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1 **Drained monotonic responses of suffusional cohesionless soils**

2
3 **Lin Ke¹ and Akihiro Takahashi²**

4
5 **Abstract**

6
7 Mechanical consequences of suffusion on the non-cohesive soils with various initial fines
8 contents under different initial effective confining pressures are presented in this paper. By
9 use of the modified triaxial permeameter, seepage tests and successive drained monotonic
10 compression tests are performed. It is found that soil drained strength decreases after
11 suffusion and a temporary drop in stiffness at the initial stage of shearing with respect to the
12 axial strain ranging from 0% ~ 1% is observed. The tests suggest that suffusion might create a
13 distinct packing of soil grains, which might result from possible accumulation of fine grains
14 at the spots where the constriction size, representing the size of pore channels in a soil, is
15 smaller than that of fines. Those “surviving” fines after suffusion may function as
16 reinforcement or jamming at the subsequent compression, resulting in a larger initial stiffness
17 of the suffusional soils.

18 **Keywords:** suffusion; drained response; cohesionless soil; soil packing

19
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24 **Introduction**

25

26 The phenomenon of suffusion in cohesionless soils exhibits itself as the gradual migration of
27 fine grains through the voids of the coarse matrix, transported by volumes of seepage water.
28 It is frequently detected in natural deposit and in earthen structures. The chronic process of
29 suffusion always accompanies with the significant dislodgement of soil grains and changes in
30 hydraulic conductivity. Suffusion may result in a loose soil structure because of the loss of
31 fine grains without great changes in the voids of the coarse matrix. The stress ~ strain
32 relationship of the suffusional soil might be greatly altered compared with the soil without
33 suffusion. There is a high possibility that the strength of the post-suffusion soil decreases due
34 to the destructive function of suffusion. Sugita *et al.* (2008) reported flow slide of several
35 embankments constructed on catchment topography (i.e., swamps and valleys) during Noto
36 Peninsula Earthquake of Japan. Because of the ground configuration, those embankments
37 may have been suffering from years of suffusion and chronically become too weak to resist
38 seismic shakings.

39

40 Although soil suffusion might be a huge threat for the stability of existing earthen structures,
41 unfortunately, few studies could comprehensively investigate the consequences of soil
42 suffusion from the perspective of soil mechanics. Chang and Zhang (2011) conducted drained
43 monotonic compression tests on a series of suffusional soil specimens in a revised triaxial
44 apparatus at different stress states. They concluded that the originally dilative soil would
45 become contractive after the loss of significant amounts of fine grains and the drained
46 strength decreased after the suffusion. Undrained monotonic compression tests on internally
47 eroded soil have been performed by Xiao and Shwiyhat (2012). They illustrated that the peak
48 deviator stress of suffusional soil was larger than that of the soil without suffusion, which

49 may be attributed to the low degree of saturation. Chang and Meidani (2012) classified the
50 mechanical behavior of suffusional soil into two categories depending on the confining
51 pressure when suffusion occurs. For the soil specimens that suffered suffusion under low
52 confining pressure, the post-suffusion void ratio was on the dense side of the steady state line
53 in void ratio \sim mean effective stress space, indicating a dilative response, whereas those
54 specimens that experienced suffusion under large confining pressure showed much
55 contractive response with a lower undrained strength. The mechanical consequences of
56 suffusion on soil seem to be obscure, which probably is due to the low saturation degree of
57 the tested specimens after suffusion. Xiao and Shwiyhat (2012) noted that the B-value of the
58 eroded soil specimens immediately after suffusion was approximately 0.86. The complicated
59 unsaturated soil behavior may produce confusing results. Therefore, further detailed testing
60 with the accurate measurements of pressures is necessary to elaborate the mechanical
61 behavior of eroded soil. Meanwhile, models for assessing the mechanical consequences of
62 suffusion have been proposed by Muir Wood *et al.* (2010). In their approach, the progress of
63 suffusion was approximated by progressively removing of grains from the assemblies of
64 circular discs at different stages of shearing. The modelling indicated that the suffusion would
65 alter the soil state from “dense” to “loose”. Hicher (2013) predicted the mechanical behavior
66 of granular materials subjected to particle removal by a micromechanics-based model and
67 concluded that erosion of soils may trigger diffuse failure in an earthen structure.

68

69 Full comprehension of the post-suffusion soil behavior is beneficial for the assessment of the
70 stability of potentially eroded earthen structures, such as levees. This study mainly discusses
71 the mechanical consequences of suffusion on non-cohesive soils. By utilizing the modified
72 triaxial permeameter, drained monotonic compression tests are performed on the suffusional
73 specimens, which would be helpful to understand the mechanical characteristics of

74 suffusional cohesionless soil.

75

76 **Experimental investigations**

77

78 The experimental investigations are performed using a modified triaxial permeameter, which
79 is capable of directly investigating not only the mechanism of suffusion but also the
80 corresponding change of soil mechanical behaviors induced by erosion of fine grains.
81 Detailed descriptions of the permeameter could be referred to Ke and Takahashi (2014).

82

83 ***Test materials***

84 In this study, the tested sand includes two types of silica sand (Silica No.3 and No.8) with the
85 same specific gravity of 2.645 but different dominant grain sizes (Ke and Takahashi 2012).
86 They are commercially available sands, frequently used as industrial polishing materials. The
87 siliceous sand is mainly composed by quartz, categorized as sub-rounded to sub-angular
88 material. Before testing, they are fully washed and dried to remove impurities. The grain size
89 distributions of Silica No.3 and No.8 are plotted in Fig. 1. Silica No.3 and No.8 correspond to
90 medium sand and fine sand, respectively (ASTM D2487-11). With larger grain size, Silica
91 No.3 works as the coarse fractions which are regarded as soil skeleton in the mixture,
92 whereas Silica No.8 is the erodible fine grains. Hereafter, without specification, the term
93 “fine grains” is referred to Silica No.8 for simplicity. The tested specimens are the binary
94 mixtures of the two sands by three different fines contents (percentage of mass ratios of fine
95 grains to total weight of soil specimen, *FC*), which are 35%, 25% and 15%. The grain size
96 distributions of the mixtures are shown in Fig. 1 indicating that all of the three specimens are
97 gap-graded. The vulnerability of tested specimens to suffusion are assessed by Kezdi’s
98 method (Kezdi, 1979), which indicates internally unstable characteristic of tested soils

99 $((D_{15c}/d_{85f})_{\text{gap}}=7.9>4$, where D_{15c} is the particle size at 15% by passing is finer of Silica No.3
100 (mm) and d_{85f} refers to the particle size at 85% by passing is finer of Silica No.8 (mm)).
101 Maximum and Minimum void ratios (e_{max} and e_{min}) of tested soil are summarized in Table 1,
102 showing that an increasing in the fines content results in a proportional reduction of e_{max} and
103 e_{min} within 0~35% fines content. This type of binary mixture is commonly referred as “coarse
104 domain soil” and the mechanical responses are largely dependent on the coarse fractions
105 (Lade *et al.*, 1998; Cubrinovski and Ishihara, 2002).

106

107 A summary of the test cases is shown in Table 2, where initial void ratio refers to the void
108 ratio of tested specimens under an effective confining pressure of 20kPa prior to
109 consolidation. Each specimen is prepared by moist tamping method that soil mixtures with an
110 initial moisture content of 10% are tamped to the target void ratio to avoid the segregation of
111 the two kinds of grains with different dominant sizes. A non-linear average undercompaction
112 criterion (Jiang *et al.*, 2003) is adopted to generate uniform soil specimens. The tamping on
113 each specimen is in a systematic manner to guarantee an identical input energy. The mean
114 effective stress at consolidation considered in this paper is 50kPa, 100kPa and 200kPa, which
115 approximately corresponds to the vertical effective stress at 5m, 10m and 20m depth,
116 respectively, on condition that groundwater table is at the ground surface and soil ground is
117 fully saturated. Some of the specimens experience suffusion at a constant inflow rate of
118 $5.17\times 10^{-6}\text{m}^3/\text{s}$ in the modified triaxial cell.

119

120 ***Test program***

121 The initial diameter and height of the moist tamped specimens prior to saturation is
122 approximately 70mm and 150mm, respectively. Necessary corrections, such as the effects of
123 buoyancy of the cap and soil, and membrane stiffness, have been considered. Overall, the test

124 program includes soil preparation, vacuum saturation, consolidation, seepage test and
125 compression test. A schematic diagram of the test procedure in the $p'-q$ stress space (mean
126 effective stress ~ deviator stress) is presented in Fig. 2. Vacuum saturation procedure (ASTM
127 D4767-11) is utilized to saturate the soil specimens. Approximately, the deaerated water with
128 a volume of 10.4 (normalized value in terms of pore volume) has been flowed through the
129 soil specimen. For the majority of tests, B values of at least 0.95 could be achieved after the
130 applying of 100kPa back pressure following the vacuum saturation procedure. The axial
131 displacement and average radial displacement have been recorded all the way to update the
132 present dimension of tested specimens. Upon completion of saturation, soil specimens are
133 isotropically consolidated until the preferred mean effective stress (i.e., 50kPa, 100kPa or
134 200kPa in this study) is reached. Seepage tests are performed at the stress state the same as
135 that of the specimen after isotropic consolidation. To demonstrate the mechanical effects of
136 suffusion on soils systematically, the imposed inflow rate for each specimen keeps constant
137 as $5.17 \times 10^{-6} \text{m}^3/\text{s}$, which is determined by considering the requirement of laminar flow,
138 restriction of excess hydrostatic pressure and acceptable range of fines loss. It may be argued
139 that a constant inflow rate could not reflect the real hydraulic conditions in dams, which is a
140 limitation of the apparatus. The seepage tests would be terminated at least after 3 hours. At
141 most circumstances, the post-suffusion B-value is larger than 0.93 because of the
142 maintenance of back pressure on the tested specimens. The axial displacement, radial
143 deformation and cumulative eroded fines mass are recorded to determine the fines content
144 and post-suffusion void ratio, which are of significance for the assessment of mechanical
145 responses. After the seepage test, a series of monotonic compression test is performed on the
146 suffusional soil without changing the cell pressure and the back pressure to investigate the
147 mechanical consequences of suffusion. The compression test, either drained or undrained test,
148 is displacement controlled with an axial strain rate of 0.1%/min, following the standard

149 criteria (ASTM D4767-11; ASTM D7181-11). The cell pressure is maintained constant while
150 the specimens are compressed at the designated strain rate.

151

152 **Mechanical influences of Silica No.8**

153

154 It is universally recognized that the presence of nonplastic fines creates a “metastable” soil
155 structure, which fundamentally alters the soil mechanical response at shearing from that of
156 clean sand. However, regarding the mechanical function of those nonplastic fines debates still
157 exist. In this paper, the tested soil mixtures contain amounts of nonplastic fine grains, Silica
158 No.8, up to 35% in mass ratio. The mechanical effects of Silica No.8 are elaborated first and
159 further mechanical behavior of soil before and after suffusion could be compared directly.

160

161 Figure 3 plots the relations of axial strain and deviator stress, and the corresponding effective
162 stress paths in p' - q diagram of the specimens with the fines contents of 35%, 25%, 15% and
163 0%, respectively, under an initial effective confining pressure of 50kPa, in the triaxial
164 compression tests under undrained condition. The skeleton sand consists of the coarse Silica
165 No.3 sand, whereas Silica No.8 serves as nonplastic fine grains. The reconstituted specimens
166 with fine grains are prepared by moist tamping method with an initial relative density of
167 approximate 47%. The moist tamped specimen of Silica No.3 is targeted at the largest
168 achievable void ratio to accentuate its dilative tendency even at loose condition. Details of
169 those specimens have been listed in Table 2. It is obviously noted that the presence of Silica
170 No.8 would decrease the soil strength, which may be attributed to the lubrication between
171 skeleton grains by the nonplastic fine grains, thereby smoothing the contacts among the
172 coarse grains. The loss of effective contacts may result in smaller soil stiffness and larger
173 compressibility. Thevanayagam and Mohan (2000) and Thevanayagam (2007) noted similar

174 evidences of the existence of the lubricated soil structures. In terms of effective stress paths,
175 the specimen with 35% fines content displays fully contractive behavior, whereas the soil
176 with less fines content becomes more dilative. Loose though, Silica No.3 without fine grains
177 exhibits fully dilative behavior throughout the compression. It is possible that for the
178 specimen containing 35% fine grains the coarse grains are separated apart by the relatively
179 large amounts of loose fine grains and the contractive behavior may be determined by the
180 compressibility of the fine grains deposited between the coarse grains. With the declining of
181 fines content, the coarse grains gradually contact with each other. The compression may force
182 the fine grains to slide into the voids and correspondingly the coarse grains move into a better
183 contact, causing dilatancy at larger axial strain. In sum, the presence of Silica No.8 decreases
184 the soil strength and inhibits the dilatancy tendency.

185

186 **Test results and discussions**

187

188 *Summary of seepage test results*

189 A concise summary of the seepage test results is presented for a fundamental understanding
190 of suffusion mechanism and its influence on the soil state. The seepage tests are performed by
191 assigning seepage fluid at a constant rate downwardly through the tested specimens by a flow
192 pump. The flow velocity, defined as the flow volume passing through unit area in unit time, is
193 sufficiently slow in the tests to guarantee a laminar flow condition. In the tests, the flow
194 velocity is gradually increased until it reaches the prescribed value of $5.17 \times 10^{-6} \text{m}^3/\text{s}$. Before
195 the onset of suffusion, without any fine grains loss, the hydraulic gradient keeps stable. Once
196 the Darcy velocity reaches critical velocity, the dislodgement of fine grains initiates and
197 correspondingly hydraulic gradient would drop, resulting in an increase in hydraulic
198 conductivity. Successive rising of Darcy velocity may further accelerate the progress of

199 suffusion and correspondingly, large amounts of fine grains would be dislodged, resulting in
200 the contractive deformation of the tested specimens. If the imposed flow rate is kept constant
201 at a value larger than critical velocity for a long period, the loss of fine grains would
202 gradually become constant, indicating the gradual decreasing of erosion rate. Along with the
203 loss of fine grains, coarse fractions may re-arrange their inter-position to reach a new
204 equilibrium and the volumetric deformation will cease. As a result, the tested specimens will
205 become loose. A summary of the changes of hydraulic parameters is indicated in Table 3.

206

207 The suffusional behavior of tested specimens is closely dependent on the hydraulic conditions.
208 In authors' tests, the assignment of seepage flow is realized by gradually raising the inflow
209 rate up to $5.17 \times 10^{-6} \text{ m}^3/\text{s}$ and maintaining this rate till several indicators become stable, such
210 as hydraulic gradient, cumulative eroded soil mass and volumetric strain. Evolution of
211 percentage of cumulative fines loss with time under different initial effective confining
212 pressures and initial fines contents is summarized in Figs. 4 and 5, respectively. It is noted
213 that for each case at the constant imposed flow rate soil experiences an initially sharp loss of
214 fine grains and gradual decreasing of erosion rate with time. The cumulative eroded soil mass
215 is larger under the smaller initial effective confining pressure and is larger for the specimens
216 with the larger initial fines content within the test range. The changes in fines content and
217 void ratios are summarized in Table 3, where the intergranular void ratio is derived by
218 regarding the volume of fine grains as that of voids. It is indicated that with the significant
219 loss of fine grains, the post-suffusion void ratios of tested specimens greatly increase.
220 Although different in the fines loss and post-suffusion void ratio, the suffusional specimens
221 with an initial fines content of 35% show similar intergranular void ratios, averagely equaling
222 to 1.3, which might be a practical comparison base for interpreting the suffusional soil
223 behavior for this study. The evolution of soil state induced by suffusion is plotted in void ratio

224 ~ fines content space (Fig. 6). The post-suffusion specimens have significantly large void
225 ratio, even larger than the maximum void ratio, and thus an extremely loose soil packing is
226 expected. A larger fines content and a smaller void ratio is observed for the specimens on
227 which seepage tests are performed under larger initial effective confining pressure, compared
228 with the specimens under lower initial effective confining pressure. Thevanayagam and
229 Mohan (2000) divided the mechanical behavior of the “coarse domain” soil mixture by a
230 demarcation line corresponding to $e_s \approx e_{cmax}$ (maximum void ratio of the coarse fractions) (Fig.
231 6). The positions of tested specimens are all above the demarcation line, indicating that the
232 packing of coarse grains is unstable and separated by fine grains, and the soil behavior is
233 affected by those active fine grains participating in the force chains. Due to the characteristics
234 of suffusion, local clogging or accumulation of fine grains might occur and consequently, a
235 particular packing of soil grains might be formed. Therefore, the drained responses of
236 suffusional soils may be different from that of the soil before suffusion.

237

238 ***Influence of initial effective confining pressure on mechanical response of suffusional soil***

239 As is discussed above, a lower effective confining pressure during suffusion would result in
240 larger volumes of voids in soil and more fines loss, and consequently, the mechanical
241 behavior of suffusional soil may be closely related with the confining pressure when
242 suffusion occurs. To reveal this relation, three drained compression tests have been conducted
243 on the suffusional specimens that initially contain 35% fine grains and have suffered
244 suffusion under the same initial effective confining pressure of 50kPa, 100kPa and 200kPa,
245 respectively. Although the post-suffusion void ratios vary for different specimens, the
246 intergranular void ratios are basically equal (i.e., approximately 1.3). If the intergranular void
247 ratio is accepted as the effective reference for the comparison of the mechanical behavior of
248 suffusional soils, the differences in the drained response may be mainly caused by the initial

249 effective confining pressure and the corresponding particular post-suffusion packing of soil
250 grains. The relation curves of deviator stress and axial strain accompanied with the evolution
251 of volumetric strain are plotted in Fig. 7, respectively, which indicate a typical contractant
252 volumetric behavior of loose sand. The deviator stress gradually develops and maintains
253 constant at a peak value, whereas the contractive volumetric strain rises to maximum and
254 keep constant. A majority of experimental investigations has revealed that an axial strain of
255 30% ~ 40% is necessary for achieving critical state of sand in drained test. Unfortunately, the
256 tests in this study were terminated at the axial strain of about 13% ~ 17%, which should not
257 be sufficiently large to present the full drained responses of suffusional specimens. To
258 compensate the limitation of insufficient straining and depict the whole picture of drained
259 behavior, a hyperbolic curve fitting is adopted to approximate the contractant soil behavior at
260 drained condition (Ferreira and Bica, 2006) and the extrapolated curves up to an axial strain
261 of 40% are shown in Fig. 7 by dash lines. It is worth to mention that the dash lines derived
262 from hyperbolic curve fitting are hypothetical. But considering the significantly large initial
263 void ratio of suffusional specimens, the fitting may reflect the drained behavior appropriately.
264 For comparison purpose, results of drained tests on the companion specimens (35N-50, 35N-
265 100 and 35N-200) under the same stress state as that of suffusional soil are plotted in Fig. 8.
266 The intergranular void ratio of companion specimens is around 1.4, slightly larger than that of
267 the suffusional soil. Herein, failure is defined as the soil state wherein the deviator stress
268 obtained at an axial strain of 15% (ASTM D4767-11; ASTM D7181-11) and correspondingly,
269 the soil strength refers to the deviator stress at an axial strain of 15%. Figure 9 displays the
270 stress ratio at failure, ratio of deviator stress to current mean effective stress, against the
271 initial effective confining pressure, indicating that the soil strength decreases after suffusion
272 and the extent of decreasing becomes smaller at larger initial effective confining pressure. It
273 can be explained that under larger initial effective confining pressure, less fine grains would

274 be dislodged by seepage flow and consequently less changes occurred in the packing of soil
275 grains, resulting in less drop in soil strength after suffusion. In terms of the volumetric strain
276 at failure in Fig. 10, the patterns of behavior of companion specimens are in accordance with
277 the common sense: because of the dilatancy tendency soil commonly fails at smaller
278 volumetric strain under smaller effective confining pressures, and the greater contractive
279 behavior is expected under larger effective confining pressures. However, a different
280 response, departing from common sense, is observed for the suffusional specimen: volumetric
281 strain at failure is larger under lower initial effective confining pressure and it becomes
282 smaller under larger initial effective confining pressure. It can be understood that under lower
283 initial effective confining pressure, more fine grains are eroded away and greater increment in
284 void ratio occurs, and correspondingly at the subsequent compression, for specimen 35E-50,
285 the effect of void ratio increment may surpass that of the dilatancy tendency under lower
286 effective confining pressure. Consequently, larger volumetric strain at failure is observed at
287 low initial effective confining pressure.

288

289 To fully interpret the reduction of soil strength after suffusion, the critical friction angle is
290 estimated. In this study, the critical state might not be reached at an axial strain of 13% ~ 17%
291 where compression tests are terminated and extrapolation of the data is necessary. The
292 identification of critical state is fulfilled by plotting the stress ~ dilatancy relation of the
293 drained tests on suffusional and companion specimens, and extending the curve to the point
294 of intersection with the zero dilatancy axis. An unique critical stress ratio $(q/p')_{cs}$ could be
295 evaluated as 1.64 and 1.74 for the suffusional and the companion specimens, and accordingly,
296 the derived critical friction angle is 40.1° and 42.4° , respectively. Due to suffusion, the
297 critical friction angle decreases by 5.7%. It may be argued that as an intrinsic physical
298 property critical friction angle should be constant regardless of the change of void ratio after

299 suffusion. However, accompanying with void ratio variation, fines content of suffusional
300 specimens have been significantly reduced, which may cause the reduction of critical friction
301 angle. Further experimental investigations on relative angularity of tested grains might be
302 beneficial to explain the change of friction angle, which might beyond the scope of the study.
303

304 Besides, a temporary declining in soil stiffness at the initial stage of shearing with respect to
305 the axial strain ranging from 0% ~ 1% is observed. Figure 11 displays the variation of secant
306 stiffness at the initial 1% of axial strain. The soil stiffness has been normalized by the current
307 mean effective stress in order to compare the cases with different effective confining
308 pressures and accentuate the uniqueness of suffusion induced packing of soil grains. For the
309 comparison purpose, the secant stiffness of the companion specimens is superimposed. Since
310 the companion specimens are similar in terms of the initial fines content and void ratio, the
311 variation of normalized secant stiffness with axial strain displays identical patterns of
312 behavior. The stiffness shows the initially largest value and declines with further compression.
313 However, the behavior pattern of the suffusional specimens is distinct from the companion
314 specimens in three aspects. Firstly, the initial secant stiffness becomes larger than that of the
315 companion specimens, which may be explained by the reinforced soil packing created by
316 suffusion. It is postulated that fine grains may probably be impeded and gradually accumulate
317 at the spots where the size of the pore tunnels, formed by coarse grains, is less than that of the
318 fine grains. At subsequent compression, those fine grains function as jamming rather than
319 lubrication, and thereby reinforcing the packing of soil grains. Secondly, temporary drops in
320 soil stiffness are observed for suffusional specimens 35E-50, 35E-100 and 35E-200, at the
321 axial strain of 0.5%, 0.4% and 0.2%, respectively. It is considered as the evidence of the
322 deterioration of the temporary reinforced soil packing with further straining. Under larger
323 effective confining pressure, the reinforcement may be easily destroyed and therefore, the

324 stiffness drop in specimen 35E-200 is found at lower axial strain. Thirdly, because of the
325 extremely loose state of the suffusional specimens, the normalized secant stiffness keeps
326 lower than that of the companion specimens after the stiffness drop.

327

328 *Influence of initial fines content on mechanical response of suffusional soil*

329 Differences in initial fines content directly result in a different soil packing before suffusion,
330 which will exert an influence on the progress of suffusion and the post-suffusion soil packing.

331 As is shown in Fig. 5, a larger amount of fines loss is observed at the specimen with larger
332 initial fines content. An understanding of the effects of initial fines content may shed light on
333 the evolution of soil packing during suffusion and mechanical responses of suffusional soil.

334 The analysis below is limited to the tests under an initial effective confining pressure of
335 50kPa, which show the largest increment in void ratio and drop in soil strength.

336

337 In a specimen, a fraction of fine grains fill the voids, whereas another fine grains separate the
338 coarse grains. Since the fine grains occupying the voids among the coarse grains may hardly
339 participate in force chains (Skempton and Brogan, 1994), the fine grains in the voids may be
340 vulnerable to suffusion and probably dislodged by seepage flow. Erosion of the fine grains
341 effectively separating the coarse grains may occur at larger Darcy's flow and the
342 rearrangement of coarse grains occurs to reach new equilibrium. Majority of the "surviving"
343 fine grains after three-hour seepage test are wedged between coarse grains and actively
344 participating in the force chains. Because of the larger voids size among coarse grains of the
345 specimen with 35% initial fines content (specimen 35E-50) compared with other specimens
346 (specimen 25E-50 and 15E-50), if the relative density is similar and fine grains are merely
347 considered as voids, specimen 35E-50 may show larger loss of fine grains. Under the same
348 initial effective confining pressure of 50kPa, different although the initial fines content is, the

349 specimens show approximately similar post-suffusion fines content (i.e., 10%~13%) but
350 different post-suffusion void ratios, as is shown in Table 3. Because of the obvious
351 differences in post-suffusion void ratio, the drained responses of those suffusional specimens
352 should be different. Figure 12 shows the results of drained compression test on specimen
353 35E-50, 25E-50 and 15E-50 under an initial effective confining pressure of 50kPa. Specimen
354 35E-50, which is the largest in post-suffusion void ratio, exhibits the lowest soil strength and
355 secant stiffness. In terms of volumetric strain, three specimens show similar amounts of
356 contractive strain within the initial 6% axial strain. Afterwards, specimen 15E-50, which is
357 the smallest in post-suffusion void ratio, become dilative at an axial strain of 14%, and
358 similarly specimen 25E-50 exhibiting dilatancy at an axial strain of 19%. Specimen 35E-50
359 does not show dilative behavior within test range.

360

361 **Distinctive packing of soil grains after suffusion**

362

363 Monotonic compression tests have revealed the somewhat different soil responses of the
364 suffusional soil: under the larger initial effective confining pressure it exhibits a less
365 volumetric strain and a temporal decline in soil secant stiffness is observed within the initial
366 1% axial strain. Since the intergranular void ratio of the suffusional specimens are
367 approximately the same and the effective confining pressure may not be sufficiently large to
368 trigger grain crushing (i.e., a maximum initial effective confining pressure of 200kPa), the
369 soil responses should be dominated by the post-suffusion soil packing and the soil grain
370 movement during shearing.

371

372 To signify the distinguished packing of soil grains after suffusion, monotonic drained test on
373 a reconstitute specimen with similar fines content and initial void ratio as that of suffusional

374 specimen 35E-50 is performed. The reconstituted specimen with an initial fines content of
375 15% is prepared by moist tamping method, targeting at the largest achievable void ratio.
376 Because of the occurrence of large volumetric deformation during consolidation, the void
377 ratio before compression is 0.81, still less than the post-suffusion void ratio of 1.0 for
378 specimen 35E-50. Figure 13 shows the drained responses of the two specimens in terms of
379 stress ~ strain relationship and corresponding development of volumetric strain. Due to the
380 larger void ratio, the suffusional specimen mostly gains less strength. However, careful
381 examination of the stress ~ strain curves within the initial 1% axial strain shows that the
382 initial secant stiffness of suffusional specimen is larger than that of the reconstituted
383 specimen and a sudden drop in deviator stress is observed around 0.5% axial strain, after
384 which soil strength and secant stiffness keep smaller than those of the reconstituted specimen
385 throughout the test range.

386

387 The above test suggests a distinguished packing of soil grains after suffusion, different from
388 reconstituted fine-grains-containing sand. Specifically, compared with the denser
389 reconstituted specimens, the suffusional specimen still becomes much stiffer at the beginning
390 of shearing. It is inferred that along with the seepage flow amounts of fine grains keep being
391 dislodged and coarse grains rearrange their positions into a new equilibrium. Because of
392 possible clogging, fine grains might be accumulated at the spots where the constriction size,
393 representing the size of pore channels in a soil, is smaller than that of fine grains. Due to the
394 rearrangement of grains, those accumulated fine grains may actively participate in force
395 chains. Different from the function of “lubrication”, those “surviving” fine grains after
396 suffusion would probably perform like reinforcement or jamming. Thereafter, the reinforced
397 post-suffusion soil packing renders the suffusional specimen much stiffer and less
398 compressible at the beginning of shearing. With the subsequent compression the

399 reinforcement is deteriorated and the suffusional specimen may behave like typical fine-
400 grains-containing sand. To further validate this assumption, a microscopic observation of the
401 post-suffusion packing of soil grains might be necessary.

402

403 **Conclusions**

404

405 The mechanical consequences of suffusion on a series of cohesionless soils are presented in
406 this paper. The tested specimens consist of the binary mixtures of Silica sand No.3 and No.8.
407 With larger grain size, Silica No.3 works as the soil skeleton, whereas Silica No.8 is the
408 erodible fine grains. Mechanically, the presence of Silica No.8 would decrease the soil
409 strength and inhibit the dilatancy tendency of Silica No.3, which may be due to the
410 lubrication function of the nonplastic Silica No.8 deposited between the skeleton grains. By
411 utilizing the modified triaxial permeameter, seepage tests are performed on those specimens
412 to create suffusion condition, and drained monotonic compression tests are performed on the
413 suffusional specimens to reveal their mechanical behavior.

414

415 Soil strength decreases after suffusion and the amounts of drops become smaller under larger
416 initial effective confining pressure. Departing from the pattern of behavior of the companion
417 specimen, the suffusional soil behaves differently: its volumetric strain at compression is
418 larger under lower initial effective confining pressure and it becomes smaller under larger
419 initial effective confining pressure. In terms of soil stiffness, the initial secant stiffness of
420 suffusional soil becomes larger than that of the companion soil and a temporary drop in soil
421 stiffness at the initial stage of shearing with respect to the axial strain ranging from 0% ~ 1%
422 is observed. It may be regarded as the evidence of the deterioration of the temporary
423 reinforced soil packing with further straining and that reinforcement may be easily destroyed

424 under larger initial effective confining pressure.

425

426 Under the same initial effective confining pressure of 50kPa, the specimen with larger initial
427 fines content shows a larger amount of fine grains loss during the seepage test, resulting in a
428 larger post-suffusion void ratio. At the subsequent compression, this specimen would exhibit
429 lower soil strength and secant stiffness.

430

431 Compression test results have revealed the probable existence of a distinctive packing of soil
432 grains after suffusion. The “surviving” fine grains after suffusion may actively participate in
433 the force chains, acting like reinforcement. The reinforced post-suffusion soil packing renders
434 the suffusional specimen much stiffer and less compressible. With the subsequent
435 compression the reinforcement will be deteriorated and the suffusional specimen may behave
436 like typical fine-grains-containing sand.

437

438 **Acknowledgement**

439

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442 KAKENHI Grant Numbers 25420498.

443

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491

492 **Table 1** Physical properties of tested soils

Physical properties	Silica No.3	Silica No.8	Mixtures with 35% Silica No.8	Mixtures with 25% Silica No.8	Mixtures with 15% Silica No.8
Fines content (<i>FC</i>) (%)	---	---	35	25	15
Maximum void ratio	0.94	1.33	0.74	0.77	0.79
Minimum void ratio	0.65	0.70	0.36	0.37	0.53

493

494 **Table 2** Details of tested specimens

Specimens	Initial <i>FC</i> (%)	Initial void ratio (e_i)	Mean effective stress at consolidation (kPa)	Post consolidation void ratio (e_c)	Relative density (%)	Type of compression
35E-50	35.0	0.59	50	0.55	48.5	Drained
35E-100	35.0	0.60	100	0.56	47.5	Drained
35E-200	35.0	0.64	200	0.57	46.2	Drained
25E-50	25.0	0.61	50	0.60	42.8	Drained
15E-50	15.0	0.68	50	0.68	43.1	Drained
35N-50	35.0	0.59	50	0.55	48.5	Drained
35N-100	35.0	0.61	100	0.56	47.5	Drained
35N-200	35.0	0.59	200	0.54	51.1	Drained
35U-50	35.0	0.60	50	0.56	47.5	Undrained
25U-50	25.0	0.61	50	0.58	47.8	Undrained
15U-50	15.0	0.68	50	0.67	46.9	Undrained
0U-50	0.00	0.88	50	0.88	21.8	Undrained

Note: Specimens named with “E” means seepage tests have been performed on the specimens at a constant inflow rate of $5.17 \times 10^{-6} \text{ m}^3/\text{s}$, whereas those with “N” indicate the companion specimens without suffusion. Those specimens named with “U” are prepared for study of mechanical influence of fine fraction.

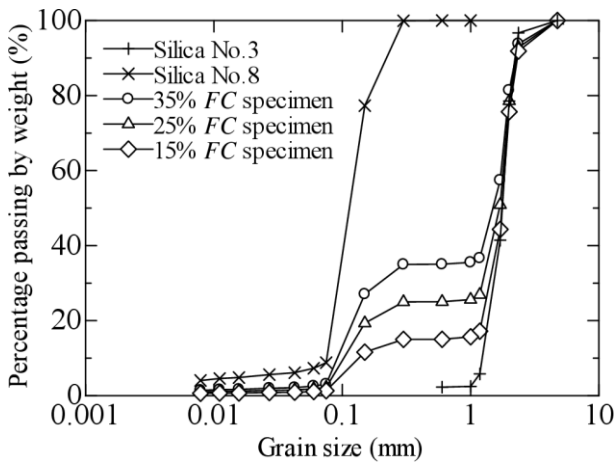
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Table 3 Summary of soil states after suffusion/before compression

Specimen	$i_{max}^{(1)}$	$k_i^{(2)}$ (m/s)	$k_e^{(3)}$ (m/s)	$FC^{(4)}$ (%)	$e_e/e_c^{(5)}$	$e_s^{(6)}$
35E-50	11.7	9.7×10^{-5}	0.028	13.5	1.0	1.29
35E-100	7.17	1.0×10^{-4}	0.010	15.9	0.92	1.29
35E-200	10.5	1.0×10^{-4}	0.008	24.5	0.77	1.34
25E-50	5.05	1.0×10^{-4}	0.009	12.0	0.81	1.06
15E-50	2.07	1.2×10^{-4}	0.010	9.98	0.78	0.98
35N-50	---	---	---	35.0	0.55	1.39
35N-100	---	---	---	35.0	0.56	1.40
35N-200	---	---	---	35.0	0.54	1.37

Note: (1) Maximum hydraulic gradient, i_{max} ;
 (2) Initial hydraulic conductivity before suffusion, k_i (m/s);
 (3) Post-suffusion hydraulic conductivity, k_e (m/s);
 (4) Fines content after suffusion/before compression for suffusional specimens and initial fines content for companion specimens, FC (%);
 (5) Void ratio after suffusion/before compression for suffusional specimens, e_e and post-consolidation void ratio for companion specimens, e_c ;
 (6) Intergranular void ratio $e_s=(e_e+FC/100)/(1-FC/100)$ (suffusional specimens) and $e_s=(e_c+FC/100)/(1-FC/100)$ (companion specimens).

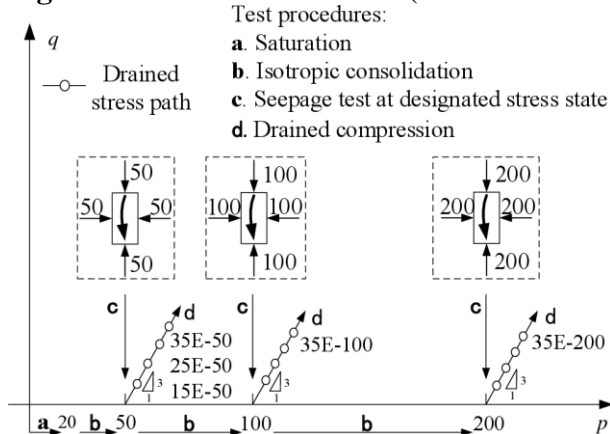
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Fig. 1. Grain size distributions (FC indicates fines content)

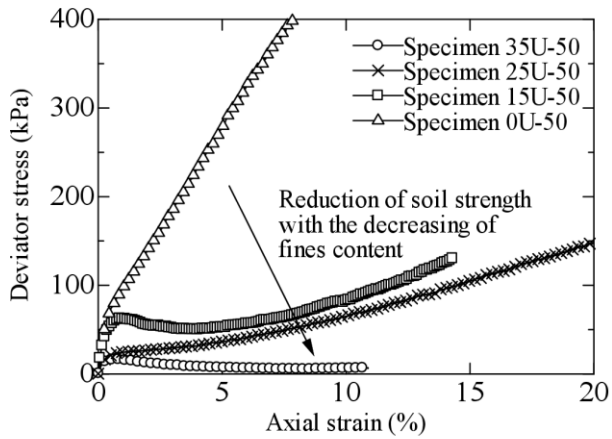


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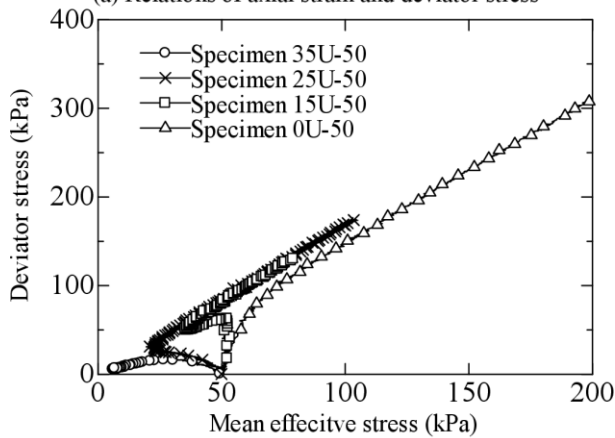
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Fig. 2. Schematic diagram of test procedures in p' - q space with test cases



(a) Relations of axial strain and deviator stress

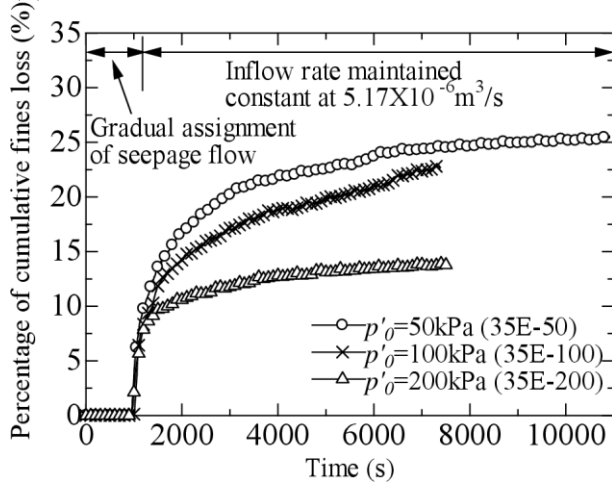


(b) Relations of mean effective stress and deviator stress

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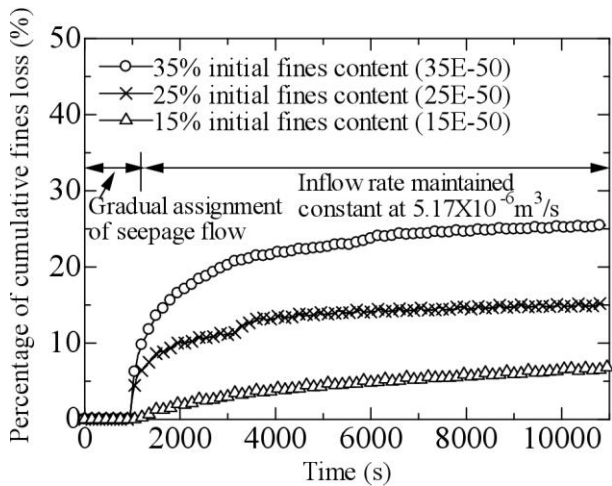
Fig. 3. Undrained compression tests on specimens with different contents of Silica No.8 under an initial effective confining pressure of 50kPa

(a) Relations of axial strain and deviator stress
(b) Relations of mean effective stress and deviator stress

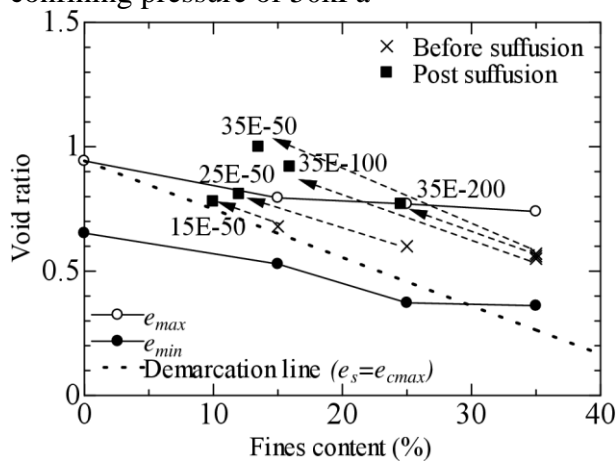


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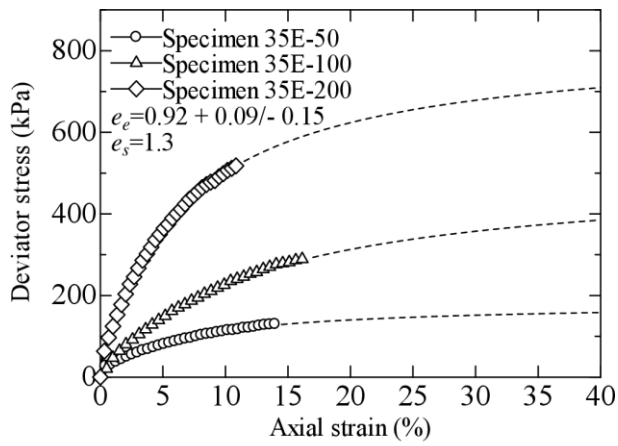
Fig. 4. Cumulative eroded soil mass with time for specimens with 35% initial fines content under different initial confining pressures



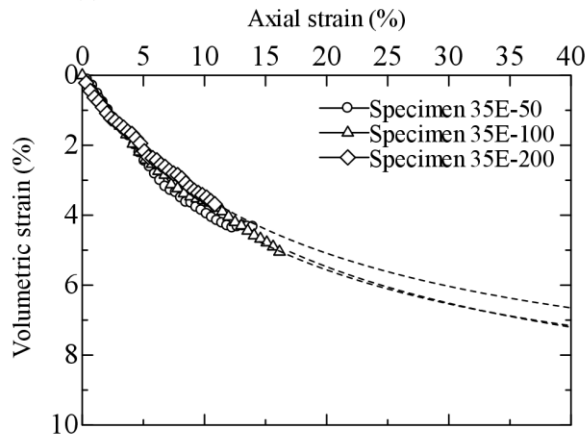
511
512 **Fig. 5.** Cumulative eroded soil mass with time for specimens tested under an initial effective
513 confining pressure of 50kPa



514
515 **Fig. 6.** Changes of soil state induced by suffusion in fines content ~ void ratio space



(a) Relations of axial strain and deviator stress



(b) Relations of axial strain and volumetric strain

516

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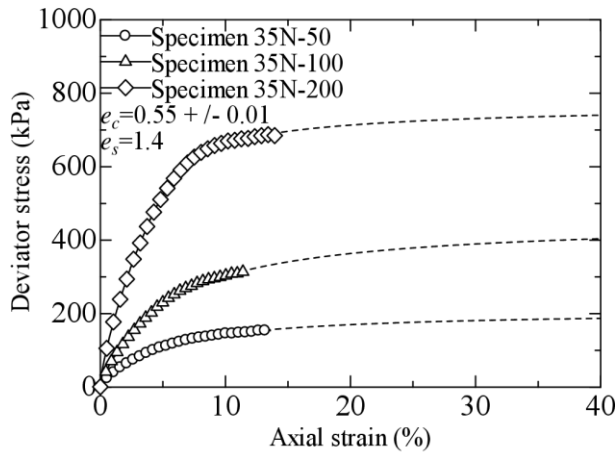
Fig. 7. Drained compression tests on suffusional specimens under different initial effective confining pressures (Dash lines indicate the extrapolated curve by a hyperbolic fitting)

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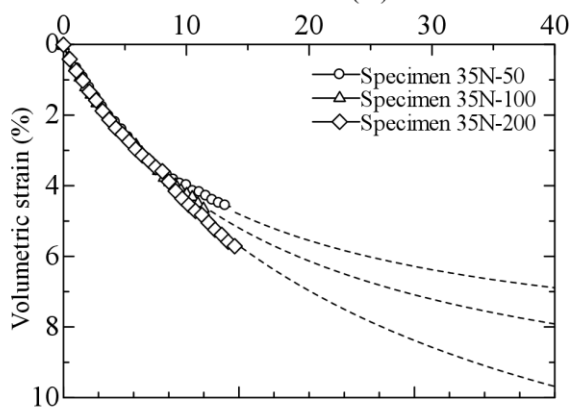
(a) Relations of axial strain and deviator stress

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(b) Relations of axial strain and volumetric strain



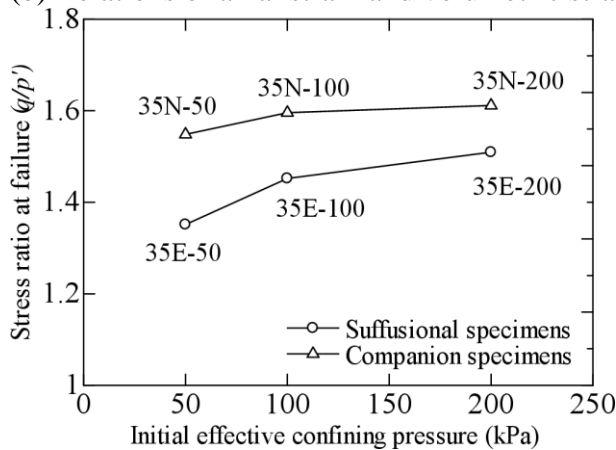
(a) Relations of axial strain and deviator stress



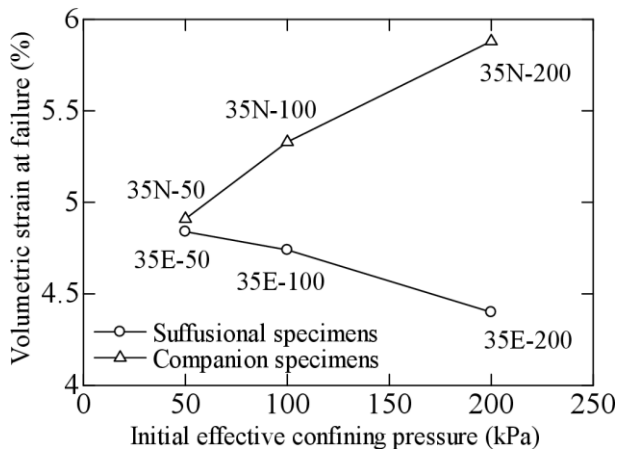
(b) Relations of axial strain and volumetric strain

521 **Fig. 8.** Drained compression tests on companion specimens under different initial effective
 522 confining pressures (Dash lines indicate the extrapolated curve by a hyperbolic fitting)
 523

524 (a) Relations of axial strain and deviator stress
 525 (b) Relations of axial strain and volumetric strain

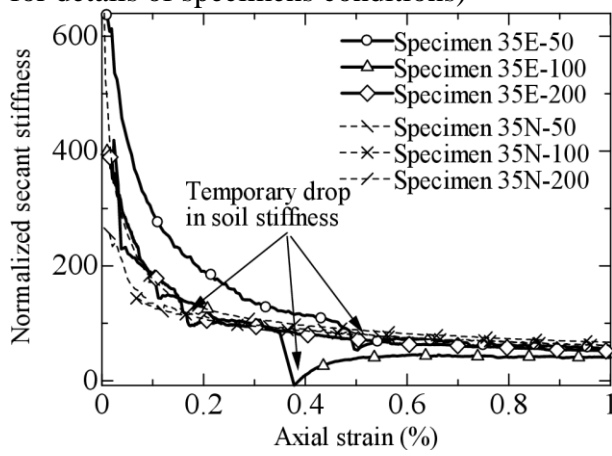


526 **Fig. 9.** Stress ratio at failure against initial effective confining pressure (refer Table 3 for
 527 details of specimens conditions)
 528



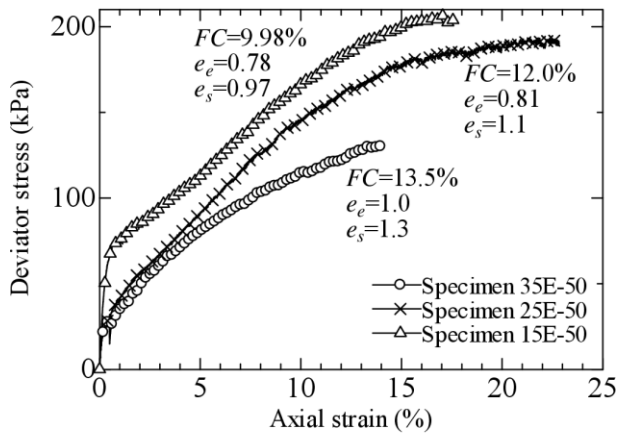
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Fig. 10. Volumetric strain at failure against initial effective confining pressure (refer Table 3 for details of specimens conditions)

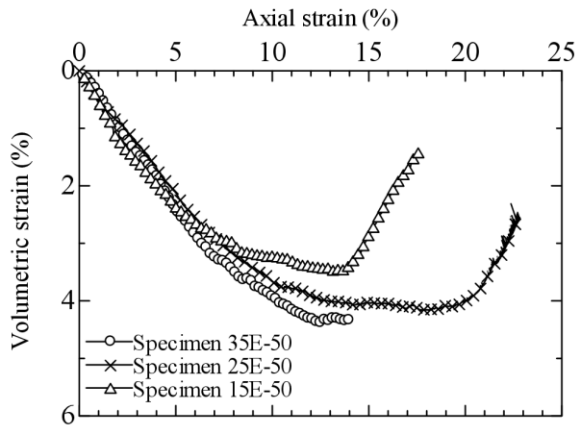


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Fig. 11. Normalized secant stiffness within 1% of axial strain



(a) Relations of axial strain and deviator stress



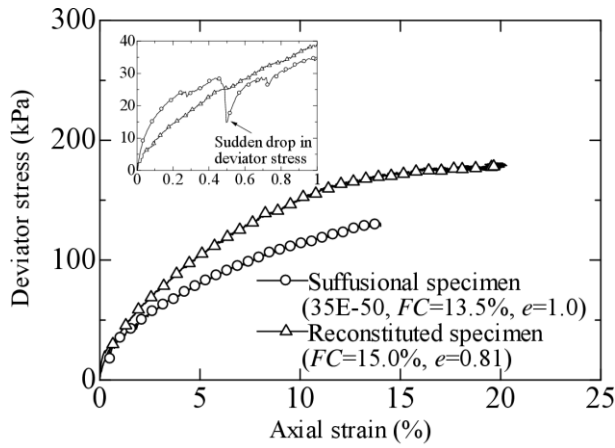
(b) Relations of axial strain and volumetric strain

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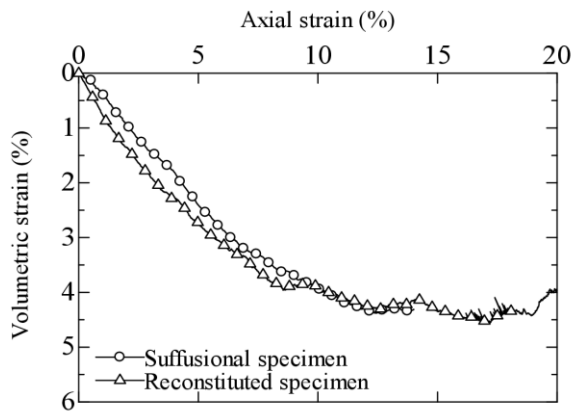
535 **Fig. 12.** Drained responses of suffusional specimens with different initial fines contents under
 536 an initial effective confining pressure of 50kPa

537 (a) Relations of axial strain and deviator stress

538 (b) Relations of axial strain and volumetric strain



(a) Relations of axial strain and deviator stress



(b) Relations of axial strain and volumetric strain

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541
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Fig. 13. Drained responses of suffusional specimen and reconstituted specimen under an initial effective confining pressure of 50kPa

(a) Relations of axial strain and deviator stress
(b) Relations of axial strain and volumetric strain