bridge abutments over liquefied ground**

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7

8 Abstract:

9 Large earthquake-induced displacements of a bridge abutment can occur, when the bridge is built
10 on a floodplain or reclaimed area, i.e., liquefiable ground, and crosses a water channel. Seismic
11 responses of a bridge abutment on liquefiable ground are the consequence of complex interactions
12 between the abutment and surrounding soils. Therefore identification of the factors dominating the
13 abutment response is important for the development of simplified seismic design methods. This
14 paper presents the results of dynamic three-dimensional finite element analyses of bridge abutments
15 adjacent to a river dike, including the effect of liquefaction of the underlying ground using
16 earthquake motions widely used in Japan. The analysis shows that conventional design methods
17 may underestimate the permanent abutment displacements unless the following two items are
18 considered: (1) softening of the soil beneath the liquefiable layer, due to cyclic shearing of the soil
19 surrounding the piles, and (2) the forces acting on the side faces of the abutment.

20

21 Keywords:

22 abutment, pile foundation, liquefaction, earth pressure, finite element analysis

23

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27

28 1. Introduction

29

30 Large earthquake-induced displacements of a bridge abutment can occur, when the bridge is
31 built on a floodplain or reclaimed area, i.e., liquefiable ground, and crosses a water channel. When
32 the abutment is located adjacent to a river dike or revetment (See Fig. 1), it is especially prone to
33 movement toward the waterfront during an earthquake, when the underlying ground liquefies.

34 In conventional Japanese design methods, the seismic performance of bridge abutments on
35 liquefiable soil is assessed by pushover analysis, i.e., by calculating the response of the abutment
36 subjected to (1) the inertial force of the superstructure and the abutment, and (2) the seismic active
37 earth pressure of the backfill. The kinematic load induced by interaction between the surrounding
38 soil and structure has been neglected, for simplicity, because liquefaction of the foundation soil
39 appears to cause a reduction of lateral soil resistance [1].

40 For structures subjected to lateral spread on level ground or gentle slopes, many procedures that
41 account for effects of the lateral spreading on their performance have been proposed [2][3][4][5].
42 However the existing procedures may not be directly applicable to bridge abutments since the
43 seismic performance of abutments is also affected by many factors, such as, (1) local deformation
44 of the adjacent river dike, (2) deformation of foundation soils caused by the weight of a road
45 embankment connected to the abutment, and (3) slumping of the road embankment itself. Because
46 the seismic response of a bridge abutment on liquefiable ground is the consequence of complex
47 interactions among all these factors, identifying the factors dominating the abutment response is
48 critical when simplified seismic design is used.

49 In addition, the critical moment for the abutment during earthquakes has to be carefully chosen
50 for such a simplified seismic design method: When the seismic performance of a pile-supported
51 bridge abutment is assessed with the pushover analysis, the response coinciding with the arrival of
52 the largest (principal) shock is generally assumed to represent the critical design condition for the
53 abutment. However, the horizontal displacement of the abutment coinciding with the principal
54 shock is not necessarily the maximum displacement the abutment will experience and the same is
55 also true for the strength and ductility demands for the structural members that form the bridge
56 abutment.

57 This paper presents the results of dynamic three-dimensional finite element analyses on bridge
58 abutments built on liquefiable ground adjacent to river dikes, taking into account the effect of
59 liquefaction on abutment response. Two configurations of the surrounding ground were modelled,
60 and the seismic response of abutments both with and without piles is presented. Forces acting on
61 the abutment as well as calculated responses of the abutment are described in detail to demonstrate

62 (1) the critical moment assumed in the conventional design methods, i.e., pushover analyses, being
63 not always appropriate and (2) marked contribution of the forces acting on the side faces of the
64 abutment in the forces acting on the abutment. The results of the analyses are presented, including
65 recommendations for revisions in the current conventional design methods employing the pushover
66 analysis for bridge abutments.

67

68 2. Numerical analysis overview

69

70 Highway bridge abutments constructed near a river channel were modelled and analyzed.
71 Two configurations of the ground surrounding the abutment were considered; a plan view and cross
72 section of the models is illustrated in Fig. 2. The bridge crosses a river, with a distance between
73 abutments of 70m. For a fully coupled three-dimensional finite element analysis, limited
74 computer resources did not permit the use of a fine mesh, so a relatively coarse mesh was employed
75 (cf. Fig. 6 in the following section). Because of this limitation, the pile foundation was modelled
76 by relatively small number of piles having large diameter.; The pile foundation was modelled with
77 six $D=2\text{m} \times L=20\text{m}$ cast-in-place concrete piles, arranged in 2x3 grids with 5m spacing. The
78 width of the bridge is 15m, and the slope of the river dike and road embankment connected to the
79 10m-high pile-supported abutment is 1V:2H. The water level was set at 7.5m below the crest of
80 the dike. The original ground level is 5m above riverbed for the cases illustrated in Fig. 2(a), and
81 10m for the cases shown in Fig. 2(b). The thickness of the liquefiable layer (loose sand deposit)
82 below the water table is 12.5m, and the materials of the dike and embankment are assumed to be the
83 same as that of the surface layer that lies above the water table. The piles are installed into a
84 bottom non-liquefiable layer (dense sand deposit) through the liquefiable layer.

85 In the numerical analyses, only a half-width of the road bridge in the y -direction was modelled,
86 in order to take advantage of symmetry. The width of the analytical domain in y -direction is 100m,
87 the length in x -direction is 240m, and the depth in z -direction from the riverbed is 20m. The
88 $x=-40\text{m}$ and $x=200\text{m}$ planes were allowed to move freely in the x - and z -directions, but not in the
89 y -direction. At $z=-20\text{m}$, all movement was restrained. Fluid flow velocities normal to the
90 analytical domain boundary were set to zero at the side and bottom boundaries. Soils, stem and
91 base of the abutment were modelled by solid elements, and the piles were modelled with elastic
92 beam elements. Because Potyondy [6] reported that the wall friction angle between smooth
93 concrete and sand is around 75% of the soil shearing resistance, no interface element was inserted
94 between the abutment and the adjacent soil. The extended sub-loading surface model proposed by
95 Hashiguchi & Chen [7] was adopted for the soil layers. Material parameters of the soil layers and

96 the structural components are listed in Table 1, where G_s =specific gravity, e_0 =initial void ratio, λ &
97 κ =slopes of the compression & swelling lines in v - $\ln(p')$ plane, ν =Poisson's ratio, k =hydraulic
98 conductivity, ρ =unit density, E =Young's modulus, I =flexural rigidity of the beam, A =area of beam
99 section, and the other parameters are specific parameters for the constitutive model used.
100 Liquefaction resistances of the non-liquefiable and liquefiable layers are summarized as the cyclic
101 shear stress ratio plotted against the number of loading cycles that cause liquefaction in triaxial tests,
102 as shown in Fig. 3. Typical stress path and stress-strain relations for the liquefiable layer soil are
103 shown in Fig. 4. Details of the numerical analysis code are described in Takahashi [8].

104 To evaluate the seismic performance of structures, two levels of earthquake motions are used
105 in Japan [9]; one is a moderate earthquake motion whose return period is smaller than the life time
106 of a structure (from 50 to 100 years) and the others are strong earthquake motions whose return
107 period is more than several hundred years. For the latter, two types of earthquake motions are
108 considered; one is the inland earthquake motion and the other is the subduction earthquake motion.
109 In this study, numerical analyses were performed to assess the seismic performance of the bridge
110 abutments against the strong earthquakes. Figure 5 shows the applied earthquake motions.
111 These are widely used in practice in Japan. One is the inland earthquake motion (Fig. 5(a), sample
112 waveform for Spectrum II [10].) The other one is the subduction earthquake motion (Fig. 5(b),
113 sample waveform for Spectrum I [10].) The earthquake motion is applied in the bridge axis
114 direction (x -direction). The equations of motion are integrated using Newmark's β method, with
115 a time step $\Delta t=0.005$ sec. System damping is represented by Rayleigh damping using a damping
116 ratio of 2.5 % in a first mode of free vibration of the system.

117 Six calculations were conducted, as listed in Table 2. Except for P-H(EQ1), the inland
118 earthquake motion (Fig. 5(a)) was applied. Before performing a dynamic response analysis, a
119 geostatic analysis was conducted, by applying the self weight gradually, in order to establish the
120 initial stress state of the system. In P-L, the road embankment was connected to the pile-supported
121 abutment, with the original ground level set to a height of 5m above the riverbed (Fig. 2(a).) For
122 this case, waterward and landward stretching of the river dike, and the slumping of the road
123 embankment, were expected. In P-H, because the ground level was set to a height of 10m above
124 the riverbed (at the same level of the roadway, Fig. 2(b).), the deformation mode of the surrounding
125 ground was thought to be simpler than for case P-L, since no complicated spreading mode of the
126 foundation ground, induced by the slumping of the road embankment in a direction perpendicular to
127 the bridge axis, was expected. By comparing cases P-L and P-H, the effect that the geometry of
128 the surrounding ground has on the seismic response of the abutment can be observed.

129 In case P-H(Fix), the "strut effect" of the bridge deck on abutment response was modelled by

130 constraining the horizontal displacement of the top of the abutment. In the geostatic analysis, it
131 was assumed that the top of the abutment is initially in contact with the deck before shaking
132 commences for all the cases. Thus, the initial stress state of the system for P-H(Fix) is the same as
133 that for the case without the strut effect (P-H). Since the critical moment in the abutment may
134 vary depending upon the earthquake motion waveform, the subduction earthquake motion (Fig.
135 5(b)) is applied in P-H(EQ1). For comparison, responses of the abutment without piles are
136 calculated in NP-L and NP-H.

137 The limitations of the analysis are: (1) the bridge deck and intermediate piers were not
138 modelled, and (2) the top of the abutment was free to move, without restriction, except in case
139 P-H(Fix). In other words, the dynamic interaction between the deck and the abutment was not
140 modelled, because our main concern was the interaction between the abutment, foundation ground,
141 road embankment, and river dike. As a result of these limitations, the calculated displacements
142 and vibration modes of the abutment may be different from those in a real bridge-foundation system.
143 In addition, since the only the two waveforms are considered, the observation on numerical analyses
144 in this study has to be taken as one of the examples. Even though we label one of the input
145 motions as the inland earthquake motion and the other as the subduction earthquake motion, the
146 used motions are not necessarily representative waveforms for these types of motions.

147

148 3. Observations on numerical analyses

149

150 In conventional Japanese design methods, seismic responses of an abutment are typically calculated
151 by the pushover analysis assuming that (1) the response coinciding with the arrival of a principal
152 shock represents the critical design condition for an abutment and (2) effects of the lateral spreading
153 on the abutment response are negligible. In this section, these major assumptions in the
154 conventional design methods are examined through observations on numerical analyses.

155

156 *3.1. Permanent deformation of the ground surrounding the abutment*

157 Ground deformations around the pile-supported abutment (P-L & P-H) at $t=30\text{sec}$ (when ground
158 shaking almost ceases) are drawn in Fig. 6. Large shear deformation of the loose sand deposit
159 under the abutment and the connected road embankment (the roadway for P-H) was observed in
160 both cases. In the case where the original ground level was lower than the height of the river dike
161 crest (P-L), the road embankment showed relatively large settlements, with marked uneven
162 settlement occurring just above the heel of the abutment pile cap. In addition, the shear
163 deformation of the liquefiable layer under the road embankment is somewhat smaller than for case

164 P-H.

165 The waterward horizontal displacements of the river dike far from the abutment are not affected
166 by abutment movement. The higher the original ground level, the larger the waterward permanent
167 horizontal displacement of the dike, i.e., the lateral spread. On the other hand, the deformation of
168 the river dike near the abutment are restrained by the abutment. Due to this restriction, the backfill
169 behind the abutment shows permanent horizontal displacement normal to the bridge axis (see the
170 horizontal ground displacement at the river dike's crest level, the lower graphs in Fig. 6).
171 Although the plots for the abutments without piles (NP-L & NP-H) are not shown here, they are
172 approximately the same as those for the pile-supported abutment, except for abutment tilting (large
173 tilting of the abutment was seen in NP-L & NP-H) and relative horizontal displacement between the
174 dike and the abutment (the relative displacement was not large in these cases).

175

176 *3.2. Excess pore water pressure response*

177 Although the above-mentioned permanent deformations of the abutment and surrounding
178 ground were caused by the generation of the excess pore water pressure in the loose sand deposit,
179 this does not necessarily mean that full liquefaction took place over the entire area. In P-L, the
180 loose sand just below the dike and embankment was not fully liquefied, whereas full liquefaction
181 did occur in other areas, as shown in Fig. 7. There are two possible reasons for this: one reason is
182 that the embankment (including the river dike) load on the foundation ground induced shear stress
183 in the foundation soil, increasing its strength against cyclic shear stress [11]. The other reason is
184 that the smaller overburden pressure at the original ground surface limits the excess pore water
185 pressure that can develop in the liquefiable layer, resulting in water migration from the embankment
186 foundation toward the original ground, thereby reducing the excess pore water pressure in the
187 embankment foundation.

188 The liquefiable layer under the roadway is also liquefied in P-H, since it does not meet the
189 conditions mentioned above, i.e., unlike P-L, there is no initial shear stress in the plane normal to
190 the bridge axis and no ground water migration from the embankment foundation toward the original
191 ground. For the cases on the non-pile-supported abutment (NP-L & NP-H), the excess pore water
192 pressure ratio just below the abutment is very small, compared to the pile-supported abutment, due
193 to the large confining pressure induced by the abutment weight (for the pile-supported abutment
194 cases, the weight of the abutment is supported by piles, and does not contribute to increasing the
195 confining stress of the liquefiable soil underneath the abutment.)

196

197 *3.3. Horizontal abutment displacement*

198 Figure 8 shows the time histories of the horizontal displacement of the top of the abutment for
199 all cases except P-H(Fix) (the horizontal displacement of the abutment top is constrained in that
200 case), together with the time histories of the channel-side shoulder of the dike far from the abutment
201 ($x=-5\text{m}$, $y=100\text{m}$ & $z=10\text{m}$), shown with a dashed line. Negative values of displacement represent
202 waterward abutment movement. When the inland earthquake is applied, the horizontal
203 displacement of the abutment increases with shaking; two large fluctuations in the horizontal
204 displacement time histories coincide with the two large shocks in the input motion (see Fig. 5).
205 For the subduction earthquake, P-H(EQ1), the displacement time history does not show a large
206 jump during the principal shock, and the displacement increases monotonically with the shaking.
207 The permanent displacements of the pile-supported abutments (P-L & P-H) are smaller than those
208 of the abutments without piles (NP-L & NP-H), and the higher the original ground level (for the
209 cases with the surrounding ground geometry shown in Fig. 2(b)), the larger the abutment horizontal
210 displacement. For all the cases the permanent abutment displacement is larger than the
211 displacement that occurs at the time of the principal shock.

212 The horizontal displacements of the river dike far from the abutment are not affected by
213 abutment movement (cf. (1) P-L & NP-L and (2) P-H & NP-H) as mentioned before. The higher
214 the original ground level, the larger the permanent horizontal displacement of the dike, i.e., the
215 lateral spread. The larger resistance of the abutment foundation against spreading results in a
216 larger relative displacement between the abutment and the spreading ground. In the pile-supported
217 abutment cases, the relative displacement is large, whereas it is very small for the abutments
218 without piles. Restraint of the ground around the abutment against spreading causes the forces
219 acting on the abutment to be larger, and affects the strength and ductility demands that are made on
220 the structural members.

221

222 3.4. Earth pressure acting on abutment back face

223 Figure 9 shows the time histories of the coefficient of horizontal earth pressure acting on the
224 abutment back face ($x=5\text{m}$). The coefficient is defined as an average ratio of the horizontal
225 effective stress to the vertical effective stress. Before the arrival of the principal shock, the earth
226 pressure acting on the back face of the abutment decreases slightly with increasing abutment
227 displacement. The earth pressure time histories show sharp spikes (the maximum earth pressures
228 that occurred during the entire shaking history) coinciding with the arrival of the first principal
229 shock. After the first principal shock, the earth pressure decreased to a nearly constant level when
230 subjected with the inland earthquake motion; when subjected to the subduction earthquake
231 (P-H(EQ1)), the maximum earth pressure does not coincide with the principal shock.

232 In Fig. 9, the coefficients calculated by the Mononobe-Okabe method are shown with arrows.
233 For the cases without piles (NP cases) and the pile-supported abutment case with a lower original
234 ground level (P-L), the maximum values are approximately equal to the Mononobe-Okabe values,
235 while in the P-H cases, especially when constrained against horizontal displacement (P-H(Fix)), the
236 maximum values were larger than the Mononobe-Okabe. In the former cases, the earth pressure
237 coefficient following the principal shock is smaller (close to the active earth pressure coefficient),
238 whereas it is relatively large in the latter cases. Even in the case when the top of the abutment is
239 restrained (P-H(Fix)), the values are far below potential passive earth pressures.

240 These observations are linked to the relative displacements between the abutments and the
241 spreading ground. When either (1) the abutment foundation has a small amount of restraint
242 against movement toward the waterfront (NP cases), or (2) the lateral spread is relatively small
243 because of a lower original ground level (P-L), the relative displacement is small and the
244 spread-induced component of earth pressure is also small. In these cases, the peak earth pressure
245 can be approximated by the Mononobe-Okabe method, and the earth pressure remaining following
246 shaking is small. For the cases with larger relative displacements, since the spread-induced
247 component of earth pressure is relatively large, the peak earth pressures can be larger than the
248 Mononobe-Okabe value.

249 When the seismic performance of a pile-supported bridge abutment is analyzed with the
250 conventional Japanese design methods, the response coinciding with the arrival of the largest
251 (principal) shock is generally assumed to represent the critical design condition for the abutment.
252 However, our observations have shown that the horizontal displacement of the abutment coinciding
253 with the principal shock is not necessarily the maximum displacement the abutment will experience.
254 These observations underscore the importance of taking into account the permanent deformations of
255 the surrounding ground.

256

257 *3.5. Bending moment of piles*

258 Bending moment diagrams for the piles, corresponding to the time when the abutments
259 experience maximum earth pressure, are plotted in Fig. 10 (for P-L, P-H, PH(Fix) & P-H(EQ1)).
260 Envelopes of the maximum and minimum bending moment are also shown, with dashed lines, in
261 the figure, along with the bending moment at the end of the shaking. These diagrams show the
262 average moment of the pile group, because there is very little variation between the moments in all
263 the piles in the group. In every case, the large bending moment occurs at the pile head ($z=0\text{m}$) and
264 at the interface between the liquefiable and non-liquefiable layers ($z=10\text{m}$). When the abutment
265 top is constrained against horizontal displacement (P-H(Fix)), the maximum and minimum bending

266 moments are very small compared to the moments in the unconstrained abutments.

267 For the cases subjected to the inland earthquake motion, the maximum earth pressure acting on
268 the back face of the abutment occurs at $t=10.88\text{sec}$ (cf. Fig. 9), and the inertia force of the abutment
269 reaches its maximum value slightly before this time. For the case with the subduction earthquake
270 motion, P-H(EQ1), the maximum earth pressure during the principal shock appears at $t=27.52\text{sec}$,
271 which almost coincides with the maximum inertia force of the abutment, while the maximum
272 throughout the shaking is at $t=37.60\text{sec}$. This is probably due to semi-long-period components of
273 input motion that follows the principal shock (a wave undulation with a period of about 2~3sec can
274 be seen following the principal shock in Fig. 5(b)). The fluctuation in the earth pressure induced
275 by this semi-long-period component of input motion, along with the forces that have already been
276 induced by significant lateral spreading, may have put the piles into a critical stress condition for
277 the case with the subduction earthquake motion.

278 For all the cases, when the earth pressure acting on the abutment is maximum, the bending
279 moment at $z=0\text{m}$ and $z=10\text{m}$ is approximately equal to the maximum and minimum bending
280 moments that occur throughout the shaking. For cases in which the maximum earth pressure
281 acting on the abutment back face occurs at about the same time that the maximum inertia force
282 occurs, (i.e., the cases with the inland earthquake motion), the critical bending moment in the piles
283 coincides with the maximum inertia force; however, this is not true for the subduction earthquake
284 case.

285 These results suggest that for the inland earthquake, critical pile bending moments can be
286 determined by the pushover analysis (even though maximum abutment displacements cannot be
287 determined by conventional methods). But when the critical bending moment in the piles is
288 caused by lateral spreading that occurs after the principal shock (such as in the subduction
289 earthquake with a relatively small peak motion but with a duration long enough to cause lateral
290 spreading), neither the maximum pile bending moments nor the maximum abutment displacements
291 can be assessed with the pushover analysis.

292

293 4. Forces acting on the abutment

294

295 The numerical analyses reveal that when the earth pressure acting on the back face (not the
296 inertia force) of the abutment is maximum, the piles are experiencing their critical strength/ductility
297 demand, even though the horizontal displacement of the abutment may not have reached its
298 maximum value yet. Although the maximum earth pressure occurs at the same time as the critical
299 bending moment in the piles, this does not necessarily mean that the earth pressure acting on the

300 back face of the abutment is the cause of the critical bending moment in the piles. In this section,
301 other components of the forces acting on the abutment are examined, in order to identify relevant
302 forces dominating bridge abutment response for conventional seismic design methods.

303 With regard to spreading soils, the abutment acts as a restraint against lateral spread; in other
304 words, the forces acting on the abutment are the result of interaction between the spreading soils
305 and the pile foundation. The NCHRP 472 Recommended Specifications for Seismic Design of
306 Bridges [12][13] implemented this concept by formulating a simplified procedure for calculating
307 the response of an abutment over liquefied ground, and Boulanger et al. [14] applied this procedure
308 to a physical model test. First, we will present the analysis results in a form similar to that used in
309 the NCHRP 472, and then we will analyze the contribution of each component of the force acting
310 on the abutment.

311 Figure 11 shows plots of the average foundation resisting forces, F_R/B , against the horizontal
312 displacement of the abutment base for P-L, P-H, P-H(EQ1), NP-L & NP-H. For the abutments
313 without piles, the resisting force is calculated by integrating the shear stress on the foundation base
314 caused by frictional resistance. The resisting force of the pile-supported abutments is determined by
315 summing the shear forces at the pile heads (the frictional resistance of the foundation soil is
316 negligible for these cases). The average resisting force corresponds to the foundation resistance
317 per unit width of the abutment. The points at the end of shaking are indicated by triangles, and the
318 times of the maximum earth pressure acting on the abutment back face is shown by double circles.

319 For the cases subjected to the inland earthquake motion (P-L, P-H, NP-L & NP-H), the
320 foundation resisting forces act to restrain the spreading soils. Therefore, the larger the foundation
321 resisting force, the smaller the permanent abutment displacement, as shown in the figure. The
322 chain lines in the figure represent the abutment displacement curves subjected to various restraining
323 forces, and the triangles correspond to points where the displacement of the pile foundation and the
324 abutment are compatible.

325 The foundation resistance coinciding with the maximum earth pressure acting on the back face
326 of the abutment (the double circle points) does not seem to depend on the geometry of the
327 surrounding ground, but instead depends on the foundation type. However, the backbone curve
328 depends on both ground geometry and foundation type, for the cases subjected to the inland
329 earthquake motion. The slope of the backbone curves decreases with shaking, that is, it decreases
330 with the relative displacement. The average shear forces are plotted against the horizontal pile
331 displacement at a depth of 8.75m (just above the interface between the liquefiable and
332 non-liquefiable layers) for P-L, P-H & P-H(EQ1), shown in Fig. 12. These figures indicate that
333 the decrease in the slope of the backbone curve that takes place as the shaking progresses may be

334 caused by softening of the soils in both the liquefiable layer and in the bottom non-liquefiable layer,
335 due to the cyclic shearing of the soil surrounding the piles. This cyclic softening effect in a soil
336 layer lying beneath a liquefiable layer is not ordinarily considered in pushover analyses, which
337 might, therefore, underestimate actual abutment displacements.

338 Comparisons between Figs. 11 and 12 bring to light the following points: (1) large changes in
339 the shear force at the pile head during the first shock are not seen in the vicinity of the interface
340 between the liquefiable and non-liquefiable layers, for the cases with the inland earthquake motion,
341 and (2) after the principal shock, the shear forces near that interface are slightly larger than the shear
342 forces at the pile head. The first observation indicates that the dynamic load delivered by the pile
343 heads during the first shock is resisted primarily by the liquefiable layer, and is not transmitted to
344 the bottom non-liquefiable layer. Figure 13 shows the stress paths of the liquefiable soil element
345 adjacent to the piles ($x=1.25\text{m}$, $y=3.75\text{m}$ & $z=-6.25\text{m}$) for P-L & P-H. The large resistance of the
346 liquefiable layer at that point in time may be attributed to the dilative behaviour of the soil, as
347 shown in Fig. 13. The latter observation illustrates the existence of the waterward lateral forces
348 against the piles at the liquefiable layer, due to the lateral spread. Although this is not insignificant,
349 we will not discuss this phenomenon any further, because our main concern here is the forces acting
350 on the abutment.

351 The foundation resisting force, $F_R = F_I + (F_B - F_F) + 2F_S$ is a reaction to the forces acting on the
352 abutment (see Fig. 14) where F_B is the forces acting on the back face of the abutment, F_F on the
353 front face, F_S on the side faces, and F_I is the inertia force. All forces except F_I are affected not
354 only by dynamic soil-structure interaction, but also by the spreading soils. Examining the
355 contributions of these forces to the abutment response is of value for purposes of improving the
356 current design method, because identification and consideration of the relevant factors dominating
357 bridge abutment response is important in the simplified design methods. This is of value not only
358 for performance assessment of the foundation itself, but also for assessing the soils surrounding the
359 abutment, since these forces are also acting to restrain the spreading soils.

360 Changes of the forces mentioned above for P-H are shown in Fig. 15. The inertia force
361 dominates the group of forces acting on the abutment during the principal shock. The forces
362 acting on the back face and side faces of the abutment increase with shaking, but the forces on the
363 front face decrease. Similar plots for NP-H are shown in Fig. 16. In this case, the forces acting
364 on the side faces are negligible. Changes in the sum of these forces, and (1) changes in the shear
365 forces acting at the pile head for P-H, or (2) changes in the integrated shear stress of the foundation
366 soil for NP-H, are plotted in the bottom of the figures. Since, (1) the force acting on a face of the
367 abutment is calculated by integrating the stresses in the soil elements that contact the abutment face

368 of interest, and since (2) the shear force in the beam element connected to the abutment base is
369 affected by the nodal forces acting on the opposite side of the pile heads, these forces were not
370 exactly identical, although they were of the same order of magnitude (with an error of about 20%).
371 Therefore, the contribution of each force acting on the abutment was determined by proportion, so
372 that the contributing forces add up to the total force.

373 Table 3 summarizes contribution ratios of the forces acting on the abutment at the time the
374 maximum earth pressure acting on the abutment back face occurs, for P-L, P-H, P-H(EQ1), NP-L &
375 NP-H. For the cases with the inland earthquake, the inertia force is the dominant force acting on
376 the abutment base. The contribution of the force acting on the abutment side face is very small for
377 the pile-supported abutments (P-L & P-H), while it is relatively large for the abutments without
378 piles (NP-L & NP-H). For the case of the subduction earthquake, P-H(EQ1), the ground has
379 already been subjected to number of shearing cycles before arrival of the large earth pressure acting
380 on the back face. This results in a smaller inertia force, and the other components contribute more
381 to the total force acting on the abutment base.

382 A similar summary for the end of shaking is shown in Table 4. For the pile-supported
383 abutment, the contributions of the forces acting on the abutment back face and front face ($F_B - F_F$)
384 are the greatest, but there are also significant contributions of force from the side faces, especially
385 when the original ground level is high (P-H & P-H(EQ1)). However, the force acting on the side
386 faces is negative (the adjacent river dike behaving as a resistance) for the cases without piles and its
387 absolute value is larger for the case with the lower original ground level (NP-L). This is related to
388 the relative displacement between the abutment and the spreading ground at the end of shaking, i.e.,
389 the larger the relative displacement, the larger the contribution of the force acting on the side faces
390 (cf. Fig. 8). Figure 17 is a plot of the forces acting on the side faces against the relative
391 displacement between the abutment and the spreading ground, for all the cases. The coefficient of
392 the force acting on the side faces is defined as a ratio of F_S to $\int_0^H L(z)\rho'gdz$, where z =depth from
393 the abutment top, $L(z)$ =length of abutment in the bridge axis direction at a depth of z (i.e., the
394 average ratio of the shear stress to the initial vertical stress). The force is uniquely related to the
395 relative displacement, and its upper limit seems to be a coefficient of about 0.5 in this study.

396 These observations suggest that, (1) the inertia force dominates the force acting on the
397 abutment base when the peak of an earthquake motion arrives before occurrence of the major
398 spreading of the surrounding ground, (2) the greater the restraining force of the abutment
399 foundation, i.e., the larger the relative displacement between the abutment and spreading ground,
400 the larger the contribution of the force acting on the abutment side faces until the side drag force

401 reaches its ultimate value. Conventional design methods employing the pushover analysis for the
402 abutment response calculation could underestimate permanent abutment displacements, unless (1)
403 the softening of the soil in the layers beneath the liquefiable layer, caused by the cyclic shearing of
404 the soils surrounding piles, and (2) the force acting on the abutment side faces, are taken into
405 account. Due consideration of these factors is recommended in order to realistically assess
406 permanent abutment displacements.

407

408 5. Conclusions

409

410 This paper presents the results of dynamic three-dimensional finite element analyses of bridge
411 abutments adjacent to a river dike, including the effect of liquefaction of the underlying ground
412 using earthquake motions widely used in Japan. We examined the validity of assumptions in the
413 conventional design methods with the pushover analysis and identified the factors dominating the
414 abutment response through the numerical analyses. Based on the analysis results and discussion,
415 the following conclusions can be drawn:

- 416 (1) The permanent displacements of pile-supported abutments in liquefied ground are smaller
417 than the displacements of abutments without piles, as expected. Irrespective of the
418 foundation type and elevation of the ground behind the river dike, the abutment
419 displacement that occurs with the principal shock of an earthquake is not the maximum
420 displacement; the final abutment displacement following the earthquake will be larger.
- 421 (2) The piles supporting the abutment are structurally critical at the time of the maximum earth
422 pressure acting on the back face of the abutment for both the inland earthquake and the
423 subduction earthquake, even though the dynamics of these two types of earthquakes are
424 completely different. For the inland earthquake, the maximum earth pressure coincides
425 with the peak of the principal shock of the earthquake. At that time, the piles are in a
426 critical condition, because the inertia force that dominates the forces acting on the abutment
427 (about 70%) is close to the maximum. For the subduction earthquake, the major lateral
428 spreading has already started before the peak earthquake motion arrives, and the forces
429 induced by soil spreading (about 80%) overshadow the maximum inertia force (about 20%).
430 A semi-long-period component of input motion following the principal shock causes large
431 fluctuations in the earth pressure. This fluctuation, along with the forces that have already
432 been induced by significant lateral spreading, puts the piles into a critical stress condition
433 when this type of earthquake is considered.
- 434 (3) The foundation resisting force is a reaction to the combined forces acting on the abutment,

435 including the forces acting on the abutment back face, on the front face, on the side faces,
436 and the inertia force. Except for the inertia force, these forces are affected by the soil
437 spreading. The forces acting on the back face and side faces of the abutment increase as the
438 relative displacement between the abutment and spreading ground far from the abutment
439 increases. The contribution of the force acting on the side faces increases along with this
440 relative displacement. In this study, the force acting on the sides faces at the end of
441 shaking is around 30-40% for pile-supported abutments, whereas this same force is
442 negligible or negative (acting as resistance for the abutment) without piles.

443 (4) Conventional design methods employing the pushover analysis could underestimate the
444 permanent abutment displacement unless (1) the softening of the soil in the layers beneath
445 the liquefiable layer, due to the cyclic shearing of the soil surrounding the piles, and (2) the
446 force acting on the abutment side faces, are taken into account. Inclusion of these factors is
447 recommended for assessing permanent abutment displacements.

448

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483
484 Table 1: Material parameters
485 (a) For soil layers

Parameter	Non-liquefiable layer (Dense sand deposit)	Liquefiable layer (Loose sand deposit)	Surface layer
G_s	2.65	2.68	2.68
e_0	0.65	0.85	0.85
κ	0.00054	0.00090	0.00090
λ	0.0072	0.019	0.019
ν	0.333	0.333	0.333
ϕ	41.3°	38°	38°
ϕ_d	27°	27°	27°
μ	0.5	1.0	0.0
ϕ_b	19.5°	19.5°	19.5°
b_r	2000	400	400
u_l	2	2	2
m_l	1	1	1
c	10	30	30
K_0	0.5	0.5	0.5
s_{ij0}	$0.7\sigma_{ij0}$	$0.2\sigma_{ij0}$	$0.2\sigma_{ij0}$
OCR	16	2	2
k (m/s)	5×10^{-4}	5×10^{-4}	–

486
487 (b) For abutment

Parameter	ρ (Mg/m ³)	EI (GN.m ²)	EA (GN)	E (GPa)	ν
Pile	2.5	4.2	79	–	–
Abutment	2.5	–	–	21	0.3

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489

490 Table 2: Analysis conditions

Case	Abutment	Ground level from riverbed*	
P-L	w/ piles	5m	
P-H	w/ piles	10m	
P-H(Fix)	w/ piles	10m	Horizontal displacement of abutment top is constrained.
P-H(EQ1)	w/ piles	10m	Spectrum I earthquake motion (Fig. 5(b)) is applied.
NP-L	w/o piles	5m	
NP-H	w/o piles	10m	

491 * Geometry of surrounding ground for 5m is illustrated in Fig. 2(a) and that for 10m is in Fig.2(b).

492
493 Table 3: Contribution ratios of the forces acting on the abutment at time of maximum earth pressure
494 acting on abutment back face

Case	P-L	P-H	NP-L	NP-H	P-H(EQ1)	
Time: sec			10.88			27.52* ¹ 37.60* ²
$(F_B - F_F)/F_R$	25%	24%	19%	25%	54%	57%
$2F_S/F_R$	3%	6%	8%	12%	25%	36%
F_I/F_R	73%	70%	73%	64%	21%	7%

495 *1: At time of maximal earth pressure during principal shock

496 *2: At time of maximum earth pressure throughout shaking

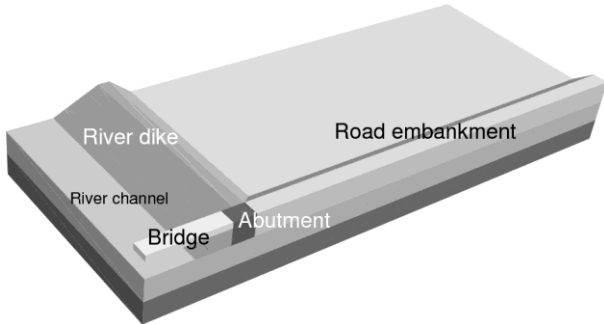
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498 Table 4: Contribution ratios of the forces acting on the abutment at end of shaking

Case	P-L	P-H	NP-L	NP-H	P-H(EQ1)
$(F_B - F_F)/F_R$	72%	59%	142%	105%	61%
$2F_S/F_R$	28%	41%	-42%	-5%	39%

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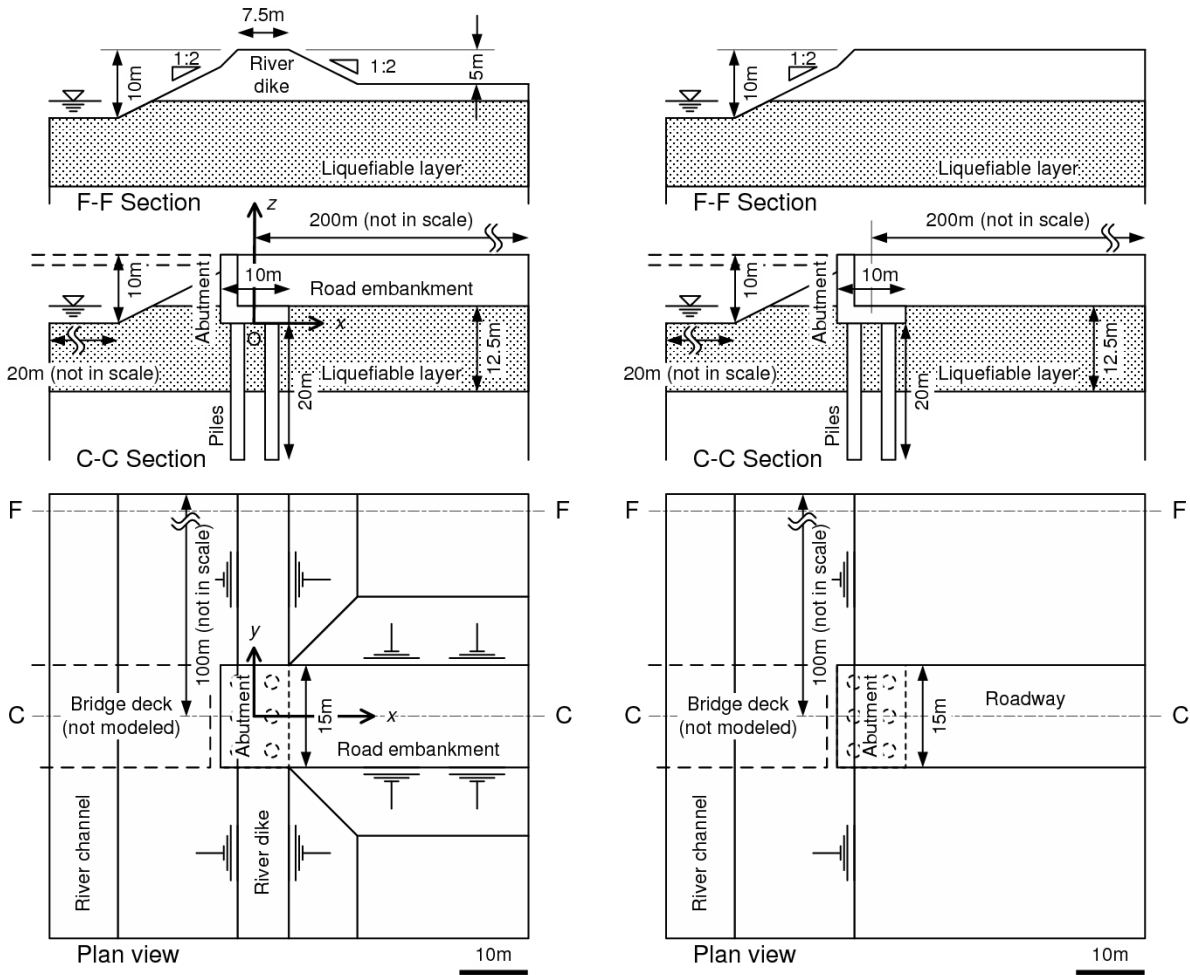


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Fig. 1: Bird's eye view of abutment for river crossing bridge



(a) Ground level is at a height of 5m above riverbed (P-L & NP-L)

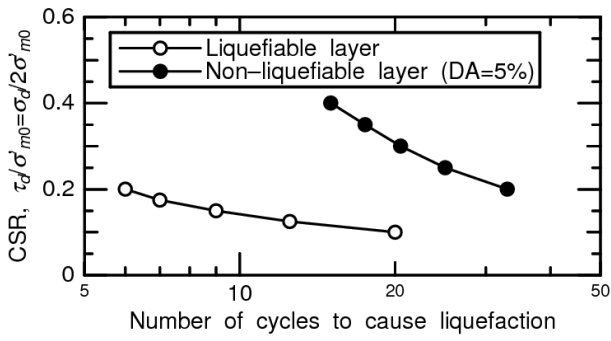
(b) Ground level is at a height of 10m above riverbed (P-H & NP-H)

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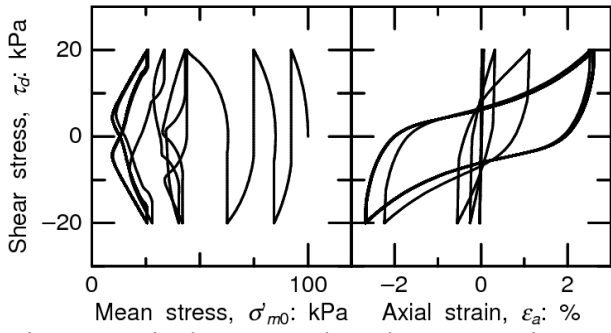
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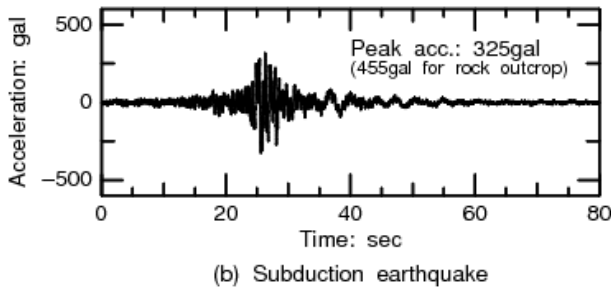
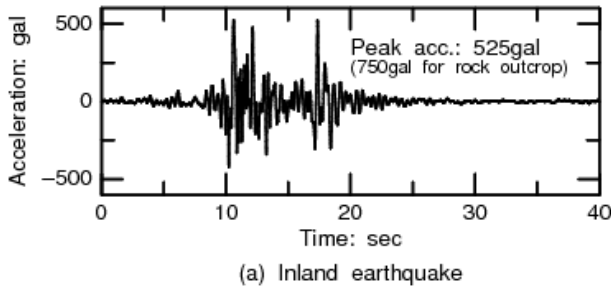
Fig. 2: Plan views and cross sections of target abutments



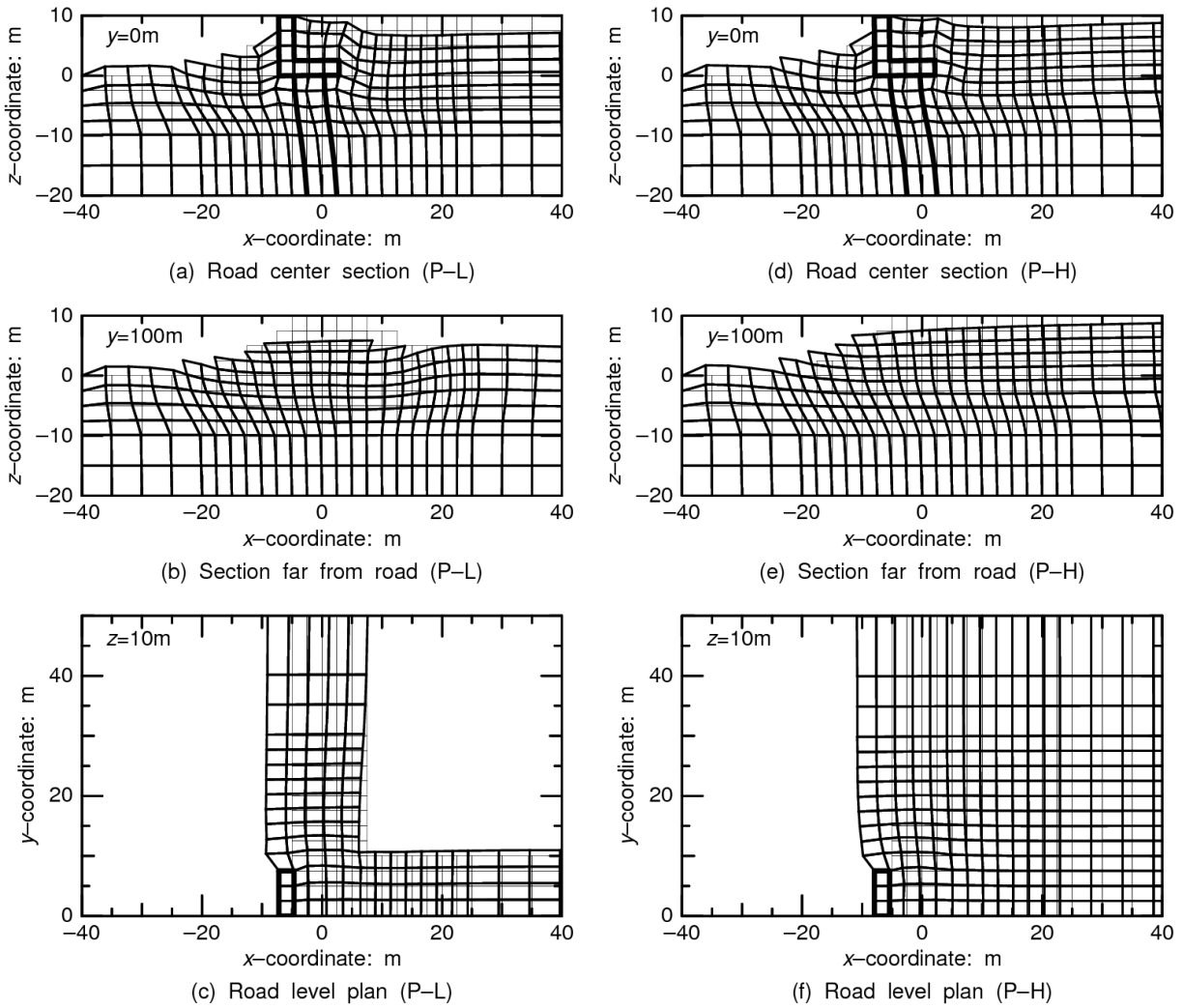
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508 Fig. 3: Relationship between cyclic stress ratio and number of cycles to cause liquefaction
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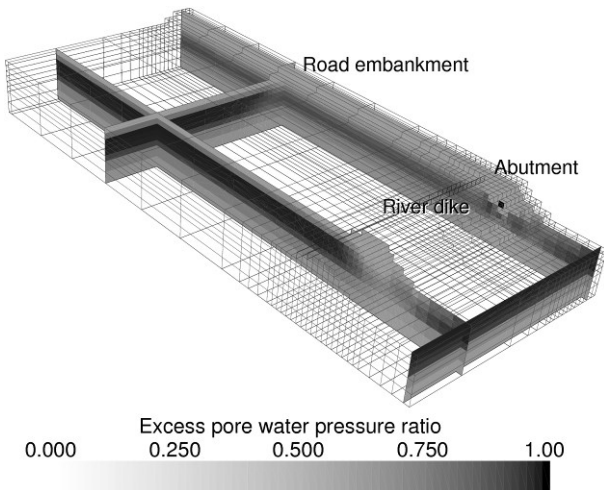
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511 Fig. 4: Typical stress path and stress-strain curves for liquefiable layer soil
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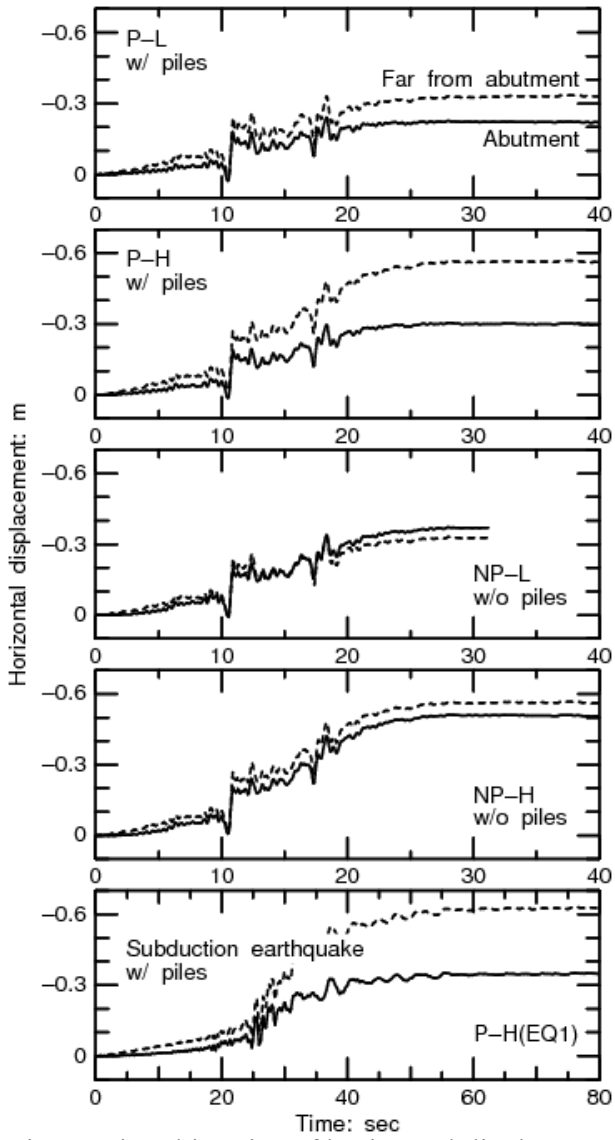
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514 Fig. 5: Applied earthquake motion time histories
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 517 Fig. 6: Ground deformations around piled abutment, where displacement scale is magnified by a
 518 factor of ten for P-L (Left) and P-H (right) at $t=30\text{sec}$
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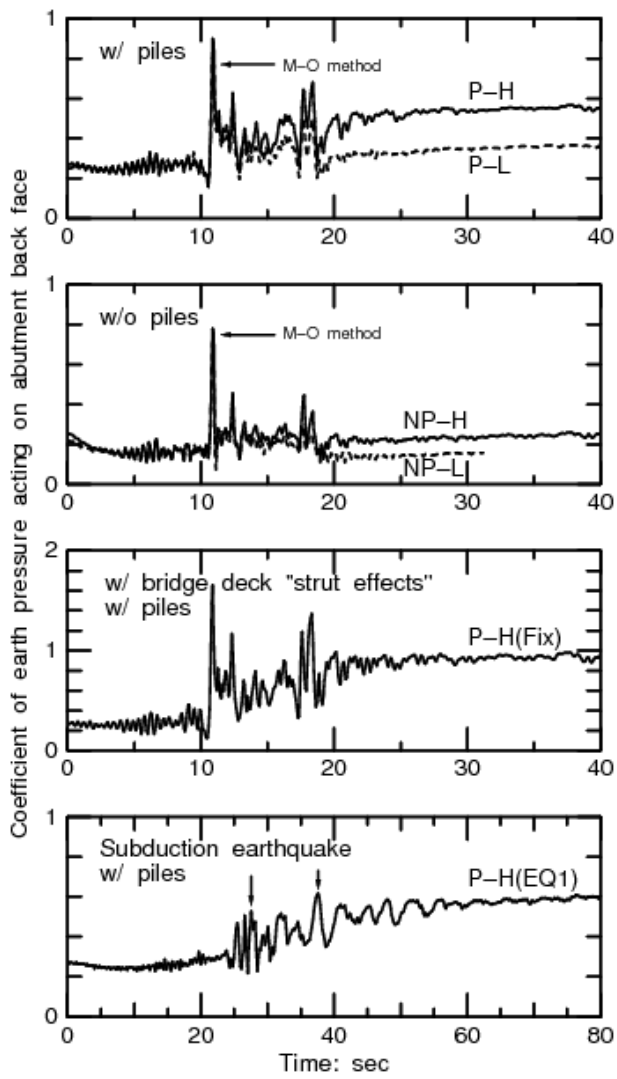


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 521 Fig. 7: Excess pore water pressure ratio contours at $t=20\text{sec}$ for P-L
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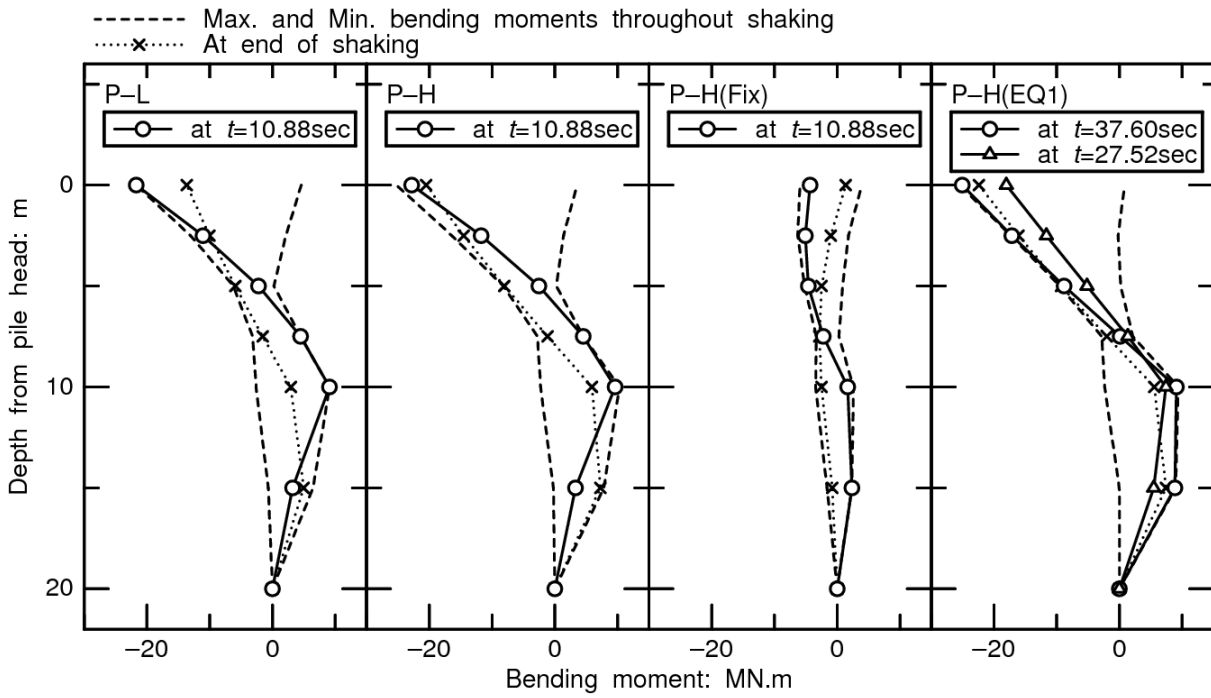


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Fig. 8: Time histories of horizontal displacement of abutment top

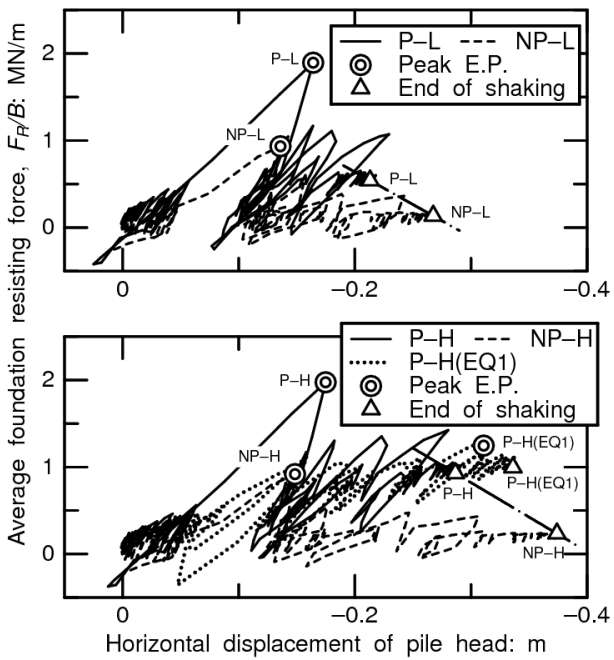


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 528 Fig. 9: Time histories of coefficient of earth pressure acting on abutment back face
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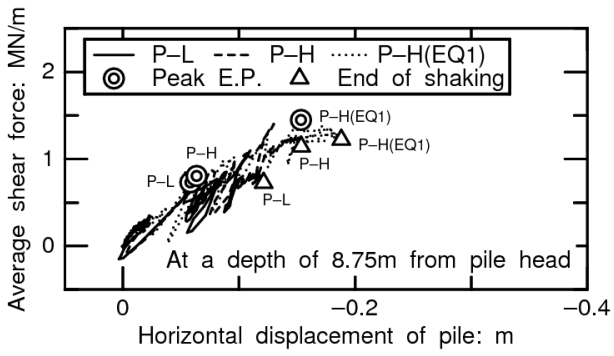
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Fig. 10: Distributions of pile bending moment at time of maximum earth pressure acting on abutment back face



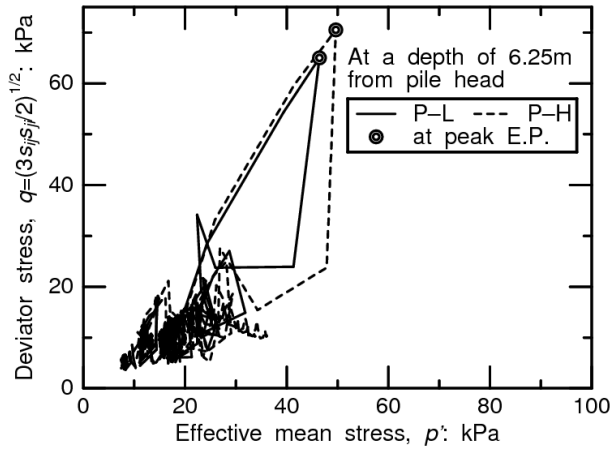
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Fig. 11: Average foundation resisting forces versus horizontal displacement of abutment base



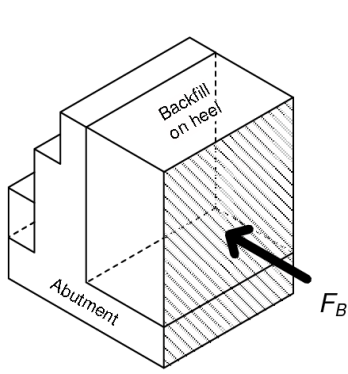
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Fig. 12: Average shear forces versus horizontal displacement of piles at a depth of 8.75m

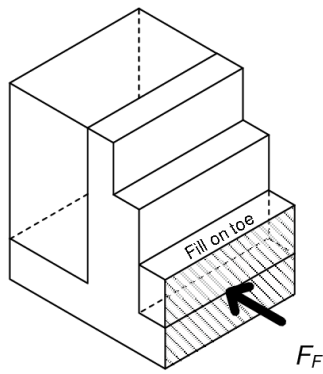


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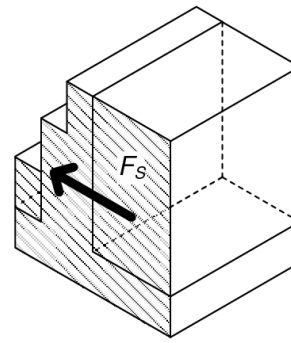
Fig. 13: Stress paths of liquefiable soil element adjacent to pile ($x=1.25m$, $y=3.75m$ & $z=-6.25m$) for P-L & P-H



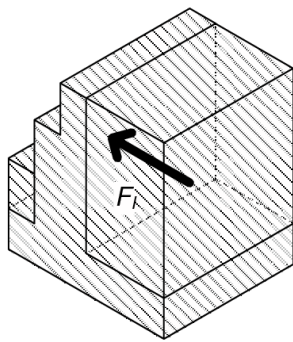
(a) Force acting on back face



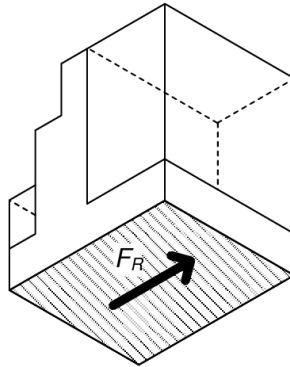
(b) Force acting on front face



(c) Force acting on side face



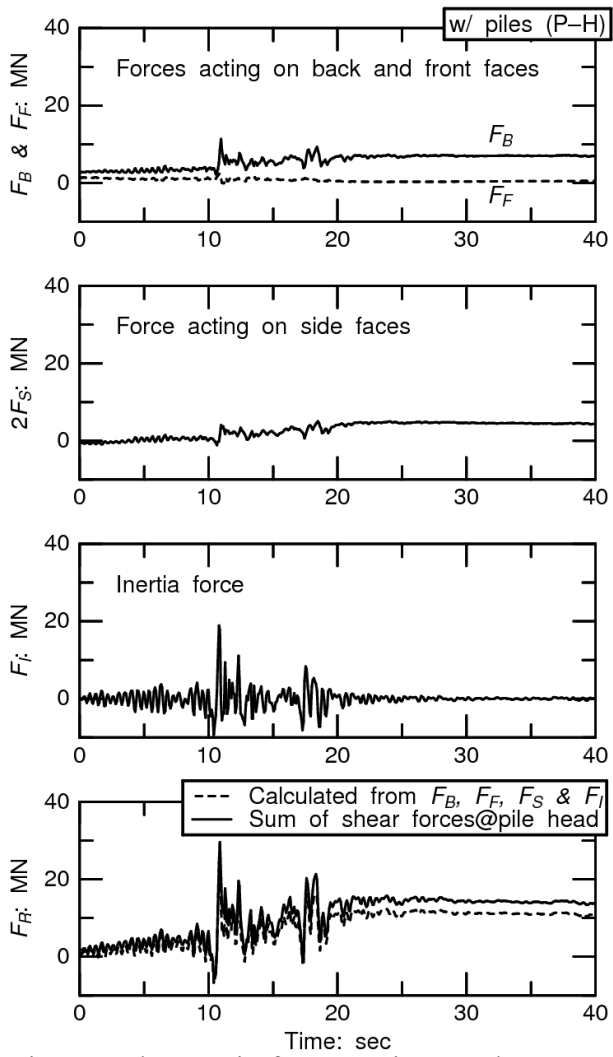
(d) Inertia force



(e) Horizontal reaction at base

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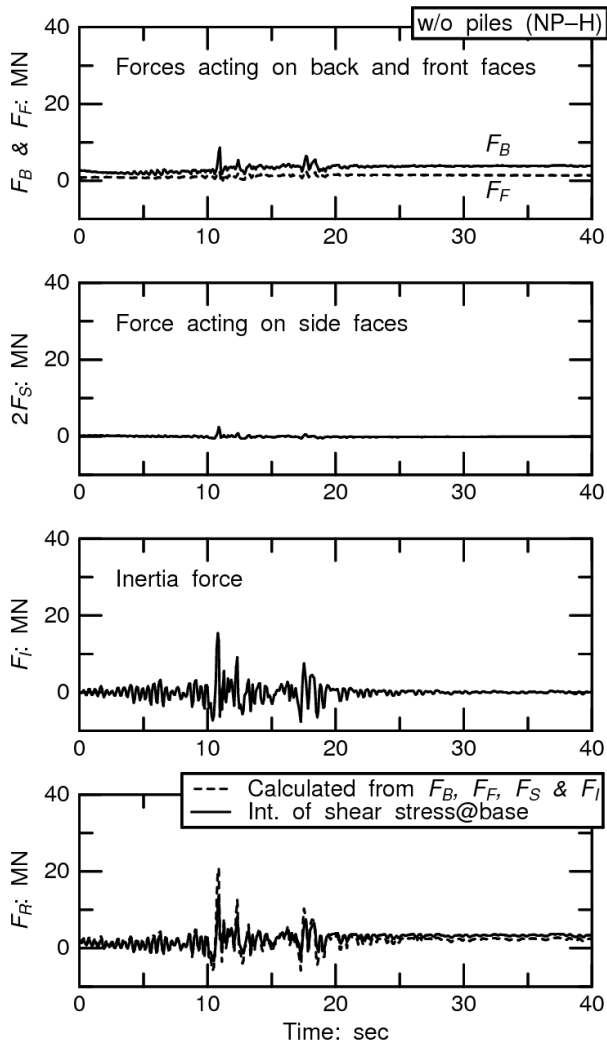
Fig. 14: Forces acting on abutment



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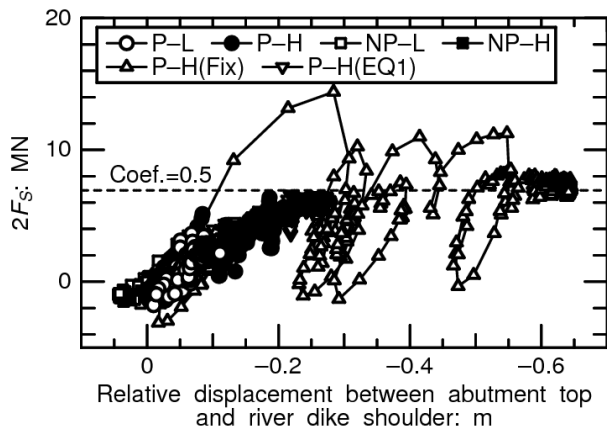
Fig. 15: Changes in forces acting on abutment for P-H

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Fig. 16: Changes in forces acting on abutment for NP-H



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Fig. 17: Forces acting on abutment side faces against relative displacement between abutment and spreading ground