

論文 / 著書情報
Article / Book Information

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Category(English)	Doctoral Thesis
種別(和文)	論文要旨
Type(English)	Summary

論文要旨

THESIS SUMMARY

専攻 : Department of	物性物理学	専攻	申請学位 (専攻分 博士 野) : Academic Degree Requested	Doctor of (理学)
学生氏名 : Student's Name	汪 正元		指導教員 (主) : Academic Advisor(main)	村上 修一
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要旨 (英文 800 語程度)

Thesis Summary (approx.800 English Words)

In this thesis, we study fractional quantum Hall (FQH) states with thin (but finite) torus geometry, where the original two-dimensional system in a magnetic field can be regarded as a one-dimensional lattice model with short-range interactions. Based on this point of view, we discuss exactly solvable one-dimensional lattice models describing the filling factor $\nu = 1/q$ Laughlin states. Using the matrix product method, the physical properties of those states are obtained analytically. We further discuss the relationship between the hierarchy of FQH states and the Haldane conjecture for quantum spin chains, by mapping the $m=1$ Jain states to effective spin chains. We also discuss the $\nu = 1/2$ FQH states in a system with Landau level mixing. The one-dimensional lattice model has a ladder structure, and the Hamiltonian can be rewritten with projection operators by converting the 2-body interaction into 3-body one.

We review the standard theory for the FQH problem. This theory well describes the FQH states as incompressible quantum fluids based on the variational wave functions. However, the supposed wave functions are written in a first-quantized form, so that there are few methods to understand the physical origin and the physics of the states. We also review some important works based on the one-dimensional framework for the FQH states with torus geometry. In the TT (Tao-Thouless a.k.a. thin-tours) limit, the model is exactly solvable, and the eigenstates can be derived. Nevertheless phase transitions occur upon deformation of the torus, in even denominator states.

We then introduce models with an exact ground state describing the $\nu = 1/q$ FQH states on a torus. We show the method to construct the ground state of the $\nu = 1/3$ model firstly, and then extend this argument to the $\nu = 1/q$ Laughlin states. We also show that the interaction of this model has the same degree of freedom as that of the pseudo potential for the Laughlin wave function, and one can naturally derive general properties of the Laughlin wave function such as the Z_2 classification and the relation between fermions and bosons. Thus our model gives a simple reference model to describe the $\nu = 1/q$ Laughlin states.

We introduce the matrix-product method to obtain the exact ground states. The physical quantities such as correlation functions, string order parameters, entanglement entropy, and excitation spectra are calculated analytically using the matrix product method. The obtained ground states have many properties similar to Laughlin states. For example, they have the common feature that the charge density functions tend to be uniform with the torus becoming isotropic. We can conclude that our solvable model captures physical features of the $\nu = 1/q$ FQH system. We show that the $m=1$ Jain's series, with the filling factor $\nu = p/(2p+1)$ and $\nu = (p+1)/(2p+1)$, can be mapped to $S=1$ effective spin chains with p sites in a unit cell by considering the dominant hopping term. By numerically analyzing, we point out that these effective spin chains have similar properties to those of $S=p$ integer Heisenberg chains with Haldane gaps which decrease as S is increased. These results give one of the explanations regarding the relationship between the hierarchy of FQH states and Haldane conjecture on the quantum spin chains.

Finally, we introduce a 1D representation of the FQH systems with Landau level mixing. We show the 2-body interactions in a $\nu = 1/2$ FQH system can be converted into 3-body interactions in each unit cell, which correspond the 3-body Haldane pseudo-potential for the even-denominator FQH states. These interactions can be written into projection operators in the Hamiltonian, so that we can find the exact ground state of this system in the thin torus.

備考 : 論文要旨は、和文 2000 字と英文 300 語を 1 部ずつ提出するか、もしくは英文 800 語を 1 部提出してください。

Note : Thesis Summary should be submitted in either a copy of 2000 Japanese Characters and 300 Words (English) or 1copy of 800 Words (English).

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