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# Customizable Strokes for Localized Stylization of View-Dependent Lines Extracted from 3D Models

Luis Cardona

Tokyo Institute of Technology:

Graduate School of Information Science and Engineering

Tokyo, Japan

Email: luis@img.cs.titech.ac.jp

Suguru Saito

Ochanomizu University:

Graduate School of Humanities and Science /

Tokyo Institute of Technology:

Graduate School of Information Science and Engineering

Tokyo, Japan

Email: suguru@is.ocha.ac.jp

**Abstract**—We propose a method to stylize individual lines and preserve their properties as the viewpoint is modified. As the camera position changes and view-dependent lines move across the surface, we track each line in order to extract and store the areas of the surface in which they appear. Each line has a unique reference that we use to check an indexed table from which we can recover its stylization after arbitrary camera movements. We call this region the *tracked area* of the line. Additionally, we provide a method for line segmentation of *occluding contours*. In our algorithm, we divide the contour lines at inflection points in order to segment them in a way that is suited for *localized stylization* as well as to better approximate artist strokes. We also optimize the line tracking process by making use of the Gaussian curvature to separate the elliptic and hyperbolic areas of the surface. In this paper we show how each line only appears in a limited area of the surface corresponding to its *tracked area*. We also discuss how to eliminate the over-segmentation caused by numerical instability of the approximations in polygonal surfaces as well as how smoothing can be used in order to deal with highly detailed models. Finally, we highlight the achievements of our system for *localized stylization* of the contour lines of 3D models.

**Keywords**—NPR; line drawings; stylization; segmentation; tracking;

## I. INTRODUCTION

### A. Background and purpose

Computer-generated 3D models have been extensively used in applications that try to replicate realistic imagery. However, there is another branch of computer graphics called NPR (Non-photorealistic rendering), that focuses on how to imitate the principles of abstraction used by artists. NPR research covers different topics like line extraction algorithms, stylization and animation coherence. Yet, there is still many problematics to solve in order to generate imagery with the same degree of abstraction and stylization as human-made drawings.

As stated in a recent study[2], most of the lines drawn by artist to convey 3D shape can be explained by some of the most commonly-known line extraction algorithms. However, artists often make global decisions such as the omission of implicit lines or stylistic decisions which tend to depart from realism. Therefore, there is a need for flexible user interfaces which enables designers to customize the appearance of drawings as well as to emphasize or omit some of its details.

Usually line drawings have a consistent style for all the scene but artists also include subtle stylization differences in each stroke. However, algorithms for extracting lines only provide local information like the location of lines or curvature data for each vertex of the mesh. Our system performs a segmentation of the extracted lines to differentiate individual continuous lines and divide them at inflection points. Once a line is selected, the user can customize it by changing its shape. We also provide an user interface to easily select each of them individually or select every line inside a *Gaussian curvature area*.

The main problem to solve in order to successfully achieve *localized stylization* of individual lines is how to recognize each of them as the same entity as the viewpoint changes.

### B. Related work

Various methods have been proposed in order to extract lines from 3D models. Image-space algorithms focus on image processing methods such as edge detection to extract the lines at each pixel of the output image[3], [4], [5], [6]. This type of algorithm generates quite convincing images but suffers from noise problems and are unsuitable for further stylization.

Object-space algorithms are based on the field of differential geometry which analyzes the properties of curves and surfaces. Previous research has successfully characterized different type of lines by making use of

derivatives of different order. The main contributions in this category are occluding contours[1], suggestive contours[7], [8], ridges and valleys[9] and apparent ridges[10].

Recently, some researches have focused on how to propagate the parameters of the lines in order to maintain the coherence of stylized strokes as the viewpoint changes or the 3D model is animated[11], [12], [13], [14], [15].

Previous papers have stated the need for user interfaces to provide better control of the rendering styles[16], [17]. These systems are useful to quickly define the style of the whole scene but do not provide the means to customize individual details.

Finally, 3D model segmentation algorithms have focused in how to divide surfaces into meaningful parts consistent with how humans perceives the shape of objects[18].

## II. ALGORITHM

In this paper, we make the assumption that the inflections of contour lines have high probability to be chosen by artists as terminal points. We will start by describing the relationship between inflections points and surface curvature.

The apparent curvature  $\kappa_{app}$  is the curvature of the contours in image-space[19].  $\kappa_{app}$  is positive at convex parts of contours, negative in the concave parts and zero at inflections. Koenderink[1] described the relationship between the apparent curvature  $\kappa_{app}$  and the Gaussian curvature  $K$  as follows:

$$\kappa_{app} = \frac{dK}{\kappa_r} \quad (1)$$

with  $d$  being the distance to the camera and  $\kappa_r$  the radial curvature.

Since visible occluding contours only appear where  $\kappa_r$  is positive, both  $\kappa_{app}$  and  $K$  have the same sign. Consequently, we use  $K$  instead of  $\kappa_{app}$  to divide the contours at inflections (where  $K = 0$ ).

In the case of *suggestive contours*, the lines only appear at hyperbolic regions (where  $K < 0$ ). As result, we can not segment these lines in the same way as *occluding contours*.

### A. Gaussian curvature areas

We segment the surface using the sign of the Gaussian curvature by separating the elliptic ( $K > 0$ ) and the hyperbolic ( $K < 0$ ) parts of the model (Fig. 1). We call these regions *Gaussian curvature areas*. The benefit of the Gaussian curvature segmentation is that not only it enables us to divide the line tracking problem in similar

subproblems but also it is directly related to the inflection points of contour lines. In the case of *suggestive contours*, the zero-crossings of  $K$  can not be related to inflection points. However, the *Gaussian curvature areas* are still useful to apply different styles and thresholds on different areas.

We make use of the connectivity data of the triangles as well as the zero-crossings of  $K$  to determine at which area each vertex belongs to. Afterwards, we pass the  $K$  zero-crossing data to a fragment shader in order to assign an unique color for each area. This shader also builds the boundaries between the areas by assigning different colors to each side of the triangles containing a zero-crossing of  $K$ . It should also be noted that, in the case of non-animated models, the Gaussian curvature is view-independent, i.e. constant, which means that the segmentation can be pre-computed. Additionally, we added the functionality of manually merge areas because the user may want to decide if a line should be segmented at the boundary between two areas or not.

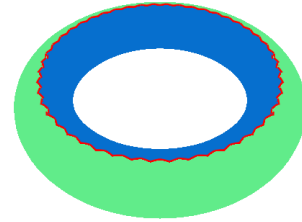


Figure 1. Gaussian curvature areas separated by the boundary where  $K = 0$  (red)

1) *Smoothing*: Meshes with high level of detail usually result in a highly fragmented segmentation. Depending on the drawing style we want to replicate, we may want to ignore some of the surface detail in favor of a more simplified line segmentation.

Smoothing is commonly used for noise removal of rough meshes, e.g. 3D scan reconstructions of physical objects. A frequently used method for smoothing meshes is Laplacian smoothing. Laplacian smoothing can be thought as the equivalent of lowpass filtering in signal processing. Desbrun et.al. [20] describes the discrete approximation of the Laplacian as a weighted sum of the one-ring neighbors of a vertex:

$$\mathcal{L}(x_i) = \sum_{j \in N} w_{ij}(x_j - x_i) \quad (2)$$

where  $x_j$  are the neighbors of the vertex  $x_i$  and  $N$  is the set of neighbor vertices.

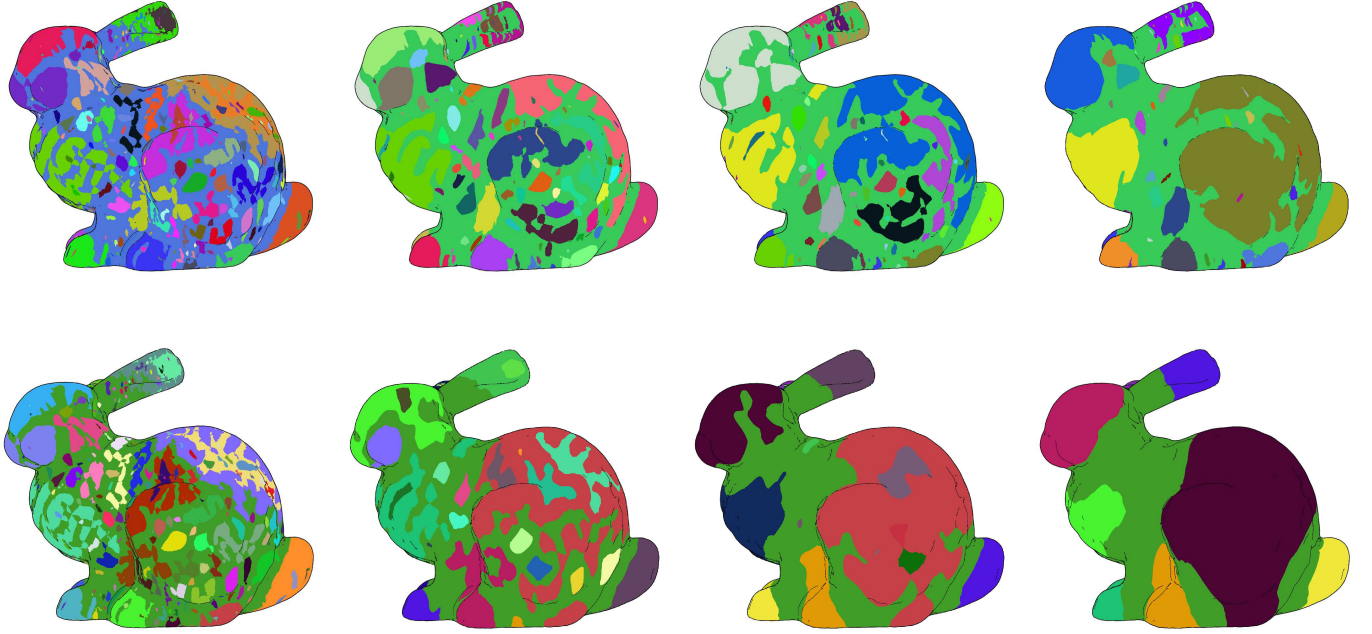


Figure 2. Original segmentation and Laplacian smoothing applied to the vertices positions (top) and the Gaussian curvature (bottom) for 5, 25 and 100 iterations.

For a given vertex, the most simple of the proposed approximations defines the Laplacian as the vector to the barycenter of its one-ring neighbors. This is also known as the *umbrella operator* and uses equal weights:

$$w_{i,j} = \frac{1}{m} \quad (3)$$

where  $m$  is the number of neighbors vertices.

The smoothed vertex positions can then be calculated as follows:

$$P_i(n+1) = P_i(n) + \frac{1}{m} \sum_{j \in N} (P_j(n) - P_i(n)) \quad (4)$$

Alternatively, Laplacian smoothing can also be directly applied to the values of the Gaussian curvature as follows:

$$K_i(n+1) = K_i(n) + \frac{1}{m} \sum_{j \in N} (K_j(n) - K_i(n)) \quad (5)$$

The results of both smoothing methods (Fig. 2) shows that as the number of iterations increases, the number of segmented areas decreases. Applying Laplacian smoothing directly to the Gaussian curvature is considerably faster because no recalculation of normals and curvatures is needed. Furthermore, the direct method tends to eliminate the over-segmentation caused by numerical instability. In comparison,

the method that includes the recalculation yields better results because it does not modify as much the shape of the boundaries of the areas but the numerical instability of the approximation of  $K$  still produces unwanted areas. However, this problem can be solved by merging the unwanted areas as described in the following section.

2) *Numerical instability*: For polygonal surfaces,  $K$  is just an approximation which can introduce undesirable artifacts (especially where the minimum curvature  $\kappa_2$  is around 0). In our case, we want to get rid of the areas which results in over-segmentation of the contour lines, i.e. the areas which are almost flat or are only bent in one direction.

We make use of a modified Sigmoid function to constrain the infinite values of the Gaussian curvature. The Sigmoid function is defined as:

$$s_\alpha(x) = \frac{1}{1 + e^{-\alpha x}} \quad (6)$$

where  $\alpha$  defines the shape of the Sigmoid function.

The following modified version takes values between 0 and 1 for positive values of  $x$ :

$$S_\alpha(x) = \frac{2}{1 + e^{-\alpha x}} - 1 \quad (7)$$

For each area, we calculate the average  $\kappa_2$  of all the vertices contained inside it:

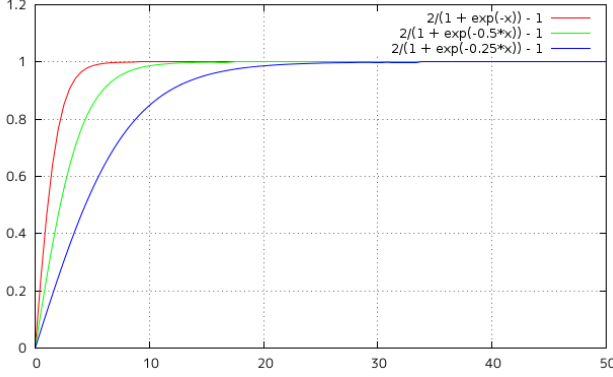


Figure 3. Modified Sigmoid function with different values of  $\alpha$

$$\bar{\kappa}_2 = \frac{1}{N} \sum_{i \in V} S_m(|\kappa_{2_i}|) \quad (8)$$

where  $V$  is the set of vertices of the area.

Finally, we merge the areas which have only one adjacent area and fulfill the following condition (Fig. 4):

$$\bar{\kappa}_2 < \delta \quad (9)$$

where  $\delta$  is an user-defined threshold.

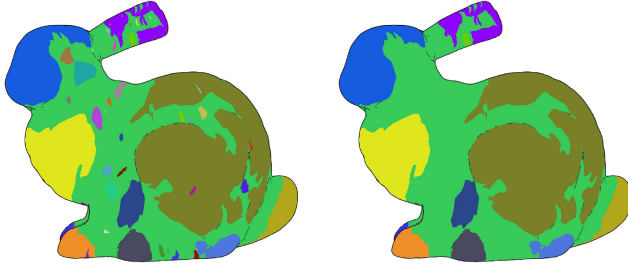


Figure 4. The unwanted areas produced by numerical instability are eliminated

### B. Generation of Tracked Areas

One of the main problems we face is that for view-dependent lines, the shape and position of each line changes depending on the viewpoint. Consequently, recognizing each contour line from frame to frame is essential to be able to stylize individual lines.

*1) Line tracking:* In our method, we check the squared distance of both start and end of a given line with all terminal points of the lines of the next frame. For the line currently being checked, we define the points  $s^k$  and  $e^k$  as the start and

end points respectively. A line in the frame  $k$  is considered the same as a line in frame  $k-1$  if the following conditions are fulfilled:

- $s^k$  and  $e^k$  are matched to the same line in frame  $k-1$
- $s$  and  $e$  are matched to different terminal points, i.e.  $s^{k-1} \neq e^{k-1}$

Additionally, we sample a number of equidistant points along each line and check the similarity of the matched lines using the Hausdorff distance:

$$h(A, B) = \max_{a \in A} (\min_{b \in B} (d(a, b))) \quad (10)$$

$$H(X, Y) = \max(h(X), h(Y)) \quad (11)$$

With  $X$  and  $Y$  being the sets of sampled point of the two lines being checked.

Therefore, in order to prevent mismatches we add the following condition:

$$H(X, Y) < \delta \quad (12)$$

With  $\delta$  being a distance threshold.

As previously stated, we decided to segment the lines at inflections points. This actually corresponds to dividing the lines as they cross the boundaries between *Gaussian curvature areas* in object-space. Therefore, we can optimize the tracking process by checking only the lines contained in the same *Gaussian curvature area*.

*2) Tracked areas:* As the camera position changes, view-dependent lines move across the surface until they eventually merge with other lines or completely disappear. Consequently, not all contour lines can be tracked at every viewpoint. It is then essential to be able to store and retrieve their references after arbitrary camera movements. Since contour lines can only appear inside a limited area, we store their references in a color-coded texture map containing the regions of the surface where each line has previously appeared (Fig. 5). We call these regions the *tracked areas*. It should be noted that the *tracked areas* can be considered as subsets of the *Gaussian curvature areas* (Fig. 6).

For any given line, we retrieve the reference from the texture map only if both of its terminal points and sampled internal points are in the same *tracked area*. The reference can then be used to recover the line stylization from the properties table (Table I). In our algorithm, the purpose of line tracking is limited to building the *tracked areas* corresponding to each contour line. Since these areas can be used to identify each line, pre-computing all the *tracked*

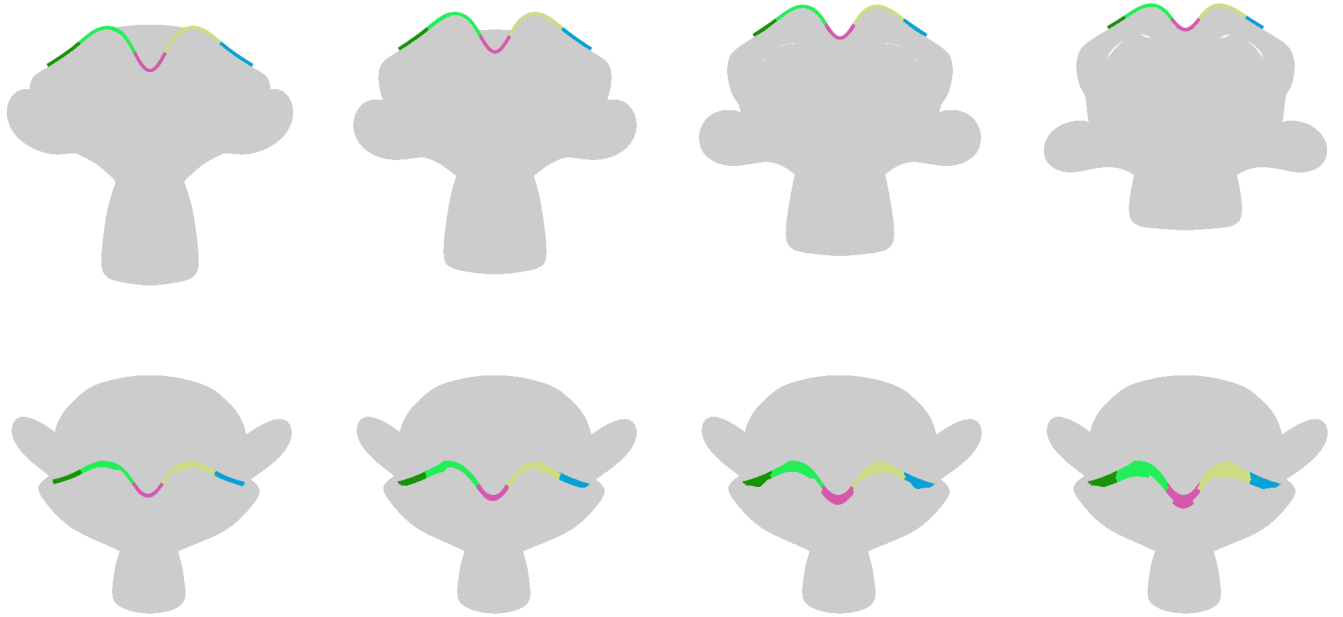


Figure 5. Five lines of a 3D model as the viewpoint changes (up) and the evolution of their tracked areas (down)

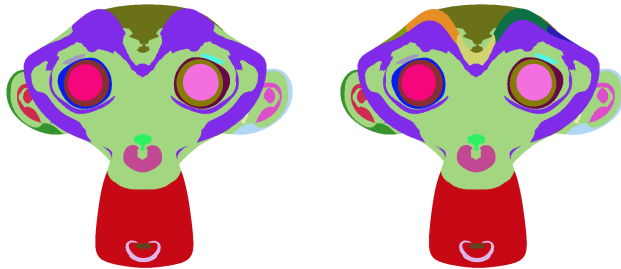


Figure 6. The original segmentation (left) and the tracked areas of 5 lines added as a subset of their corresponding Gaussian curvature area (right)

Reference	Line properties
0	$\omega, \alpha_T, \alpha_L, \dots$
..	..
..	..
..	..
n	$\omega, \alpha_T, \alpha_L, \dots$

Table I  
THE PROPERTIES TABLE INDEXED BY EACH LINE REFERENCE

*areas* would allow us to just retrieve the reference directly from the color-coded texture map, making further tracking unnecessary.

### C. Line rendering

We chose a commonly used method for line rendering that extrudes triangles strips along the zero-crossings in the

normal direction. As opposed to other line primitive based methods, this rendering method enable us to change the width along lines as much as we want. We also added length dependent width and tapering[21] using the same modified Sigmoid function defined in (7) of section II-A2. We can obtain a variety of line shapes by changing the  $\alpha$  coefficients of the Sigmoid functions. We can then calculate the width at a certain position of a line as follows:

$$W = \omega S_{\alpha_L}(L) S_{\alpha_T}(l) \quad (13)$$

With  $\omega$  being the user-defined base width,  $L$  the total length of the line and  $l$  a scalar taking normalized values increasing as we move away from the nearest terminal point.

## III. RESULTS

In our implementation, the user can select each line separately and change its properties or select a Gaussian curvature area and modify at once all the lines contained inside it. The process to stylize a line only needs to be done for one viewpoint because its properties are preserved as the camera moves. As result, our system not only frees the user from the tedious process of customizing all lines for every viewpoint and but also as opposed to previous stylization approaches[16], [17], we are able to stylize each line individually. For an experienced user, the whole process of stylizing the contour lines of the models shown in Fig. 7, 8 and 9 can be done in a few minutes. Additionally, we showed how unwanted areas caused by numerical instability can be



eliminated and also compared two smoothing methods for highly detailed models.

#### IV. CONCLUSION

We have proposed a method for *localized stylization* of *occluding contours* that preserves the properties of the lines as the viewpoint change. However, future approaches should implement more robust tracking methods to prevent incorrect matches. Our system only provides control over the line shape and therefore we should extend the range of customizable properties. In addition, given that different lines may appear in common regions, we should add support for overlapping *tracked areas*. We should also note that our algorithm partially supports *localized stylization* of *suggestive contours* but it is still lacking compared to *occluding contours*. Finally, the segmentation of contour lines may be extended to consider other important points like the extremas of contour points as possible candidates for terminal points.

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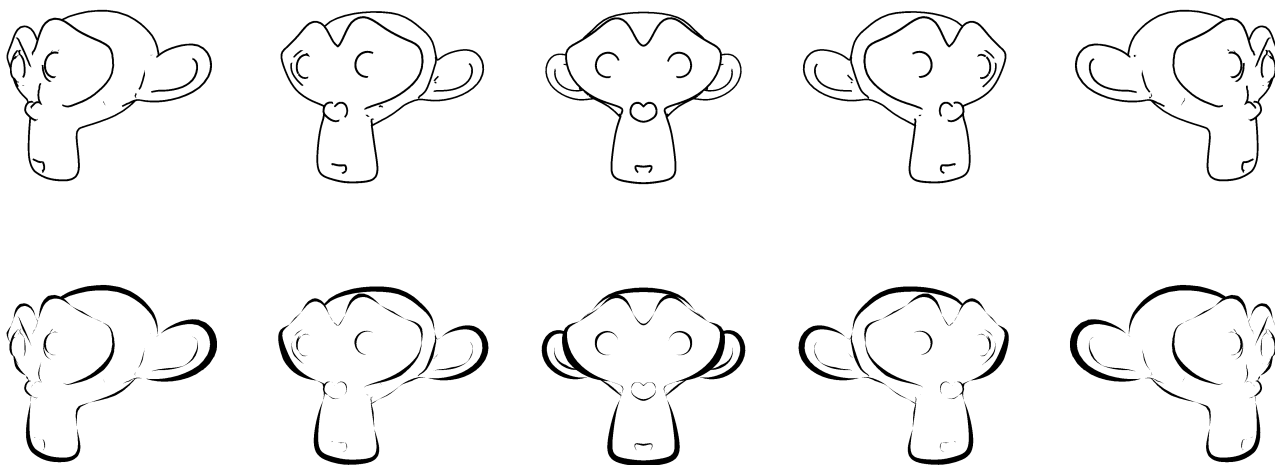


Figure 7. A monkey 3D model without stylization (up) and with *localized stylization* (down) as the viewpoint changes

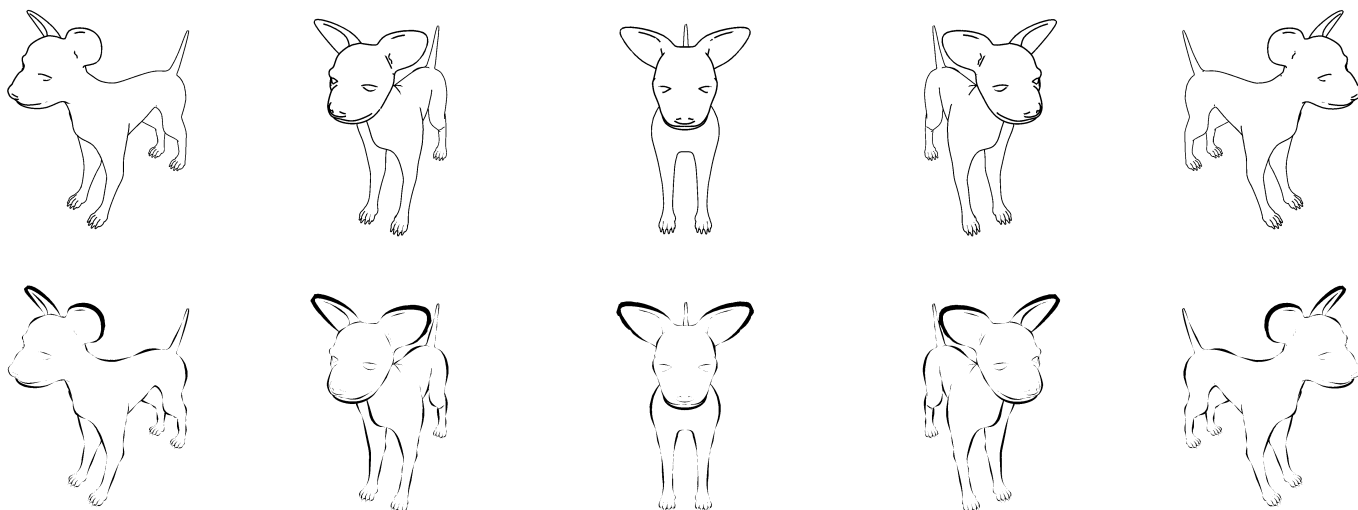


Figure 8. A dog 3D model without stylization (up) and with *localized stylization* (down) as the viewpoint changes



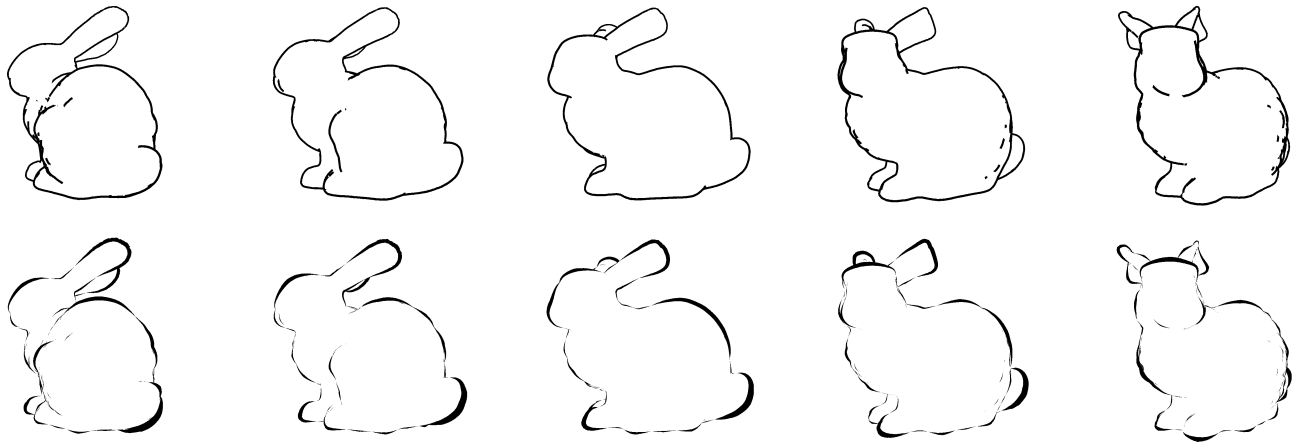


Figure 9. Stanford bunny without stylization (up) and with *localized stylization* (down) as the viewpoint changes