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1 **Triaxial erosion test for evaluation of mechanical consequences of internal erosion**

2
3 Lin Ke and Akihiro Takahashi*

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7 Lin Ke

8 Graduate student, Department of Civil Engineering,

9 Tokyo Institute of Technology, Japan

10 E-mail: ke.l.aa@m.titech.ac.jp

11
12 Akihiro Takahashi*

13 Associate Professor, Department of Civil Engineering

14 Tokyo Institute of Technology, Japan

15 E-mail: takihiro@cv.titech.ac.jp

16 * Corresponding author

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28 **1 Introduction**

29

30 It is universally recognized that seepage-induced erosion would lead to catastrophic
31 consequences: approximately half of the dam failures are due to soil erosion (Richards
32 and Reddy, 2007). The phenomenon that those valleys on catchment topography, which
33 may have been suffered from years of internal erosion, were vulnerable to fail during
34 Noto Peninsula Earthquake of Japan in 2007 raises the concern about the possible
35 influence of internal erosion on the soil microstructure change and, consequently, the
36 strength change. The gap-graded soils, like sandy gravels or silty sands, are especially
37 vulnerable to internal erosion because of their deficiency in certain grain size
38 (Skempton and Brogan, 1994). Due to the inconformity of the definition of soil erosion
39 in literature, the common term “internal erosion” is used here to describe the target
40 phenomenon that small grains are eroded through the voids between the coarse grains
41 by seepage flow. It develops chronically, usually accompanying with a great quantity of
42 seepage flow over years. Meanwhile, during the internal erosion, there are dramatic
43 changes in soil porosity and hydraulic conductivity. Muir Wood *et al.* (2010) proposed a
44 theoretical model to evaluate the mechanical influence of internal erosion and
45 concluded that the soil strength would decrease if significant amounts of fine grains
46 were removed. Chang and Zhang (2011) experimentally proved this conclusion by a

47 series of drained compression tests on the gap-graded cohesionless soil. It was found
48 that the originally dilative soil would become contractive after internal erosion.

49

50 Although internal erosion is such a huge potential risk for the earth structure safety,
51 hitherto, few laboratory tests have been fully developed to comprehensively assess the
52 mechanical consequences of internal erosion on gap-graded sands by taking account of
53 both monotonic and cyclic loadings. One of the main difficulties lies in guaranteeing a
54 high saturation degree in soil specimens during erosion test, which can be hardly
55 fulfilled in a conventional apparatus. Without a comparatively high saturation degree,
56 laboratory tests on those internally eroded soils might not be well performed. Moreover,
57 since internal erosion is chronic phenomenon, it would be better if the laboratory
58 erosion tests could last for relatively long period. Upon those difficulties, this paper
59 presents a newly developed triaxial seepage apparatus, capable of maintaining back
60 pressure in a soil specimen during erosion test and directly obtaining the mechanical
61 response of internally eroded soils. Preliminary test results, including drained
62 monotonic tests, undrained monotonic tests and undrained cyclic tests on internally
63 eroded soil, are discussed by comparing them with the mechanical responses of the
64 specimens without erosion.

65

66 **2 Critical Reviews of Available Internal Erosion Tests**

67

68 The well-known standardized laboratory tests for soil erosion are pinhole test ([ASTM](#)
69 [D4647/D4647M-13](#)) and the double hydrometer test ([ASTM D4221-11](#)), developed by
70 [Sherard *et al.*](#) and [Decker *et al.*](#) respectively in the 1970s. The purpose of those tests is
71 to identify the dispersive clay in soils, which are highly prone to internal erosion. The
72 recently developed laboratory tests to study the soil erosion of cracks include slot
73 erosion test (SET) and hole erosion test (HET) ([Wan and Fell, 2004a and 2004b](#); [Bonelli](#)
74 [et al., 2006](#); [Haghighi et al., 2013](#)), which could determine the erosion rate, the
75 minimum hydraulic shear stresses to initiate piping erosion, and their relationships to
76 the soil properties. SET and HET are mainly served for the dam risk assessment.
77 [Indraratna et al. \(2013\)](#) developed the Process Simulation Apparatus for Internal Crack
78 Erosion (PSAICE) to assess the erosion rate of a sandy soil with cracks at different
79 hydraulic gradients. For practical purpose, several other test methods have been
80 proposed to evaluate the soil erosion potential in channels/canals or around the
81 soil-structure surface, including flume test ([Arulanandan and Peery, 1983](#)), jet erosion
82 test ([Moore and Masch, 1962](#)), rotating cylinder test ([Moore and Masch, 1962](#)) and
83 erosion function test ([Briaud et al., 2001](#))

84

85 The phenomenon that the base soil that satisfies the geometrical criteria may fail due to
86 erosion of fine grains, discovered in the base soil and filter compatibility studies
87 inspired the laboratory test on those “poor graded” soils, such as gap-graded or coarse
88 widely graded soils. In those experimental investigations, not only the soil geometric
89 characteristics, but also the influence of flow velocity, flow direction, hydraulic gradient
90 and possible chemical reaction is taken into consideration. The main apparatus
91 comprises a permeameter cell together with the transducers for the measurement of pore
92 water pressure spatial variations and effective stress distribution along the specimen. To
93 prevent the formation of large seepage channels along the fixed-wall, an extra layer,
94 such as a compressive rubber layer or a silicon grease layer against the inside wall is
95 necessary. The permeameter cell is usually transparent in order to record the process of
96 internal erosion by either microscopic or visual observation. For those cases conducted
97 with external loading, the permeameter cell is mounted into a reaction frame to
98 accommodate an axial loading system. Vertical effective stress on the top surface is
99 calculated from axial force of the loading rod. A displacement transducer mounted on
100 the loading rod monitors the axial displacement. The tested soils are either above one
101 filter layer or sandwiched between two filter layers.

102

103 Controlled seepage flow is necessary for internal erosion test. Occasionally, a light

104 vibration is also applied on soil sample to ensure full erosion. The seepage flow is
105 usually unidirectional, either upward or downward, which is generated by the hydraulic
106 pressure difference between the top and bottom of a specimen. In the earlier
107 experiments, the inlet hydraulic pressure is maintained by a constant-water-head tank
108 while the outlet is open to atmosphere or connected to another constant-water-head tank.
109 The flow rate is estimated by measuring the volume of discharge effluent per minute by
110 a cylinder. To overcome the possible errors in the constant head control system, several
111 improvements have been applied. [Tanaka and Toyokuni \(1991\)](#) maintained the constant
112 upstream water head by one stabilization tube and one overflow tube. [Tomlinson and](#)
113 [Vaid \(2000\)](#) kept the hydraulic head at the inlet by throttling a valve open to the water
114 supply pressure while that at the outlet is maintained by submerging the permeameter
115 into a large water bath with a constant water head. Flow rate is monitored by the volume
116 of effluent out of the water bath. The water circulation system is usually adopted in
117 experiments as well. [Lafleur \(1984\)](#) recirculated the water by means of a system of
118 solenoid valves that ensured refilling of the upstream tank when it was empty. [Kenney](#)
119 [and Lau \(1985, 1986\)](#) pumped the water in the effluent tank back to upper water tank to
120 fulfill the circulation of seepage water. However, those systems could not reach the
121 comparatively high hydraulic gradient that is usually necessary to initiate internal
122 erosion in soils subjected to surcharge. Two pressurized storage reservoirs, namely

123 influent and effluent reservoirs, are introduced as inflow and outflow tank to obtain the
124 larger hydraulic gradient. To prevent the dissolution of air into water, which might lead
125 to great errors in erosion test, each tank has an internal membrane acting as an
126 air-over-water interface. The water temperature in the storage reservoir and inlet/outlet
127 tanks keeps at constant temperature ($20\pm 1^\circ\text{C}$).

128

129 The eroded soil collection system is of great significance for the internal erosion test. In
130 case of non-cohesive soil, for the downward flow test, the eroded soil is collected at the
131 base of a permeameter. A drainage system, such as a silicon hose directed by a conical
132 trough, is better to be included to prevent the possible clogging. For upward flow test, a
133 gentle air flow through a thin tube at the top of the sample could be applied to avoid the
134 sedimentation of the eroded grains (Sterpi, 2003). With regard to those cases with
135 difficulties in installing the soil collection system, especially for the upward flow test, a
136 graphical method proposed by Kenney and Lau (1985) could be used to approximately
137 assess the fraction of eroded fine grains as well as the largest eroded fine grains based
138 on the amounts of movements of grain size distribution curves after erosion (Wan,
139 2006). In case of cohesive soil, a flow-through turbidimeter could be connected to the
140 outlet pipe to assess the eroded soil mass (Bendahmane *et al.*, 2008; Marot *et al.*, 2011).

141

142 The weakness of the commonly used fixed-wall permeameters in the laboratory
143 investigations is the sidewall leakage, which may result in great errors in calculating
144 hydraulic conductivity. The flexible-wall permeameters, on the other hand, could
145 minimize the leakage and permit applying back pressure to improve the saturation
146 degree of tested specimens. By controlling the vertical and confining pressure, the
147 vulnerability of soils to internal erosion could be tested under various stress states. Due
148 to those merits, recent erosion tests are performed in a revised triaxial cell. [Richards and](#)
149 [Reddy \(2010\)](#) developed a true triaxial piping test apparatus to assess the backwards
150 erosion potential of a wide range of soils, particularly non-cohesive soils, at various
151 stress states. The apparatus mainly consisted of the true triaxial load cell, capable of
152 applying a range of mutually perpendicular pressures, inlet-outlet pressure control panel,
153 an inlet-flow control panel, turbidimeter and several pressurized vessels. It is worth
154 stressing that the key component of erosion triaxial test is the eroded soil collection
155 system, the design of which should ensure the eroded soil grains are perfectly collected.
156 [Bendahmane et al. \(2008\)](#) studied the influence of hydraulic and mechanical
157 characteristics of cohesive soils on internal erosion in a developed triaxial apparatus. A
158 drainage system was added at the bottom of the cell. The soil erosion rate was estimated
159 through a photo sensor. [Shwiyhat and Xiao \(2010\)](#) studied the changes in soil hydraulic
160 conductivity and soil volume induced by internal erosion. The base pedestal of the

161 triaxial apparatus was modified to allow discharge effluent and eroded soil grains to be
162 captured in an effluent tank. Similarly, [Chang and Zhang \(2011, 2013\)](#) investigated the
163 internal erosion potential of gap-graded sands subjected to multi-step seepage flow and
164 conducted drained compression test on those eroded sands. The eroded soil grains were
165 collected by a detachable container at regular intervals.

166

167 The above-mentioned triaxial erosion tests are mostly hydraulic gradient controlled type.
168 By imposing hydraulic pressure on a soil specimen, the internal erosion could initiate if
169 the critical hydraulic gradient is reached. The inlet hydraulic pressure is usually
170 maintained by a pressurized water tank and the outlet is open to the atmosphere. Under
171 this circumstance, the test time is strictly restricted by the volume of the water tank.
172 However, since internal erosion is a chronic phenomenon (it usually takes years in
173 nature), a continuous constant seepage flow sustaining for a relatively long time is
174 necessary. Another drawback with this setup is that back pressure could not be applied,
175 which may result in a low saturation degree in tested specimens and consequently, a not
176 well performed undrained compression test. The triaxial apparatus in this paper adopts
177 the constant-flow-rate control mode, which would ensure continuous water supply for a
178 relatively long time. Meanwhile, the back pressure is maintained on tested specimens
179 during the erosion test through a specially designed buffer. Inside of the buffer, a

180 consecutive monitoring system is installed which permits continuous recording of the
181 eroded soil mass.

182

183 **3 Triaxial Internal Erosion Apparatus**

184

185 The newly developed triaxial internal erosion apparatus could directly investigate not
186 only the hydraulic characteristics of soils at the onset and the progress of internal
187 erosion but also the change of soil mechanical behaviors induced by internal erosion. It
188 is applicable for testing non-cohesive soils. The design is improved after preliminary
189 one-dimensional seepage tests in a fixed-wall permeameter (Ke and Takahashi, 2012). It
190 mainly consists of a constant-flow-rate control unit, an automated triaxial system and
191 eroded soil collection unit. The recorded variables include the pressure differences
192 generated by the seepage flow, soil axial & radial strain, cumulative eroded soil mass
193 and pore pressures. The whole system allows independently synchronous control of the
194 hydraulic condition and the stress state of tested specimens. Photograph of the triaxial
195 permeameter is shown in Fig. 1 and the schematic illustration of the overall system is
196 shown in Fig. 2.

197

198 3.1 Constant-flow-rate control unit

199 Hydraulic gradient and Darcy velocity are the vital parameters for hydraulics. For those
200 sands with large hydraulic conductivity ($>0.001\text{m/s}$), seepage test by the
201 hydraulic-gradient-control manner may not be appropriate because of the comparatively
202 small hydraulic gradient to intrigue and maintain the internal erosion. An accurate
203 control of the hydraulic pressure and estimation of the head loss in tubes, valves and
204 fittings is necessary, which however is difficult in practice. The flow-rate-control mode,
205 on the other hand, could avoid the above-mentioned difficulties. [Richard and Reddy](#)
206 [\(2010\)](#) concluded that flow velocity might be the fundamental characteristic responsible
207 for erosion in non-cohesive materials, which could yield more consistent results. In this
208 apparatus, the seepage test is performed by the constant-flow-rate manner. The control
209 unit is composed of a rotary pump with the maximum flow rate of 1360mL/min for
210 pumping water flow through the specimen and a Low Capacity Differential Pressure
211 Transducer (LCDPT) for measuring the pressure drop from the top to the bottom of
212 tested specimens. The output of LCDPT is highly linear within the range of $0\sim 20\text{kPa}$. In
213 order to maintain the flow rate constant, all the flow channels are designed as the same
214 size: 7.5mm -in-diameter plastic tubes with relatively large stiffness are used. To
215 minimize the effect of tube stiffness on the measurement of deviator stress, the tube is
216 arranged in spiral ([Fig. 3](#)). For common triaxial equipment, an annular porous stone is
217 typically used at the interface between soil and water in the top cap. However, in this

218 apparatus, instead of porous stone, a perforated plate is mounted in top cap, which
219 directly attaches specimen, to minimize the possible water head loss. The same as is at
220 the pedestal, the details of which will be given later. The seepage water is pumped from
221 a water tank, which is filled with water and kept at room temperature, at least 24 hours
222 before use. Since the back pressure is maintained during seepage tests, the volume of
223 the indissolved air bubbles in seepage flow may be shrunk and their influence on the
224 soil saturation degree may be minimized. During the experiment, the range of the
225 assigned inflow rate must ensure the resulting pressure drop is well below the confining
226 pressure to prevent the separation of membrane from soil specimen.

227

228 3.2 Automated triaxial system

229 The automated triaxial system used, capable of investigating either the static or cyclic
230 soil behavior, could conduct measurements and controls by PC through 16-bit A/D and
231 D/A converters. The vertical load could be automatically applied by a motor-gear
232 system at any rate. The maximum load is 50kN. The system has zero backlash on
233 reversal of the load, which would realize the continuous cyclic loading without any
234 stress relaxation. The cell pressure is applied by the air pressure which is maintained
235 constantly at 700kPa through an automatic air compressor. All the pressure lines are
236 connected to a drying system to remove any condensed water. The control of the cell

237 pressure is by E/P (Electronic to Pneumatic) transducers, which is linked to PC through
238 a 16-bit D/A board. The axial load is measured by the load cell internally mounted
239 above the top cap, which eliminates the effects of any friction on the loading shaft. The
240 soil effective pressure is known from another Difference Pressure Transducer, which
241 joins the specimen base and cell. Pore pressure is obtained at the base of a specimen by
242 a pressure transducer mounted at the pedestal. Three pairs of clip gauges with the
243 capacity of ± 2 mm are employed to measure the radial deformation. All the measuring
244 devices are connected to amplifiers and then to a PC through a 16-bit A/D converter. All
245 the controls of the triaxial testing and data recording are through a program with the
246 interactive visual interface, written by Visual C++.

247

248 The base pedestal is specially designed to accommodate the internal erosion test (Fig. 4).
249 The main component is the drainage system to prevent the possible accumulation of
250 eroded soil at the bottom, which would cause clogging. It includes a conical trough and
251 a plastic tube fitted at the outlet of the trough, directly connected to the soil collection
252 system. This space gives freedom in determining the filter, either the granular type or
253 the wire mesh with openings. A paradox comes up in the filter determination. For soil
254 element test, it is significant to ease the influence of boundary frictions on the measured
255 material properties. In practice, to minimize the non-uniformity in stresses and strains

256 induced by end restraint, a lubrication layer, such as a silicone grease layer or latex
257 rubber is utilized (Kuwano *et al.*, 2000). However, that layer would cause great water
258 head loss and serious clogging during erosion test due to the high viscosity. A
259 compromise in free ends may be necessary. In this apparatus, the filter is the 5mm-thick
260 steel mesh with smooth surface (Fig. 5). The opening size of the mesh follows the
261 recommendation of Japan Dam Conference which specified that the mesh should fully
262 hold the coarse grains and permit the erosion of fines (Uno, 2009). The adopted opening
263 size is 1mm in this apparatus.

264

265 3.3 Eroded soil collection unit

266 The main component of the eroded soil collection unit is the pressurized sedimentation
267 tank (Fig. 6). The acrylic tube is mounted between a steel top and base plate, and is
268 sealed by means of O-rings and five external tie rods. Inside of the tank, a
269 160mm-in-diameter acrylic cylinder with full of water is built in. During the seepage
270 tests, the discharge effluent with dislodged fines directly flows into the cylinder through
271 a pipe that connects the inlet valve and the cylinder. The end of the pipe is fully
272 submerged in the cylinder to prevent the admission of air bubbles into the tested soil
273 specimen. The cumulative eroded soil mass is gained by continuously weighing the
274 light tray which is fully submerged in the cylinder to collect the eroded soil grains.

275 The waterproofed load cell that has high sensitivity could record the cumulative eroded
276 soil weight within a continuous period. The theoretical resolution of the load cell is
277 0.00015N (approximately 0.015g). Due to the magnitude of noise and zero shift induced
278 by the data collection system, some deviations may exist. To drain off the seepage water,
279 a solenoid valve with timer is fixed at the outlet drainage line. The valve is capable of
280 opening and closing at a determined interval of time. During erosion tests, the back
281 pressure in the tested soil specimen is maintained through the sedimentation tank.

282

283 **4 Main Testing Procedures**

284

285 The purpose of the study is to investigate the erosion characteristics of the cohesionless
286 soil and its mechanical consequences. Therefore, the main testing procedures include
287 erosion tests on the reconstituted soil specimens, monotonic compression or cyclic
288 shearing tests on the eroded specimens and post-erosion grain size distribution analysis.

289 A detailed description of each procedure is presented as following:

290

291 4.1 Saturation and consolidation

292 The vacuum saturation procedure ([ASTM D4767-11](#); [JGS 0525-2000](#)), including two
293 stages, is adopted in this study. The top and bottom of the tested specimen is connected

294 to two separate reservoirs. After specimen preparation, vacuum is supplied to the
295 specimen through both water reservoirs gradually until -80kPa. The pressure difference
296 between the specimen pressure and the cell pressure is kept constant as 20kPa during
297 the increment of vacuum. Allow deaerated water slowly inject into the specimen
298 upwardly. The inflow rate should be sufficiently slow to avoid the filtration of soil
299 grains in the specimen. After three-quarters of the deaerated water has flowed through
300 the specimen, slowly return the specimen pressure to 0kPa and increase the cell pressure
301 to 20kPa, keeping the pressure increment constantly as 20kPa all the way. Then let the
302 remaining deaerated water of the upper reservoir inject into the specimen again. A total
303 water volume of 10.4 (normalized value in terms of pore volume) has been flowed
304 through the soil specimen. The inlet valve of sedimentation tank should be closed all the
305 way to avoid any possible soil grain loss.

306

307 The application of back pressure begins after the completion of the vacuum saturation
308 procedure. In this apparatus, back pressure could be applied from either the double
309 burette or the sedimentation tank (Fig. 2). Both of them are pressurized simultaneously
310 and connected to the tested specimen. Initially the valve connected to the sedimentation
311 tank is closed. The cell pressure and back pressure are increased incrementally with the
312 drainage valves to the double burette, which is connected to the top and bottom of the

313 specimen, opened. The size of each increment is 50kPa. For the majority of tests, a
314 B-value of higher than 0.95 could be achieved after applying a back pressure of 100kPa.
315 At this circumstance, the pressure inside the sedimentation tank reaches 100kPa as well.
316 Then close the double burette valve and slowly open the sedimentation tank valve.
317 Minor adjustments might be necessary to ensure the back pressure reaches 100kPa and
318 then wait until the readings from pressure gauges become stable. The recordings of the
319 load cell inside the sedimentation tank indicate that there is hardly fines loss due to the
320 application of back pressure.

321

322 The consolidation is performed by an automatic control system. Cell pressure gradually
323 increases up to the target value at a fairly low increment (i.e., 1kPa/min) to avoid soil
324 grains migration. Axial stress, controlled by a motor, increases correspondingly to keep
325 the determined effective stress ratio (effective axial stress/effective radial stress)
326 constant. In this study, soil specimens are isotropically consolidated until the preferred
327 stress state. After consolidation, the specimens are ready for erosion tests.

328

329 4.2 Erosion test

330 From the erosion test, it is expected to detect the critical Darcy velocity, at which
331 internal erosion initiates. To well demonstrate the mechanical effects of internal erosion

332 on soils, the imposed inflow rate for each specimen should be held constant as a
333 reference. After several trial tests, an inflow rate of 310mL/min for the tested soil is
334 selected because the loss of fines at this rate is significantly large, which would
335 highlight the differences between the eroded specimen (ES) and the non-eroded
336 specimen (NS) in terms of stress-strain relationship. The procedure for the inflow rate
337 increments in this study is shown in [Fig. 7](#). Based on the authors' previous experience of
338 conducting upward seepage tests in a fixed-wall permeameter on the similar sandy soils
339 ([Ke and Takahashi, 2012](#)), the initiation of internal erosion would occur at a fairly low
340 Darcy velocity, which is approximately 0.02~0.12cm/s (i.e., equivalent to the inflow
341 rate of 48mL/min~277mL/min through a 70mm-in-diameter circular section) depending
342 on the density and fines content of the tested specimen. Therefore, the initial increment
343 of inflow rate is set approximately at 10(mL/min)/min: increase the inflow rate to
344 10mL/min in 1min and allow the seepage flow to become steady for the next 1min. The
345 trial tests indicate that a short duration (e.g. 1min) is sufficient to stabilize the seepage
346 flow. As long as erosion initiates, the amounts of eroded fines would increase with the
347 increasing of inflow rate. The increments of inflow rate at this stage could be relatively
348 larger to shorten the test. Then in this study, the inflow rate is increased to the target
349 value of 310mL/min at the increments of 50(mL/min)/min once the it reaches
350 100mL/min. This inflow rate of 310mL/min will be maintained constant until (1) the

351 recorded hydraulic gradient is steady; (2) the effluent become clear and clean by visual
352 observation; (3) no further eroded fines loss (i.e., <0.2g per 10min); (4) no further
353 increases in the axial and radial strain of the tested specimen. Commonly, the erosion
354 test would be terminated after 3 hours. The inflow rate is decreased gradually till there
355 is no pressure difference between the top and bottom of the specimen. Then close the
356 inflow valve and let the specimen stay still until the readings of the pressure gauges
357 become stable. B-value is checked again.

358

359 The stress state of the specimen during the erosion test is maintained the same as that
360 after isotropic consolidation. The cumulative eroded fines mass is recorded
361 automatically by the load cell inside of the sedimentation tank. The balance of the light
362 tray is realized by the following procedure: before the erosion test, the cylinder is filled
363 with deaerated water so that the light tray is fully submerged. After applying the target
364 pressure of 100kPa to the sedimentation tank, the tray would reach equilibrium within
365 10min. Then set the readings of “eroded soil mass” as zero and start recording. During
366 the erosion tests, authors found that the readings of the cumulative eroded soil mass
367 were influenced by the impact force, generated from the flow jet. It became obvious if
368 larger inflow rate was assigned. To minimize the effect of the impact force on the light
369 tray, a funnel with a 15mm-in-diameter opening at the end has been fastened on the steel

370 frame to surround the inlet pipe. Position of the funnel outlet is aligned with the tray
371 center. The details are shown in [Fig. 8](#). It works as a buffer that could decrease the
372 velocity of flow jet as well as a drainage that could facilitate the eroded fines uniformly
373 settled down onto the light tray. The axial displacement, radial deformation and the pore
374 water pressure difference generated by the seepage flow is recorded at every 1s
375 automatically.

376

377 4.3 Undrained and drained compression test

378 Undrained and drained compression test is performed at the same stress state as that of
379 erosion test to investigate the mechanical consequences of internal erosion. The
380 compression test is displacement controlled with the axial strain rate of 0.1%/min,
381 following the standard criteria ([ASTM D4767-11](#); [ASTM D7181-11](#); [JGS 0524-2000](#);
382 [JGS 0525-2000](#)), to allow the pore pressure to reach equilibrium. The confining
383 pressure is maintained constant while axial displacement increases at the designated
384 strain rate. Axial stress could be obtained from the load cell amounted to the piston. The
385 recorded data from the eroded soil collection unit indicate that there is hardly fines loss
386 due to compression.

387

388 4.4 Undrained cyclic test

389 To quantify the effect of internal erosion on the cyclic resistance, undrained cyclic tests
390 are performed on the eroded specimens (ES). After erosion test, the soil specimens are
391 subjected to a cyclic shear stress in axial direction under the same effective confining
392 pressure as that of erosion test with a cyclic stress ratio (CSR) of 0.12. The axial strain
393 rate is 0.5%/min, which is sufficiently slow to allow the equilibrium of pore pressure in
394 the tested specimens.

395

396 **5 Test Specimens**

397

398 5.1 Test materials

399 The grain size distribution of a soil could be split into coarse components and fine
400 components. In this study, the tested specimens are the binary mixtures of two types of
401 silica sands (silica No.3 and No.8) with different dominant grain sizes. The siliceous
402 sand is mainly composed by quartz, categorized as sub-rounded to sub-angular material.
403 According to the Unified Soil Classification System ([ASTM D2487](#)), they correspond
404 to SP. The grain size distributions are shown in [Fig. 9](#).

405

406 With larger grain size, the silica No.3 sand works as the soil skeleton in the mixtures
407 while the finer silica No.8 sand is the erodible fines. Hereafter, the silica No. 8 is

408 referred to fines for simplicity even though the silica No. 8 is not strictly classified as
409 fines. The mass fraction of silica No.3 and No.8 in the mixture is determined
410 considering the geometrical restriction: the volume of fines should be less than that of
411 the voids among coarse grains. The estimated maximum mass of the fines fraction in the
412 mixture is approximately 37% (Ke and Takahashi, 2012). In this study, a fines content
413 of 35% is adopted. The grain size distribution and the physical properties of the mixture
414 are shown in Fig. 10 and Table 1.

415

416 To ensure the internal erosion would occur during the erosion test, the vulnerability of
417 the mixture to internal erosion is assessed by six currently available methods proposed
418 by U.S. Army Corps of Engineers (1953); Istomina (1957); Kezdi (1979); Kenney and
419 Lau (1985, 1986); Burenkova (1993) and Mao (2005). The evaluation results are shown
420 in Table 2. The results indicate that the mixture is potentially unstable and vulnerable to
421 internal erosion if seepage takes place.

422

423 5.2 Specimen preparation

424 The tested specimen is 70mm in diameter and 150mm in height. The technics of moist
425 tamping (Ladd, 1978) is employed to prevent the segregation of the two different sized
426 grains. The method is developed based on the fact that when typical sand is compacted

427 in layers, the compaction of each succeeding layer may further densify the layers below.
428 The concept of “undercompaction, U_n ” is recommended to assess the effects of
429 densification. It indicates how much percent a layer should be less densified than the
430 target value. In this study, a non-linear average undercompaction criterion, which is
431 proved to be reliable in generating uniform soil conditions (Jiang *et al.*, 2003), is
432 adopted. The average undercompaction of each layer in a moist tamped specimen is
433 shown in Fig. 11.

434

435 The specimen preparation procedures are as follows: determine the oven-dried weights
436 of clean silica No.3 and No.8 for a test according to the fines content and relative
437 density. The initial water content is determined as 10% from the previous trials and
438 errors, at which a uniform specimen would be achieved. Thoroughly mix the soils with
439 deaerated water to make sure the distribution of fines in a specimen is uniform. Equally
440 separate the wet mixture into 10 pieces and keep them in a zipped bag to equalize
441 moisture at least 16 hours before use. The specimen is prepared layer by layer. Weigh
442 the amount of material required for each layer, and place it into the mold by scoop. Each
443 layer is compacted to the required height determined by “undercompaction”. The initial
444 soil weight could not be directly checked after preparation. Therefore, the after-test
445 oven-dry weight of the soil specimen together with the eroded soil weight should be

446 checked.

447

448 **6 Test Results and Discussions**

449

450 To understand the mechanical effects of internal erosion, several soil specimens are
451 tested. A summary of the test cases is shown in [Table 3](#). The effective confining pressure
452 is 50kPa, which is approximately equal to the earth pressure of 5m in depth. Three
453 different types of triaxial tests, including undrained compression, drained compression
454 and undrained cyclic tests, are conducted on the internally eroded specimens (50EU,
455 50ED and 50EC). To specify the mechanical consequences of internal erosion, the same
456 triaxial tests are performed on the un-eroded soil specimens (50NU, 50ND and 50NC)
457 at the same effective confining pressure of 50kPa for the comparison purpose.

458

459 **6.1 Internal erosion characteristics**

460 In this study, hydraulic gradient is defined as the ratio of the recorded pressure drop
461 induced by seepage flow to the specimen length corrected by the vertical deformation.
462 The variation of hydraulic gradient at the initial 900s, 900s~2000s and 0s~11000s
463 during the seepage test is plotted in [Figs.12a, 12b and 13a](#), respectively. Generally, it is
464 indicated that the hydraulic gradient varies with the progress of erosion. For the initial

465 900s (Fig. 12a), a moderate drop of hydraulic gradient is discovered at 480s
466 ($Q=50\text{mL/min}$, $v=0.021\text{cm/s}$), which is considered as the onset of internal erosion. The
467 effluent becomes slightly turbid with small amounts of fines suspending. However, the
468 eroded soil mass at this stage could not be obtained because the load cell is not able to
469 catch the weight of suspended grains. By visual observation, the suspending fines are
470 very little and therefore, the cumulative eroded soil mass at this stage is considered as
471 zero. A sharp increase of the hydraulic gradient is detected at approximate 880s
472 ($Q=100\text{mL/min}$, $v=0.042\text{cm/s}$) at which the increment of the flow rate begins increasing
473 from $10(\text{mL/min})/\text{min}$ to $50(\text{mL/min})/\text{min}$ (Fig. 12b). The sharp increase may be
474 attributed to the clogging of fines among the constrictions of coarse grains when large
475 amounts of fines begin eroding off. Another possibility is related with the influence of
476 “hammer effects” which refers to the phenomenon that a sudden increase or decrease in
477 flow rate would affect the hydraulic properties of soil specimens (Tomlinson and Vaid,
478 2000). This effect is obvious when opening the inlet valve at the starting of the tests and
479 closing the valve at the end. It may induce the unexpected movement of soil grains
480 which would affect the detection of critical Darcy velocity. The characteristics of
481 internal erosion are fully exhibited at this stage. The hydraulic gradient dramatically
482 drops while a large amount of fines is eroded off (Fig. 13b), which supposedly results in
483 the increase of effective porosity. If the seepage flow is assumed to follow Darcy’s law

484 ($v=ki$), the hydraulic conductivity could be estimated on condition that Darcy velocity
485 and hydraulic gradient is known. It is found that the hydraulic conductivity increases
486 with the decreasing of hydraulic gradient. This trend will continue until a new
487 equilibrium among the soil grains is reached when the hydraulic gradient and the
488 cumulative eroded soil mass become constant. The ultimate hydraulic conductivity is
489 about 150 times larger than the initial value together with the loss of approximately 70%
490 fines (mass ratio of eroded fines to initial fines). No critical clogging is detected at the
491 end of the erosion test probably because the size of voids among coarse grains is
492 sufficiently large for the fines passing through.

493

494 The incessant erosion of fines from the tested specimen would lead to a change in the
495 soil fabric, which is represented by the increase of volumetric strain, and void ratio.
496 **Figures 13c and d** displays the development of the axial and radial strain of the soil
497 specimen during erosion test. In general, the soil specimen is prone to be contractive
498 with the progress of erosion. The soil deformation is found be sudden and rapid. Two
499 obvious jumps in deformation are detected around 2400s and 5600s. It is inferred that
500 along with the dislodgement of the fines, the coarse grains would correspondingly
501 rearrange their relative positions and finally reach a new equilibrium in a short period.
502 This phenomenon is in accordance with the practice. The dam failure induced by

503 internal erosion is usually sudden without any pre-warning, such as a large deformation.

504

505 The back pressure in the soil specimen during erosion test is plotted in [Fig. 13e](#).

506 Although the pressure slightly deviates from the target value due to the regular

507 opening/closing of the drainage valve of the sedimentation tank, basically the back

508 pressure is maintained constant in the tested soil specimen. The B-value, checked after

509 erosion test, is usually higher than 0.93, which may indicate a relatively high saturation

510 degree.

511

512 6.2 Post-erosion grain size grading

513 Grain size distribution could characterize the geometrical variation of soil specimens

514 due to internal erosion. [Kenney and Lau \(1985\)](#) concluded that fines loss due to erosion

515 could cause the post-erosion distribution curve shift downward from the original curve.

516 The extent of the movement proportionally increases with the amount of fines loss. In

517 this laboratory test, the post-erosion specimen is equally divided into two layers: top

518 layer and bottom layer. The grain size distribution curve of each layer is determined by

519 performing sieving test ([ASTM D6913-04](#); [JIS A1204](#)). The soil of each layer has been

520 oven-dried at 110°C for 24h before sieving. [Figure14](#) shows the typical grain size

521 distribution curves of a post-erosion soil specimen. Both of the post-erosion curves for

522 the upper layer and the bottom layer move downward from the original curve, the extent
523 of which is corresponding to the fines loss. It is noted that there is more fines loss in the
524 upper layer.

525

526 6.3 Drained test results and discussions

527 **Figure 15** plots the stress ~ strain curves together with the corresponding volumetric
528 strain curves for the drained monotonic compression on the ES and NS specimens. It is
529 noted that the deviator stress of the ES specimen is larger at the same small strain level
530 (within 1%) comparing to that of the NS specimen while that value becomes smaller at
531 the same medium level (approximately 1% ~ 16%). Both of the volumetric strain curves
532 are contractive and the ES specimen has slightly less volumetric deformation. It is
533 inferred that the larger initial stiffness of the ES specimen is caused by the accumulation
534 of fines at the contact points among coarse grains where local reinforcement may be
535 formed in the seepage test. However, this reinforcement may be deteriorated for the
536 subsequent compression, which is corresponding to the medium strain level. With larger
537 void ratio, the ES specimen at the subsequent compression may show smaller deviator
538 stress at the same axial strain. To validate this assumption, microscopic observations of
539 the eroded soil fabric might be necessary. Overall, the drained strength of the ES
540 specimen is basically lower than that of the NS specimen as expected. It is in

541 accordance with findings by [Muir Wood *et al.* \(2010\)](#) who concluded that internal
542 erosion would cause lower soil strength and [Chang *et al.* \(2011\)](#) who experimentally
543 proved that the drained compressive strength would drop after internal erosion.

544

545 6.4 Undrained test results

546 Undrained tests are conducted at an axial strain rate of 0.1%/min under the initial
547 effective confining pressure of 50kPa. Each test lasts for at least 180min, which may be
548 slow enough to guarantee the full equilibrium of pore pressure with a minimum B value
549 of 0.93. The undrained responses of the tested specimens in terms of stress ~ strain
550 curves are presented in [Fig. 16](#). For the undrained compression, the deviator stress of
551 both the ES specimen and NS specimen reach a marked peak at low axial strain,
552 approximately 1%, followed by the strain softening. When the specimens arrive the
553 phase transformation point the soil behavior becomes dilative. This phenomenon is
554 more obvious in the ES specimen. The peak deviator stress of the ES specimen is fairly
555 larger than that of the NS specimen. However, the after-peak undrained deviator stress
556 of the ES specimen becomes smaller at the medium strain level. [Xiao and Shwiyhat](#)
557 [\(2012\)](#) speculatively attributed this higher undrained compressive strength of the ES
558 specimen to the loss of saturation degree during erosion test. From authors' point of
559 view, it might be related with the soil fabric change as well. It is universally accepted

560 that the mechanical behavior of granular soils is highly influenced by the orientation
561 and arrangement of soil grain, and the contact between the grains. The fabric of a soil
562 specimen would be greatly changed by erosion progress and local reinforcement might
563 be formed as is discussed in 6.3. Consequently, the undrained peak deviator stress of the
564 ES specimen may become larger in the small axial strain level. An investigation of the
565 new arrangement of soil grains might be necessary for the further study. To this end, a
566 microscopic observation of the eroded soil fabric should be involved.

567

568 6.5 Undrained cyclic test results

569 **Figures 17 and 18** show the cyclic behavior of the NS and ES specimens, respectively,
570 under the cyclic stress ratio of 0.12 with the monotonic compression data superimposed.
571 Both of the specimens show non-reversal loading condition: the plastic axial strain
572 develops with cyclic loops. The NS specimen shows flow deformation, which is
573 common in loose sand. The strain would continue developing with the decreasing of
574 mean effective stress. For the ES specimen, initially, its behavior follows the “flow
575 deformation” pattern. However, this trend is inhibited as soon as the specimen loaded
576 sufficiently to initiate dilation with further straining. [Vaid and Chern \(1985\)](#) termed this
577 phenomenon as “limited flow deformation”. Comparing to the NS specimen, the ES
578 specimen would fail after more cyclic loops. Here the cyclic test data are presented to

579 demonstrate that the apparatus is capable of conducting the undrained cyclic tests on the
580 internally eroded specimens. For further detailed explanations of the cyclic behavior of
581 the internally eroded soil, more tests at different cyclic stress ratios might be necessary.

582

583 6.6 Discussions on undrained test results

584 Commonly, soil becomes loose after erosion due to the large amounts of fines loss
585 (Table 3) and therefore, the eroded soil is expected to show contractive tendency at
586 shearing. However, the undrained monotonic and cyclic tests on the eroded specimens
587 in this study indicate a much dilative behavior after erosion, which may be attributed to
588 the mechanical influence of (1) fines content (*FC*) and (2) geometrical properties of
589 coarse grains. Hitherto, the mechanical influence of non-plastic fines on the soil
590 behavior is somewhat contradictory in literature. Some laboratory investigations
591 indicate the presence of non-plastic fines would result in the increasing of sand
592 dilatancy (Pitman *et al.*, 1994; Salgado, *et al.*, 2000; Ni *et al.*, 2004; among others)
593 while some other studies show a contrary tendency (Zlatovic and Ishihara, 1995; Lade
594 and Yamamuro, 1997; Carraro *et al.*, 2009; among others). The influence of the
595 non-plastic fines content, which is the content of silica No.8 in this study, on the soil
596 undrained strength is experimentally investigated by performing undrained monotonic
597 compression tests on the reconstituted soil specimen with three different fines contents

598 (0%, 15% and 35%). The soil specimens are prepared by the moist tamping method.

599 Since the void ratio of the eroded specimens is much larger than that can be achieved by

600 the moist tamping method, the initial void ratios are set as large as practical, but are

601 smaller than that of the eroded specimens. **Figure 19** plots the stress ~ strain curves

602 together with the corresponding stress paths in stress space for the soil specimens at an

603 effective confining pressure of 50kPa. The initial void ratio and fines content before

604 compression are denoted in the figures. It is noted that the soil specimen with 35% fines

605 content shows partial collapsive behavior after reaching the peak deviator stress: with

606 the subsequent compression, the soil continues deforming and reaching a residual

607 strength. In contrast, the specimen with 15% fines content implies a temporary loss of

608 shear strength after initial peak, which is called “quasi-steady state” in literature. With

609 further compression, the soil becomes dilative and gradually gains strength. In terms of

610 the loose soil specimen without any fines content, the soil response is completely

611 dilative. Therefore, for the tested soil in this study, the presence of the fine silica No.8

612 sand would decrease the soil strength and restrain the soil dilatancy. One of the

613 consequences of internal erosion is the great amounts of fines loss. The eroded soil

614 specimen with less fines content may show dilative response and consequently, gain

615 higher strength comparing to the un-eroded specimen with higher fines content.

616 Furthermore, the coarse soil used in this study, the artificial silica No.3 sand, shows full

617 hardening behavior without any sign of strength reduction after the yield point even at
618 loose condition (i.e., the initial void ratio is 0.84 in Fig. 19). Dilative soil response
619 caused by the mechanical effect of fines content and geometric properties of coarse
620 grains may have surpassed the contractive tendency induced by the increase in the void
621 ratio. Thus, the eroded soil presents dilative tendency.

622

623 6.7 Test repeatability

624 The repeatability of the seepage test is validated by comparing the primary parameters
625 noted in Table 4. The internal erosion generally occurs at the similar Darcy velocity.
626 However, irregular deviation exists in the hydraulic gradient and hydraulic conductivity,
627 which may be attributed to the difference in homogeneity among the reconstituted soil
628 specimens. The volumetric strain and the cumulative fines loss are basically close,
629 which might imply the good repeatability of the seepage test. In terms of the triaxial
630 tests, the undrained responses of specimen 50EU and 50EU-R are plotted in Fig. 20 to
631 show the consistency of the test data. There are somewhat variations in the undrained
632 response, especially for the post-peak stage. The peak and post-peak deviator stress of
633 the specimen 50EU-R is higher than that of 50EU, which might be due to the difference
634 in the initial void ratio and fines content before the compression test. In contrast, at the
635 initial stage of the compression, both specimens show similar behavior.

636

637 **7 Summary and Conclusions**

638

639 A newly developed triaxial internal erosion apparatus, capable of directly investigating
640 not only the hydraulic characteristics of soils at the onset and the progress of internal
641 erosion under preferred stress state but also the mechanical behaviors of those internally
642 eroded soils, is presented. By introducing a sedimentation tank, back pressure could be
643 maintained in the tested specimens during erosion test to ensure a relatively high
644 saturation degree. A measurement system of the cumulative eroded soil mass is installed
645 in the tank to continuously record the eroded soil mass. Erosion tests are performed by
646 constant-flow-rate control manner with the measurement of the induced pressure
647 difference between the top and bottom of the tested specimens. Volumetric strain of the
648 soil specimen could be assessed by measuring the axial and radial deformation. The
649 mechanical consequences of internal erosion could be evaluated by directly performing
650 undrained and drained compression tests or undrained cyclic tests on the eroded soil.

651

652 In this study, the binary mixtures of two types of silica sands (silica No.3 and No.8)
653 with different dominant grain sizes are tested. With larger grain size, the silica No.3
654 works as the soil skeleton in the mixture while the finer silica No.8 is the erodible fines.

655

656 For the erosion test, the hydraulic gradient dramatically drops with the erosion of a large
657 amount of fines. The soil grains correspondingly rearrange their relative positions until
658 a new equilibrium is reached. At the end of erosion, the hydraulic gradient and the
659 cumulative eroded soil mass become constant. The ultimate hydraulic conductivity is
660 about 150 times larger than the initial value together with the approximate 70% fines
661 loss (mass ratio of eroded fines to initial fines). The erosion of fines would lead to an
662 increase of the volumetric strain of the tested specimen. The soil deforms in a
663 contractive way. The post-erosion grain size distribution analysis indicates that there is
664 more fines loss in the upper layer.

665

666 The drained compressive strength of the ES specimen is lower than that of the NS
667 specimen. For the undrained test, the peak deviator stress of the ES specimen is fairly
668 higher than that of the NS specimen. However, the after-peak undrained deviator stress
669 of the ES specimen becomes smaller at the medium strain level. In terms of the
670 undrained cyclic test, the NS specimen follows the “flow deformation” pattern while the
671 ES specimen shows “limited flow deformation”. The ES specimen would fail after more
672 cyclic loops. Microscopic observations of the eroded soil fabric (i.e., the accumulation
673 spots of fines) might be necessary for explaining the mechanical behavior of the eroded

674 soil.

675

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680

681 **NOTATION**

682 e : Void ratio

683 FC : Fines content

684 i : Hydraulic gradient

685 k : Hydraulic conductivity (cm/s)

686 p' : Mean effective stress (kPa)

687 q : Deviatoric stress (kPa)

688 Q : Inflow rate (mL/min)

689 v : Darcy velocity (cm/s)

690

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837

Table 1 Physical properties of tested soil

| Physical Property | Value |
|--|---------------------|
| Specific Gravity, G_s | 2.645 |
| Maximum Void Ratio, e_{\max} | 0.74 |
| Minimum Void Ratio, e_{\min} | 0.36 |
| Initial Relative Density, D_r (%) | 30 |
| Median particle size D_{50} (mm) ⁽¹⁾ | 1.54 |
| Effective particle size D_{10} (mm) | 0.038 |
| Uniformity Coefficient C_u | 45.9 |
| Curvature Coefficient C_c | 0.59 |
| $(H/F)_{\min}$ ⁽²⁾ | 0.050 |
| $(D_{15c}/d_{85f})_{\text{gap}}$ ⁽³⁾ | 7.9 |
| Conditional factor of uniformity, h' ⁽⁴⁾ | 1.3 |
| Conditional factor of uniformity, h'' ⁽⁵⁾ | 8.5 |
| Grain Description | Subround-Subangular |

839 Note:

840 (1) D_x denotes the grain size finer than which the soil weight by percentage is $X\%$.

841 (2) F is the weight fraction of the soil finer than size d ; H is the weight fraction of the soil in the
842 size ranging from d to $4d$.

843 (3) A soil could be split into a coarse fraction (c) and a fines fraction (f). D_{15c} is the grain size
844 finer than which the soil weight by percentage is 15% for the coarse fraction; d_{85f} is the
845 grain size finer than which the soil weight by percentage is 85% for the fines fraction.

846 (4) $h' = D_{90}/D_{60}$

847 (5) $h'' = D_{90}/D_{15}$

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Table 2 Assessment of the mixture's vulnerability to internal erosion

| The method used to assess internal erosion potential | | Stability |
|--|--|------------------|
| Criteria | The mixture is internally stable if | |
| U.S. Army (1953) | $C_u < 20$ | U ⁽¹⁾ |
| Istomina (1957) [Ref. Kovacs (1981)] | $C_u \leq 20$ | U |
| Kezdi (1979) | $(D_{15c}/d_{85f})_{\max} \leq 4$ | U |
| Kenney and Lau (1985, 1986) | $(H/F)_{\min} \geq 1$ ($0 < F < 0.2$) | U |
| Burenkova (1993) | $0.76 \log(h'') + 1 < h' < 1.86 \log(h'') + 1$ | U |
| Mao (2005) | $4P_f(1-n) \geq I^{(2)}$ | U |

850 Note:

851 (1) "U" means Unstable;

852 (2) P_f is the fines content by weight in soil; n is the porosity.

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Table 3 Summary of test conditions

| Specimen | Initial void ratio | Void ratio after consolidation | Void ratio after erosion | p' (kPa) | Erosion | Test type | CSR ⁽⁶⁾ |
|----------|--------------------|--------------------------------|--------------------------|------------|------------------|-------------------|--------------------|
| 50NU | 0.60 | 0.56 | --- | 50 | N ⁽¹⁾ | CU ⁽³⁾ | --- |
| 50ND | 0.59 | 0.55 | --- | 50 | N | CD ⁽⁴⁾ | --- |
| 50EU | 0.60 | 0.55 | 0.96 | 50 | Y ⁽²⁾ | CU | --- |
| 50EU-R | 0.60 | 0.56 | 1.00 | 50 | Y | CU | --- |
| 50ED | 0.59 | 0.55 | 0.94 | 50 | Y | CD | --- |
| 50NC | 0.60 | 0.56 | --- | 50 | N | CC ⁽⁵⁾ | 0.12 |
| 50EC | 0.60 | 0.57 | 1.01 | 50 | Y | CC | 0.12 |

855 Note:

856 (1) "N" means no erosion;

857 (2) "Y" means erosion at the assigned inflow rate of 310mL/min;

858 (3) "CU" means Consolidated-Undrained test;

859 (4) "CD" means Consolidated-Drained test;

860 (5) "CC" means Consolidated-Cyclic test;

861 (6) "CSR" means Cyclic Stress Ratio.

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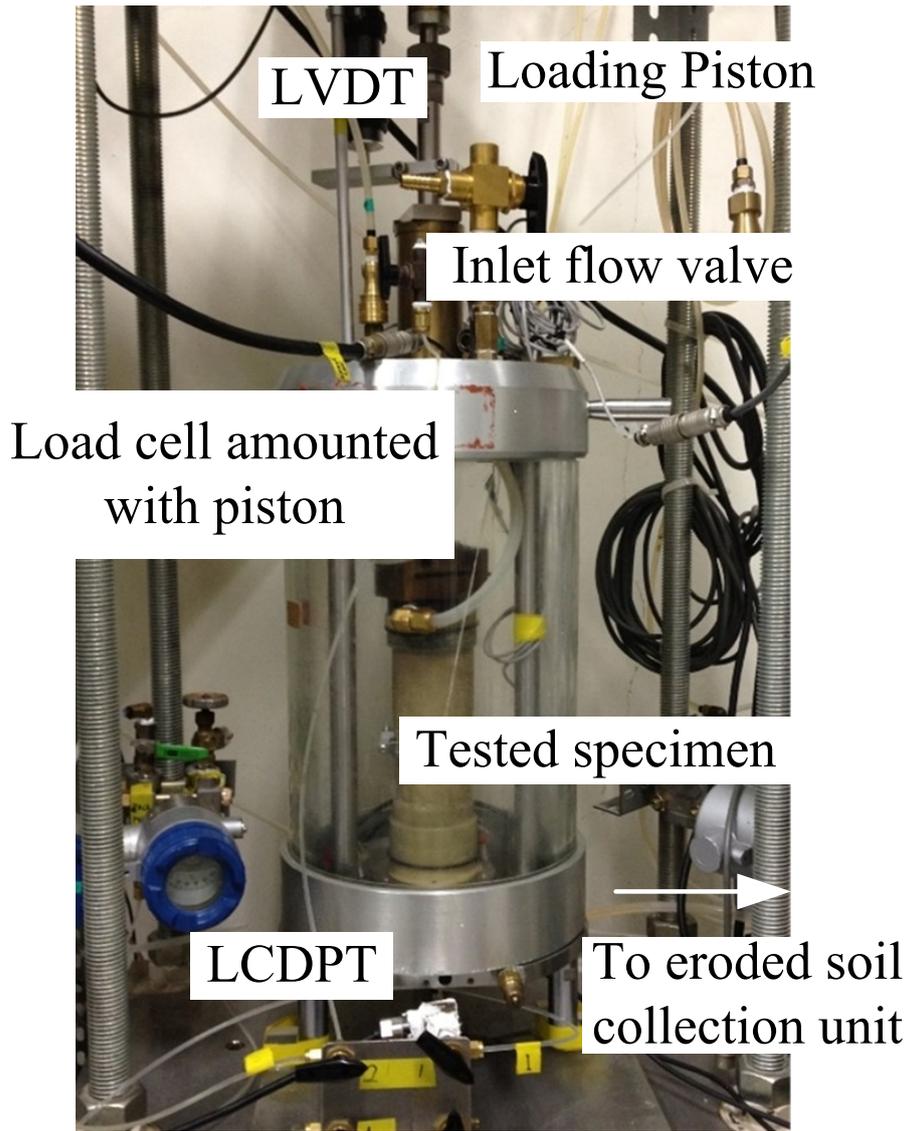
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Table 4 Repeatability of seepage tests

| Specimen | Critical Darcy velocity (cm/s) | Maximum Hydraulic gradient | Ultimate hydraulic conductivity (cm/s) | Volumetric strain (%) | Cumulative eroded soil mass (g) |
|----------|--------------------------------|----------------------------|--|-----------------------|---------------------------------|
| 50EU | 0.021 | 11.71 | 2.8 | 3.94 | 250.60 |
| 50EU-R | 0.018 | 8.86 | 2.0 | 3.14 | 233.15 |
| 50ED | 0.020 | 10.05 | 1.9 | 3.36 | 233.30 |
| 50EC | 0.018 | 8.51 | 2.0 | 3.76 | 230.29 |

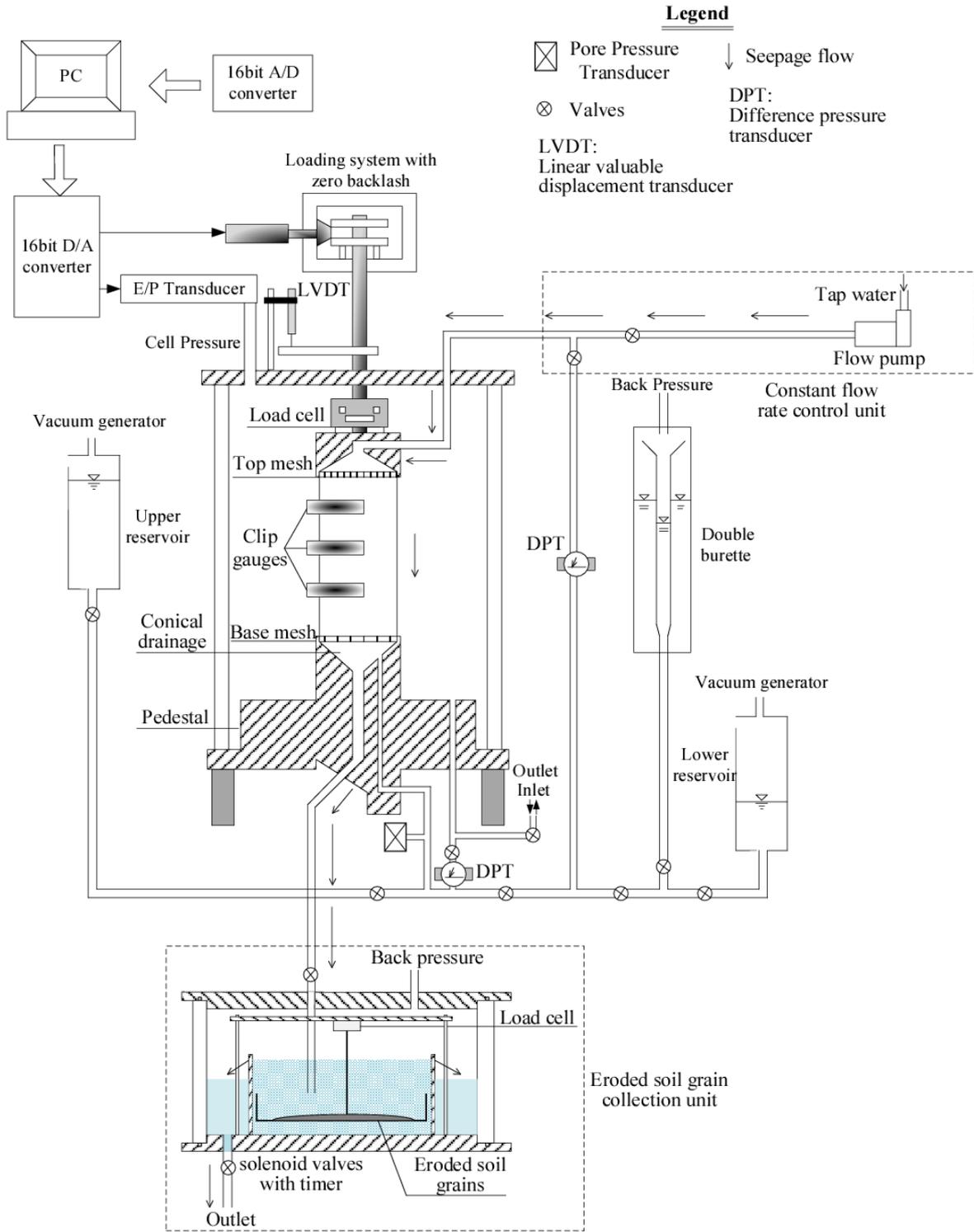
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Fig.1 Photography of the triaxial permeameter



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Fig.2 Schematic diagram of main triaxial seepage test assembly



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Fig.3 Details of spiral tube



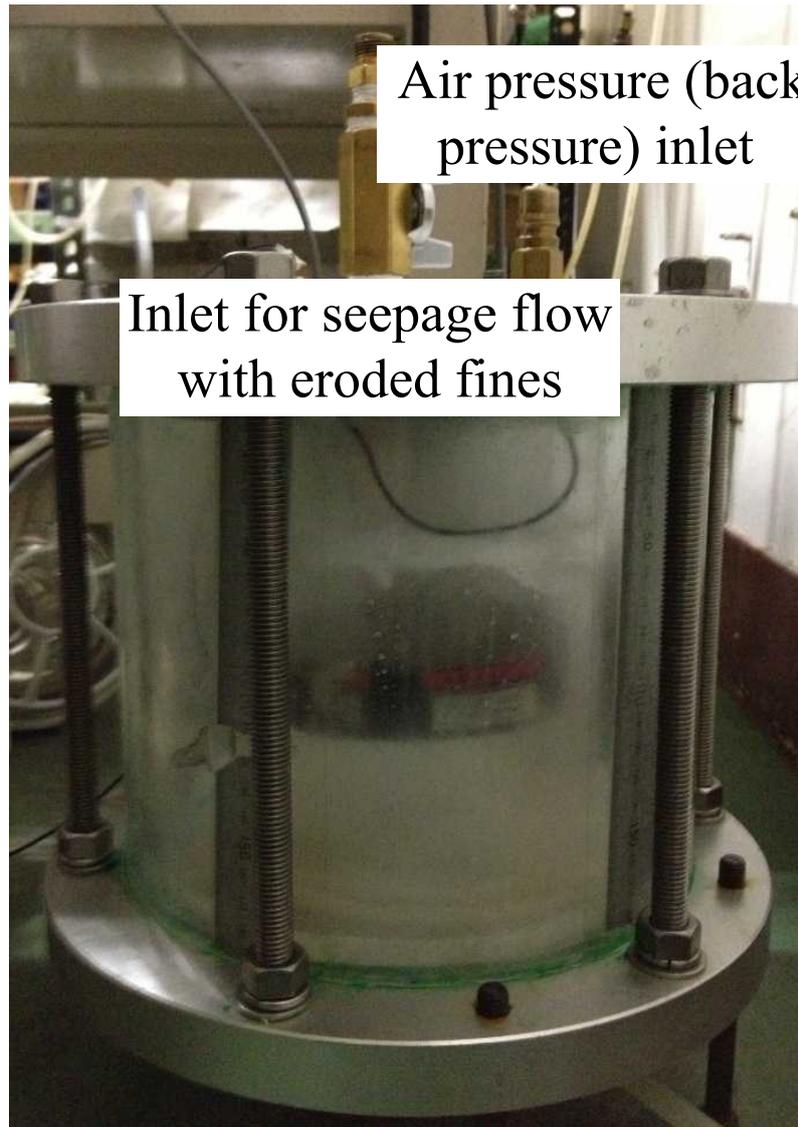
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Fig.4 Base pedestal



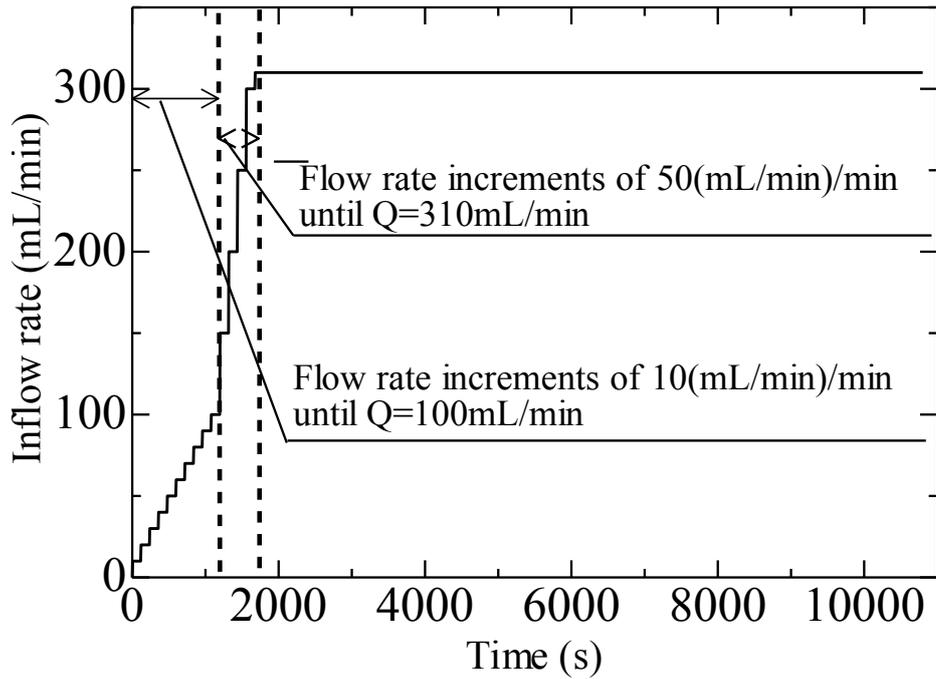
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Fig.5 Two 5mm-thick meshes (1mm opening)



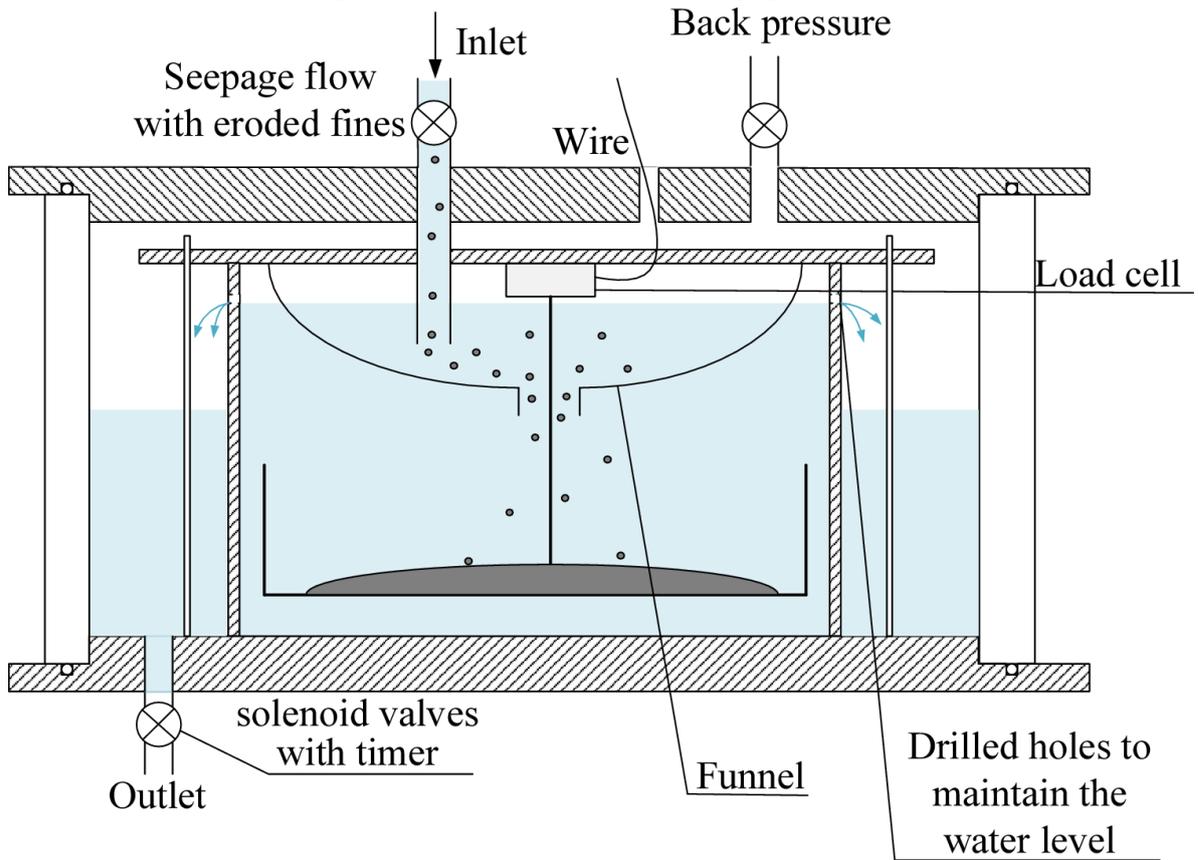
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Fig.6 Eroded soil grains collection unit



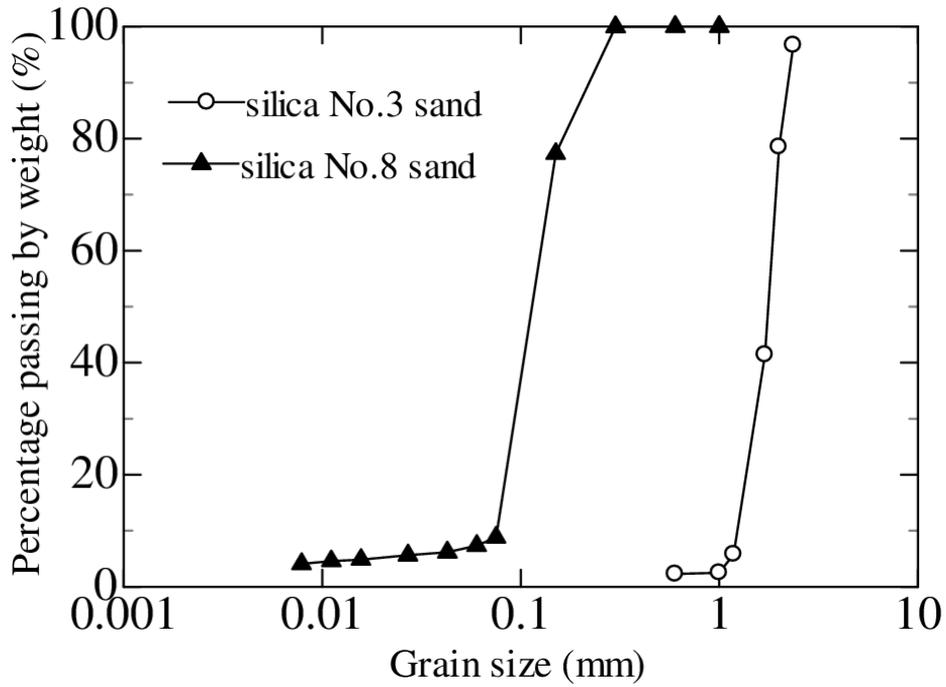
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Fig.7 Flow rate increments in seepage test



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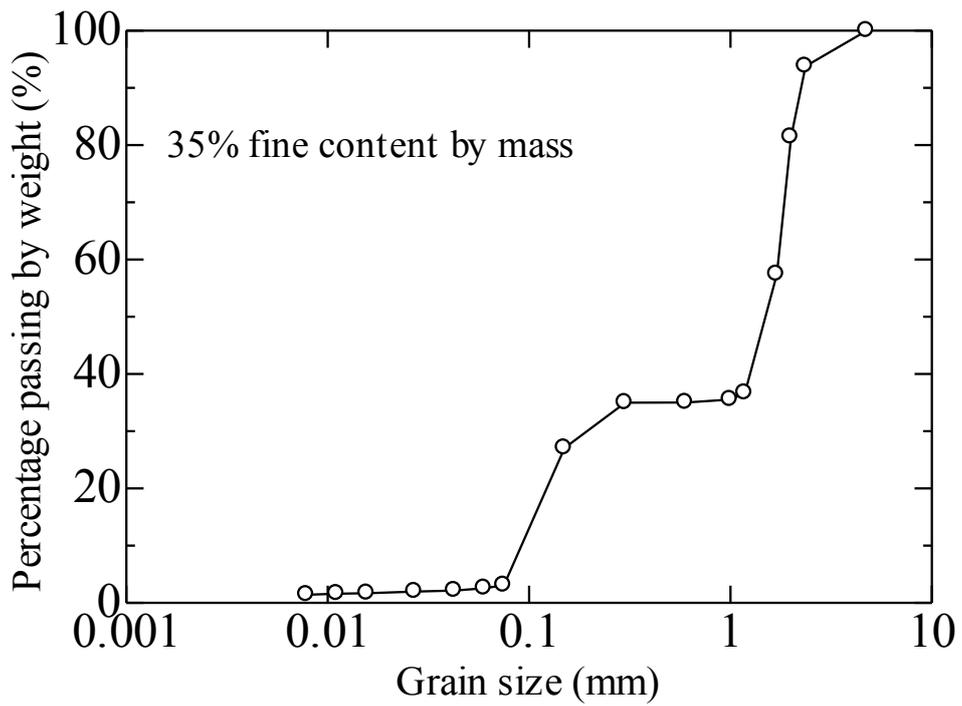
Fig.8 Improved eroded soil particles collection unit



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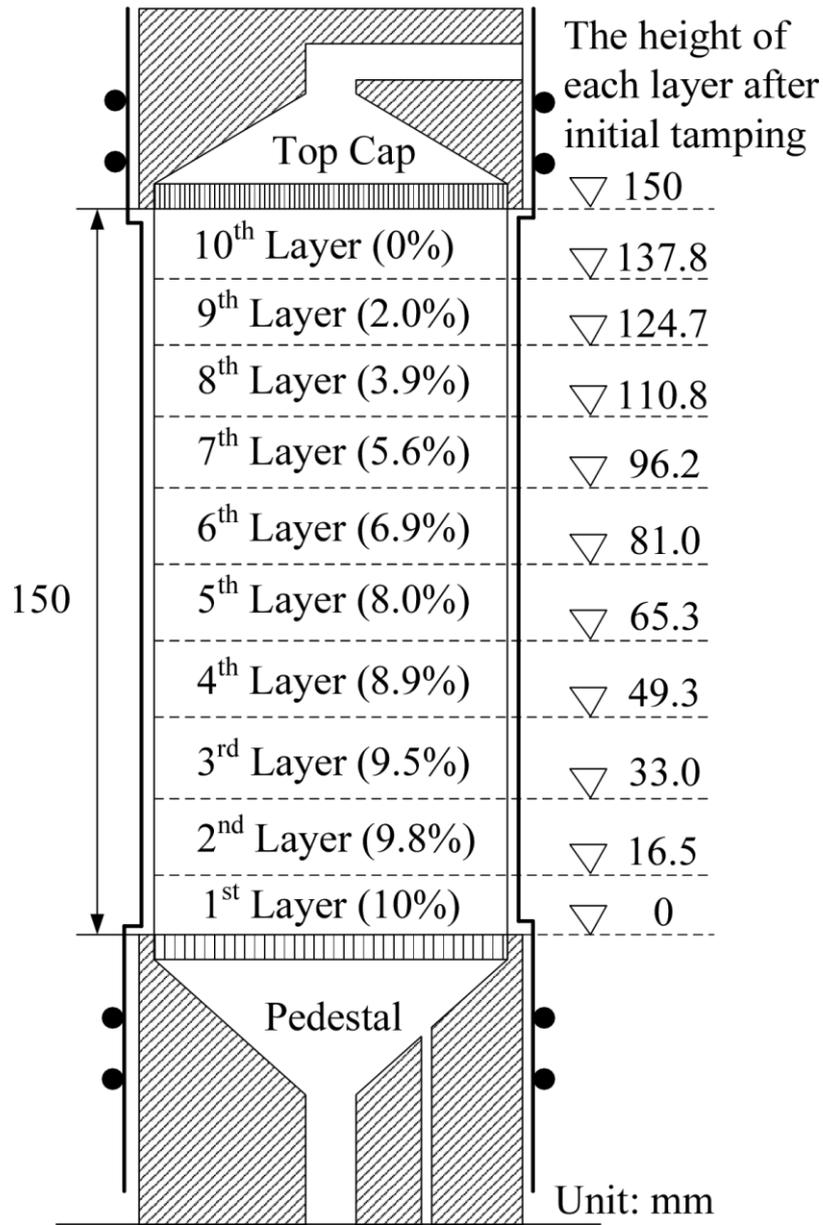
Fig.9 Grain size distribution curves of Silica No.3 and No.8



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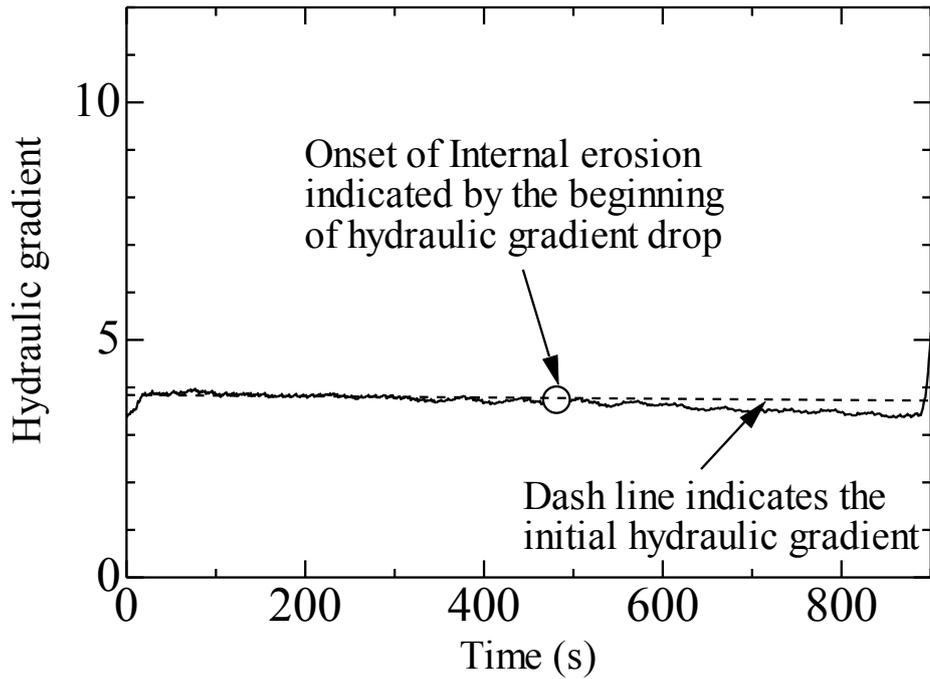
Fig.10 Grain size distribution curve of the mixture



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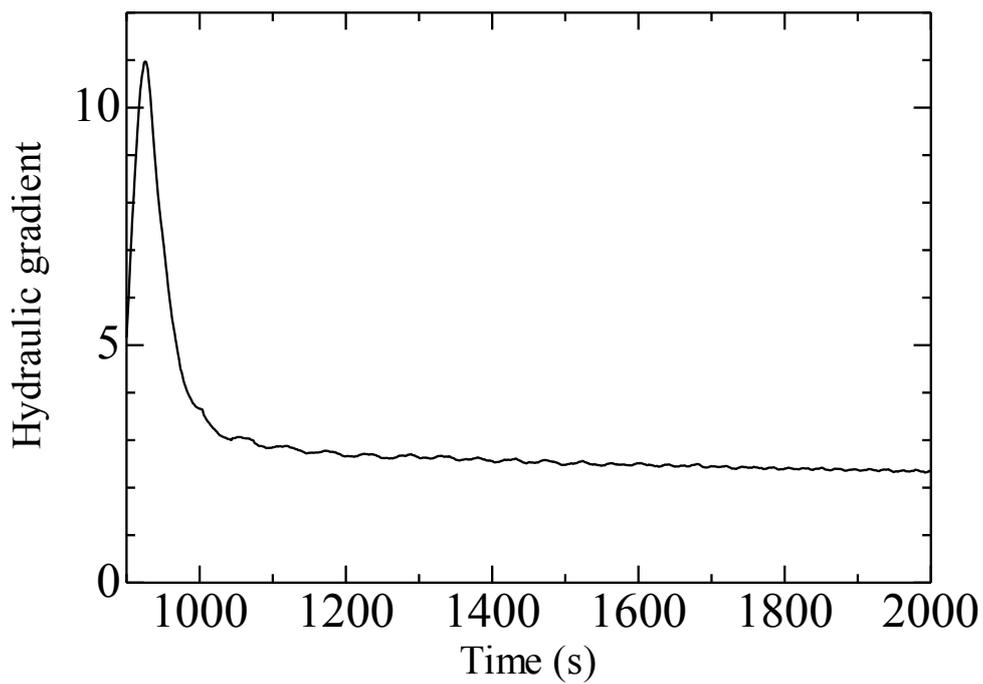
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Fig.11 Average Undercompaction of each layer



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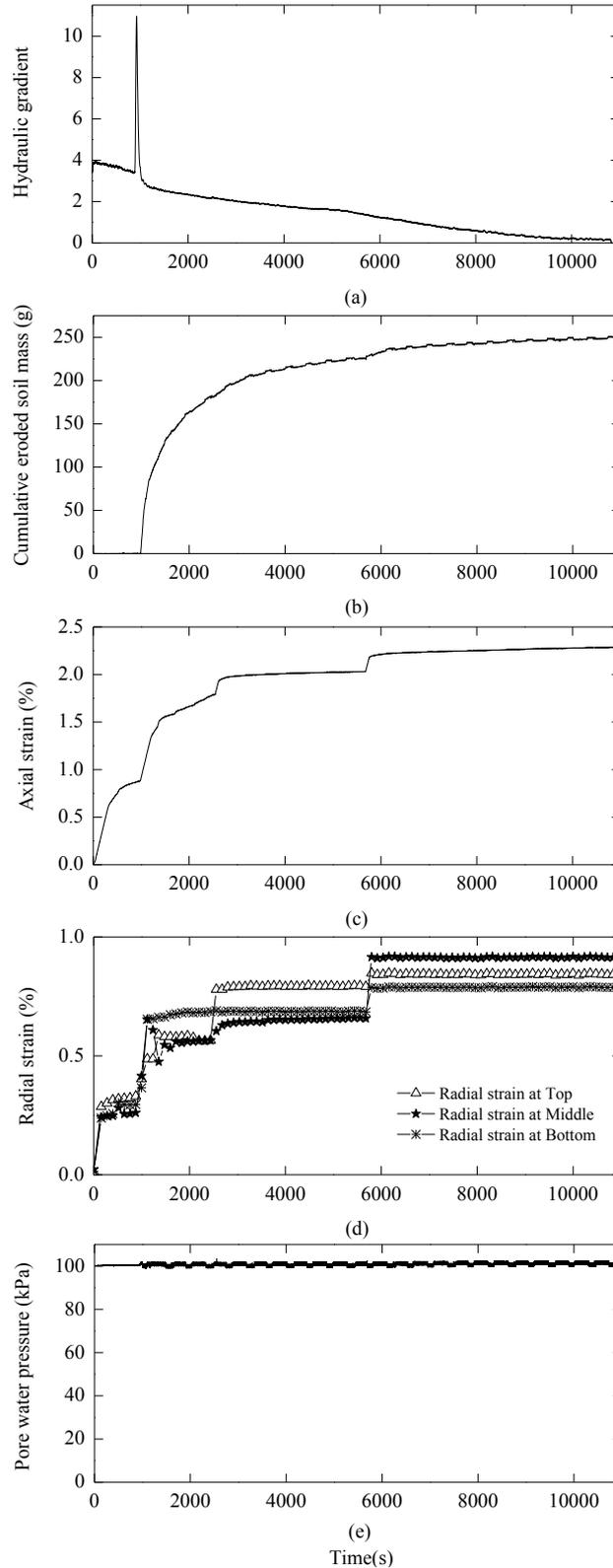
(a) Initial 900s since the beginning of seepage test



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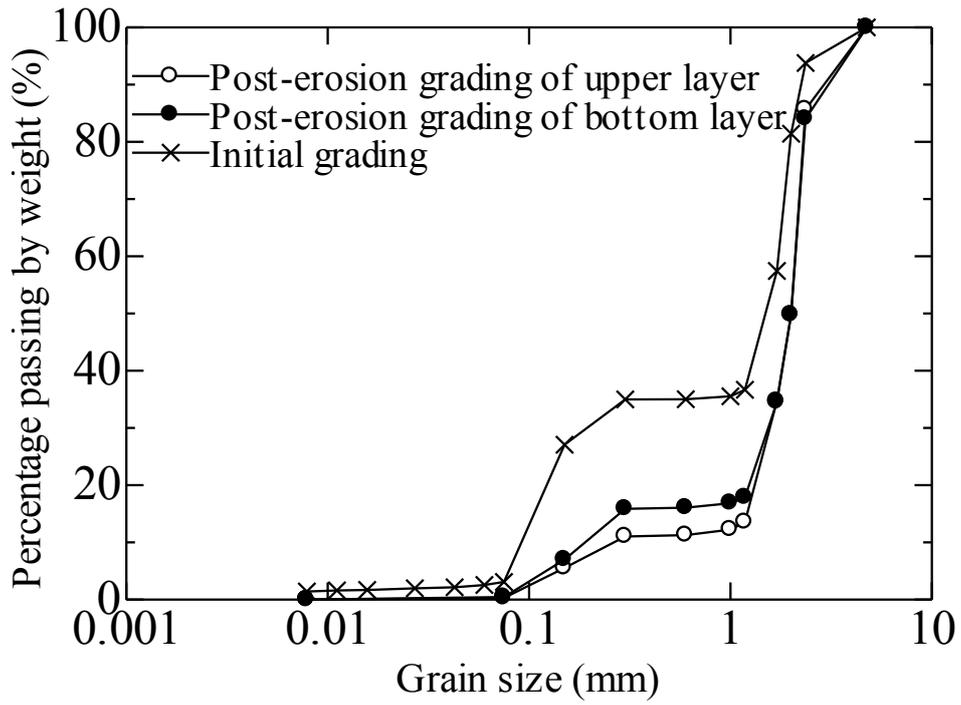
(b) From 900s to 2000s

Fig.12 Change of hydraulic gradient with time (Specimen 50EU)



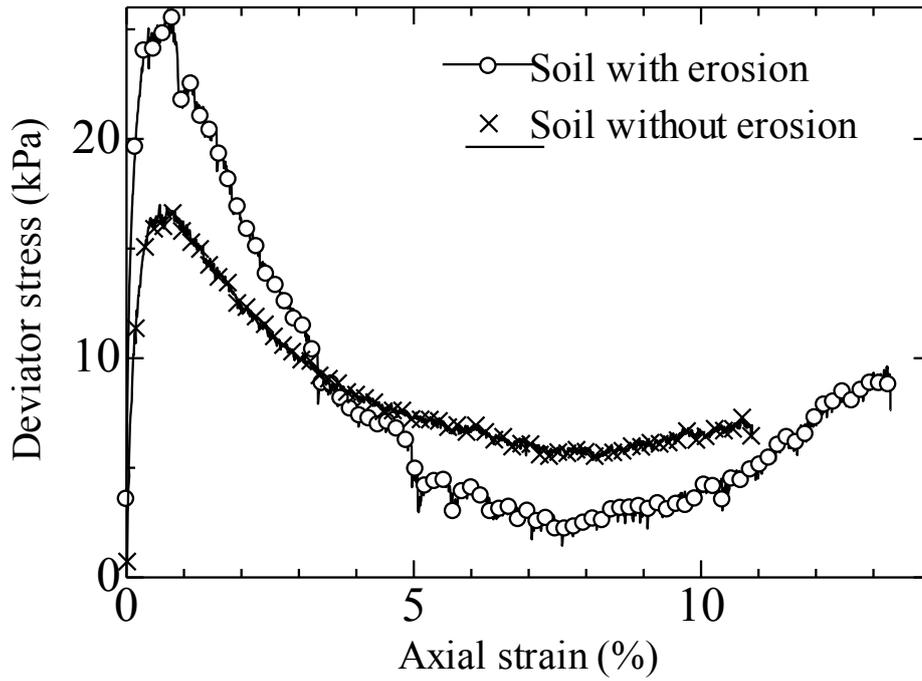
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894 Fig.13 Relation of parameters of seepage tests with time (Specimen 50EU): (a)
 895 Hydraulic gradient with time; (b) Cumulative eroded soil mass with time; (c) Axial
 896 strain with time; (d) Radial strain with time; (e) Applied back pressure during seepage
 897 test.



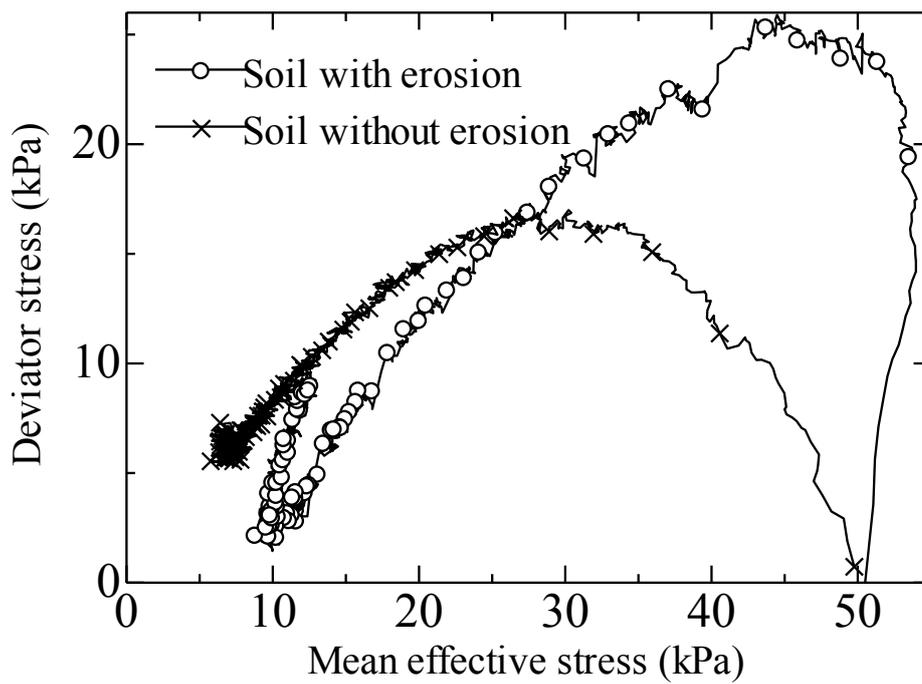
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Fig.14 Grain size distributions of the upper and bottom layer of soil specimen after internal erosion (Specimen 50EU)



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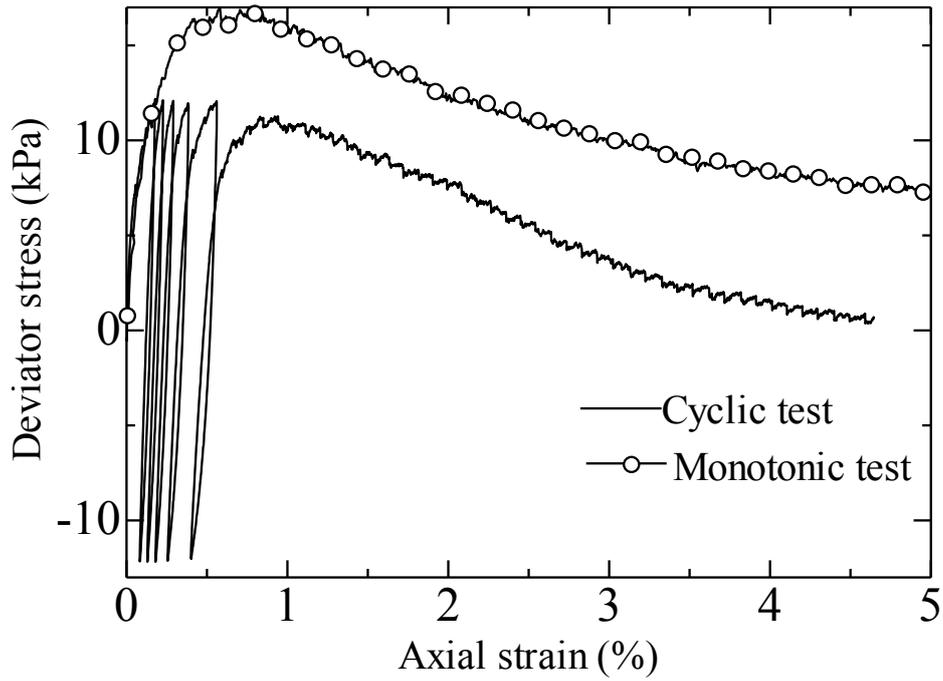
(a) Relation of deviator stress and axial strain



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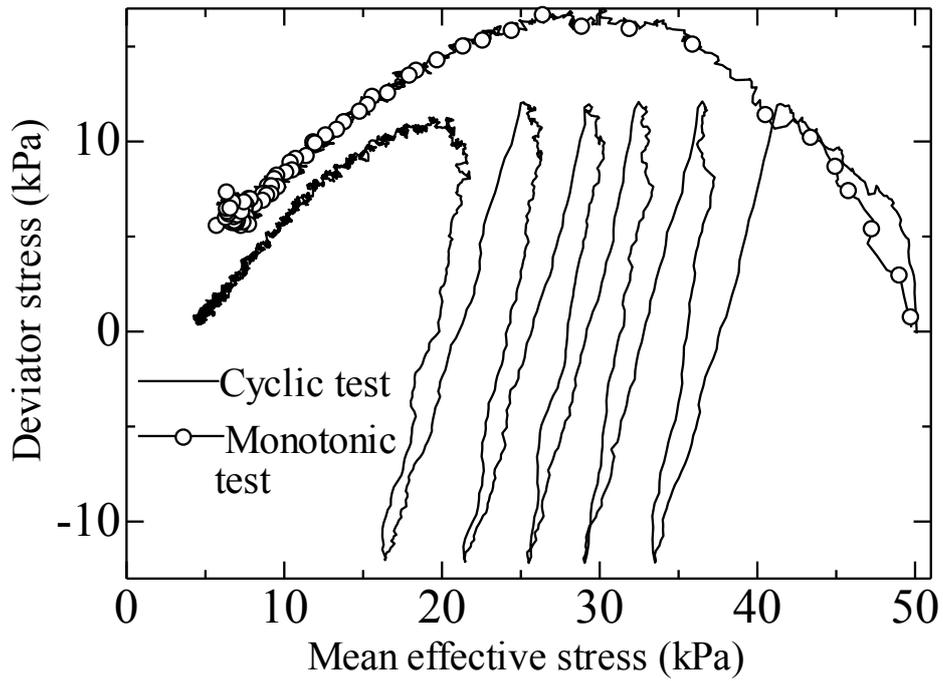
(b) Relation of deviator stress and mean effective stress

Fig.15 Undrained test on the specimens with erosion and without erosion



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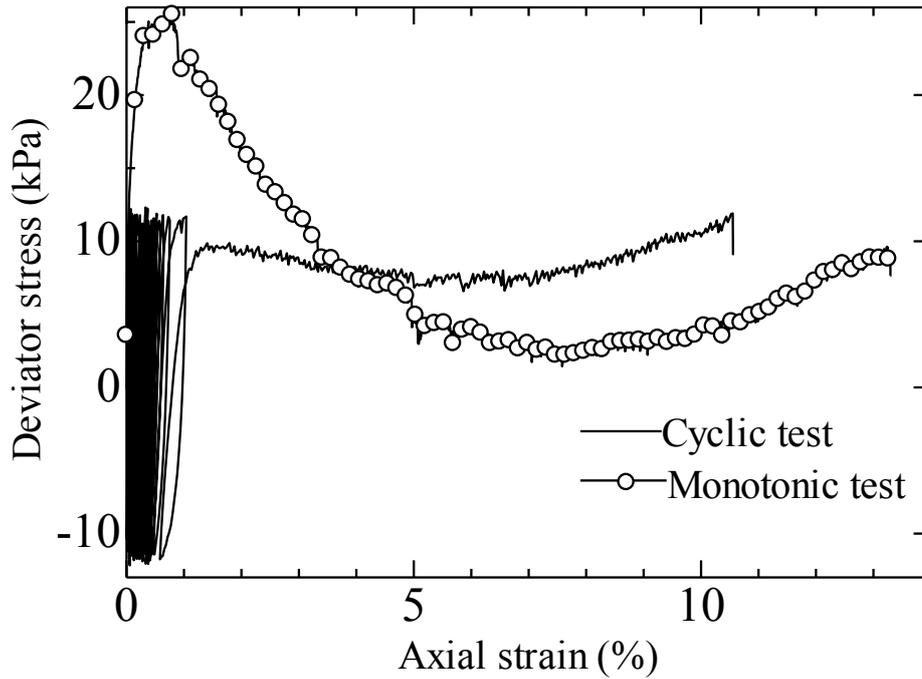
(a) Relation of cyclic deviator stress and axial strain with superimposed monotonic compression test data under undrained condition (CSR=0.12)



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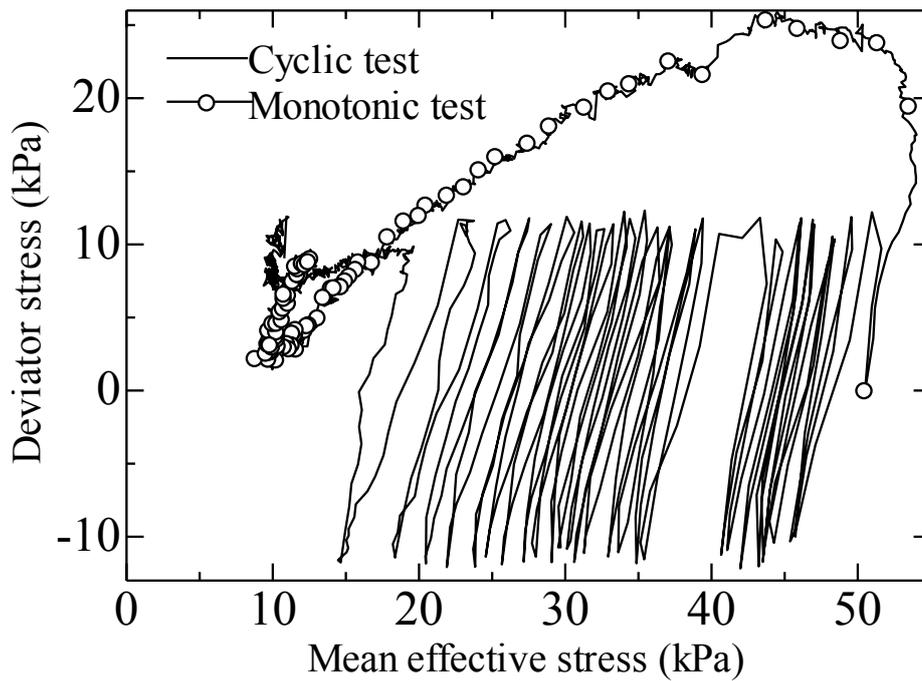
(b) Relation of cyclic deviator stress and mean effective stress with superimposed monotonic compression test data under undrained condition (CSR=0.12)

Fig.16 Cyclic behavior of NS specimen



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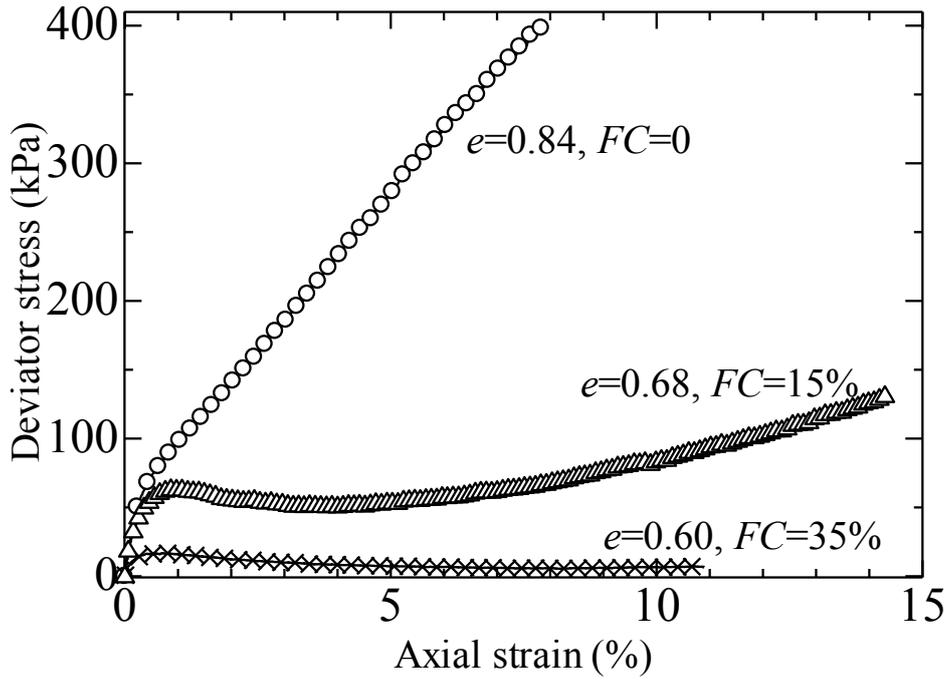
(a) Relation of cyclic deviator stress and axial strain with superimposed monotonic compression test data under undrained condition (CSR=0.12)



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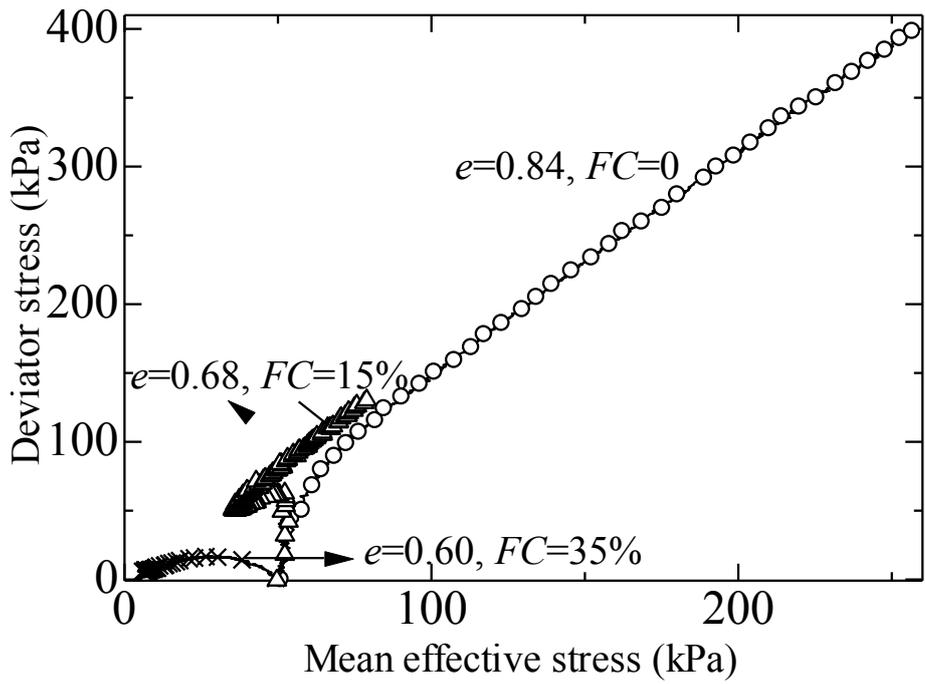
(b) Relation of cyclic deviator stress and mean effective stress with superimposed monotonic compression test data under undrained condition (CSR=0.12)

Fig.17 Cyclic behavior of ES specimen



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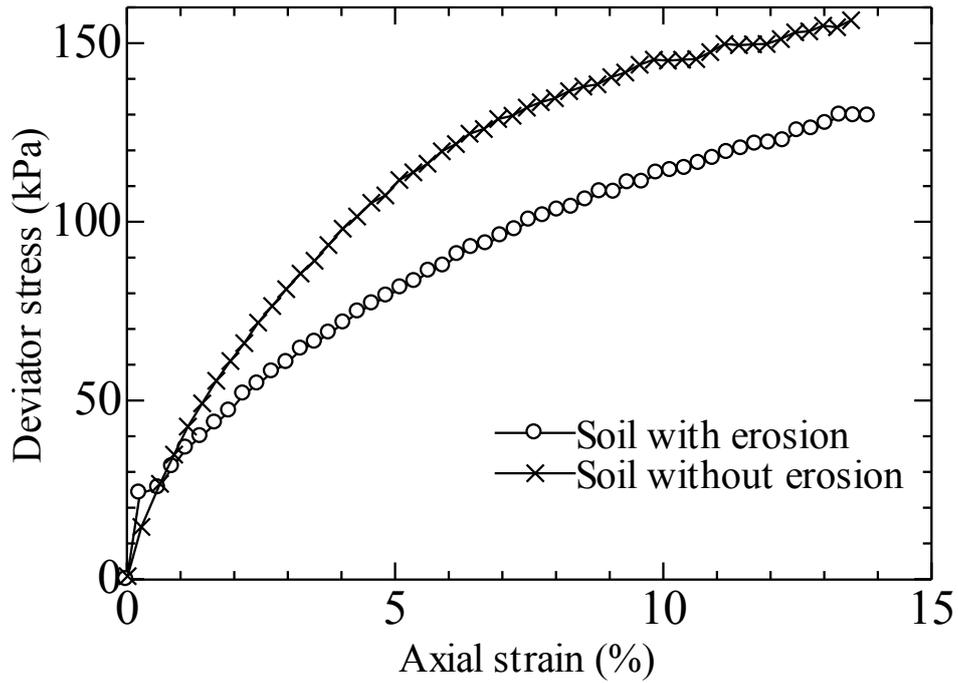
(a) Axial strain versus deviator stress



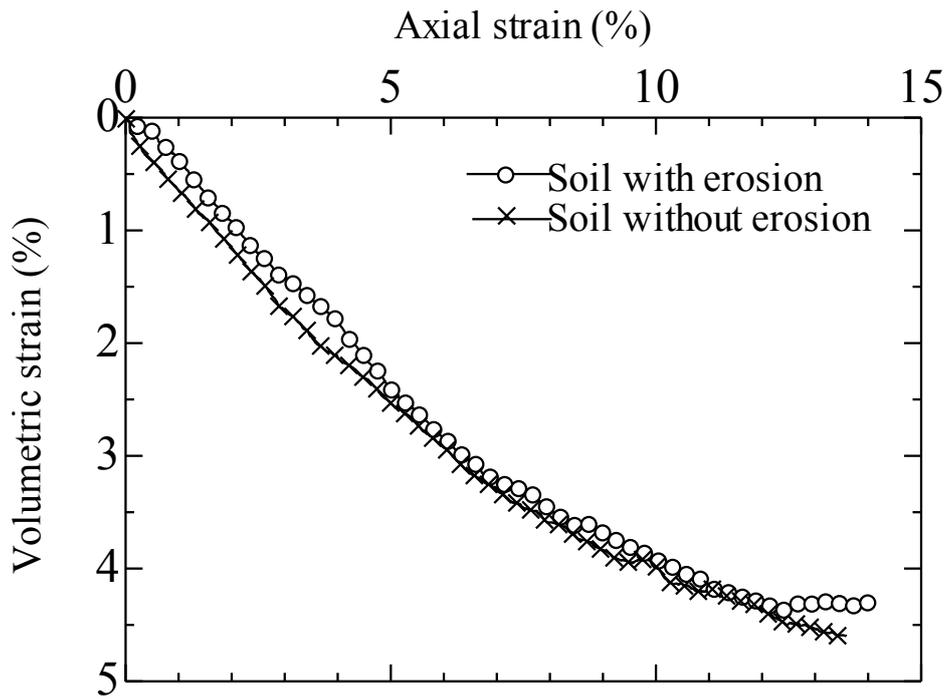
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(b) Mean effective stress versus deviator stress

Fig.18 Undrained response of the tested specimens with different fines content



(a) Relation of deviator stress and axial strain

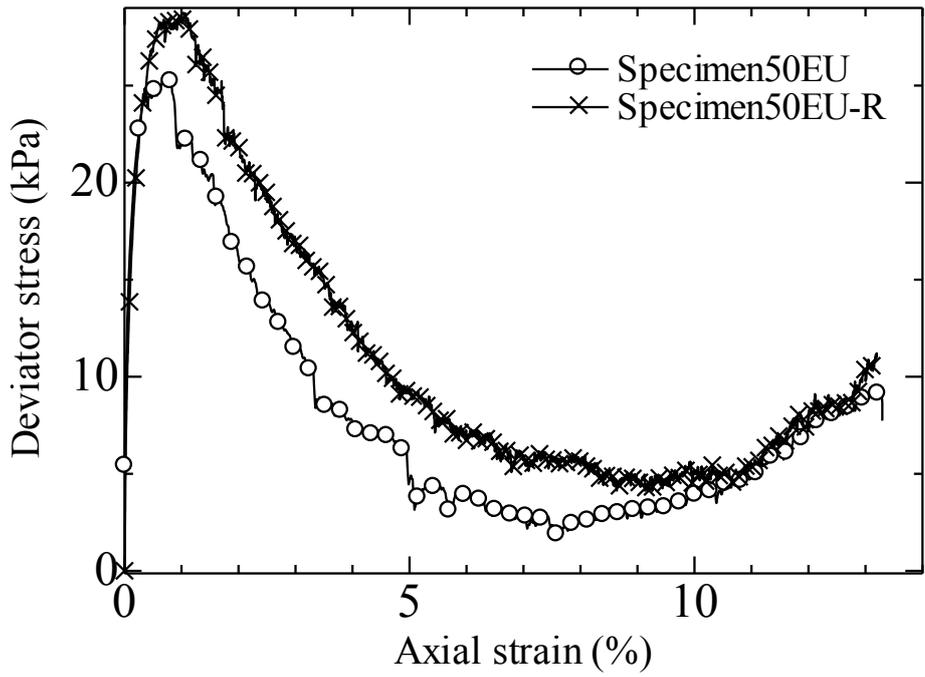


(b) Relation of volumetric strain and axial strain

Fig.19 Drained test on the specimens with erosion and without erosion

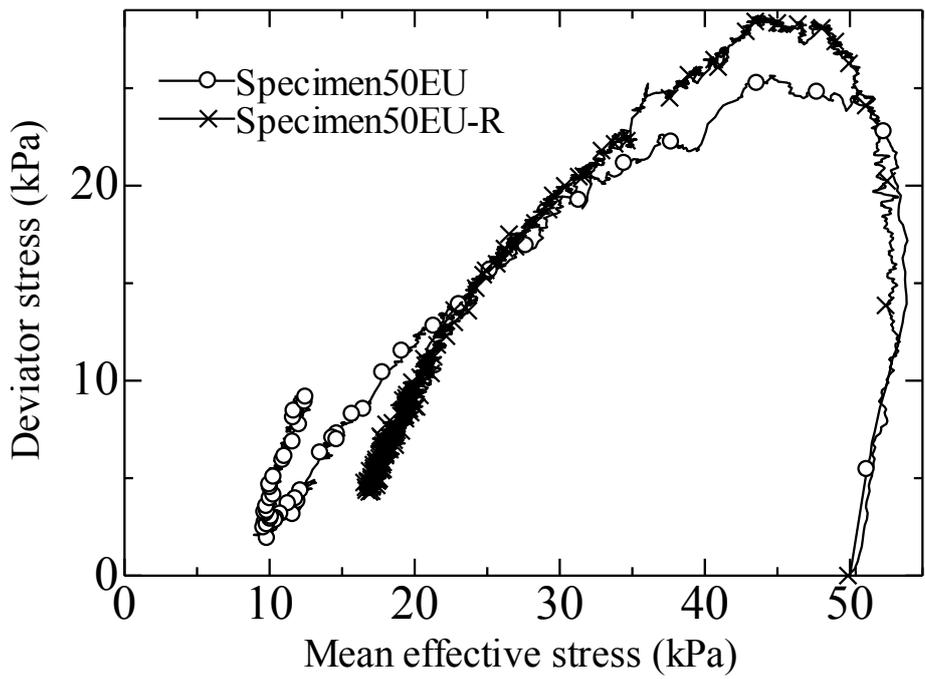
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(a) Axial strain versus deviator stress



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(b) Mean effective stress versus deviator stress

Fig.20 Repeatability of the undrained test on eroded specimen