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著者(和文)	張庭維, 佐藤大樹
Authors(English)	Ting-Wei Chang, Daiki Sato
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## Zero-Crossing-Rate Based Global Damping Model of VE Systems Considering Frequency Sensitivity

正会員 〇張庭維\*

同 佐藤大樹\*\*

Wind-Induced Response, Global Damping Model, Viscoelastic,  
Frequency Sensitivity, Zero Crossing Rate.

## 1. Introduction

To well model the viscoelastic (VE) damper, the fractional derivative (FD) model can express the strain, temperature, and frequency dependency<sup>[1]</sup>. The wind time<sup>[2]</sup> (memorizing past data) is required for calculating the FD model, and the amount of data to be stored becomes enormous in the case of a long-period motion such as a wind response. Therefore, it is unsuitable for wind response analysis of high-rise buildings with many VE dampers installed. The global damping (GD) model<sup>[3]</sup>, which is expressed by only two parameters considering the natural frequency and damping ratio, is easily used for the wind-resistance design of the VE-damped structures but lacks considering its frequency dependency. The paper aims to propose a zero-crossing-rate-based method to simplify the frequency-sensitive VE-damped structure into the GD model considering the coupling effect by its frequency dependency and wind.

## 2. Target building and analytical model

The height of the target building is a  $H = 200$  m with an aspect ratio  $H/\sqrt{BD} = 4.0$ , whose  $D = B = 50$  m. Due to the wind-induced response of high-rise buildings is mainly caused by the contribution of the 1st mode<sup>[4]</sup>, the simulation in this study focused on the 1st modal single-degree of freedom (SDOF) model, including the frame with frame damping, the brace, and a VE damper (Fig. (1)). In the simulation, the natural period of frame is set as  $T_f = 0.02H$ . The 1st modal stiffness  $K_f$  and damping coefficient  $C_f$  of the frame can be obtained by Eq. (1, 2).

$$K_f = M \left( \frac{2\pi}{T_f} \right)^2 = M\omega_f^2, \quad C_f = 2M\omega_f\xi_f(\omega_f) \quad (1, 2)$$

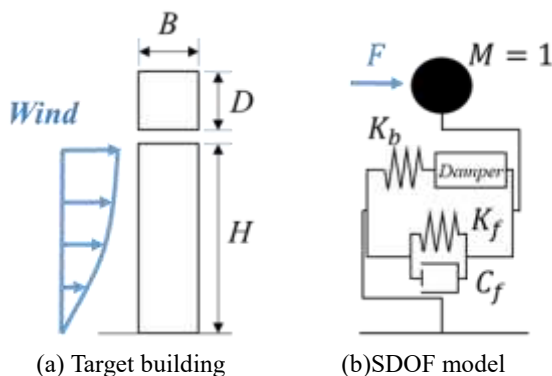


Fig. 1. Target building

## 3. Analytical wind

Fig. (2) shows examples of the 1st modal analytical wind force in the (a) along-wind and (b) across-wind directions in the time

history. For the along-wind force, to avoid the transient response in time-history analysis, the first and last 50 s were modified by envelope. Fig. (3) shows the 10-ensemble-averaging normalized power spectral density (PSD) of the 1st modal analytical wind force, in the along-wind (in red) and across-wind (in blue) directions. The PSD of the along-wind had the high power of a wide band at low frequencies. In contrast, the normalized PSD of the across-wind had a peak close to the frequency of 0.1 Hz.

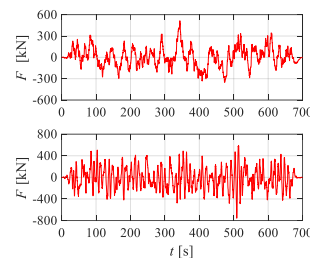


Fig. 2. Time history of wind force (a) along-wind without mean, (b) across-wind

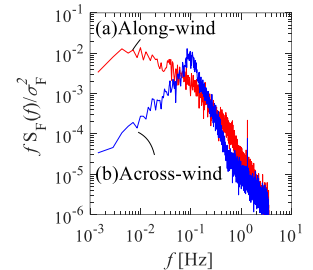


Fig. 3. Normalized PSD of wind force by 10-ensemble-averaging

## 4. VE systems

## 4.1. Resonance-frequency-based GD (RF-GD) model

The GD model (Fig. (4)) is commonly used in the wind-resistance design code for the damper.

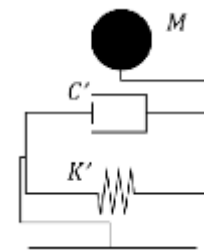


Fig. 4. GD model

To simplify the FD model into the GD model considering resonance frequency, this study names it the resonance-frequency-based global damping (RF-GD) model. The equivalent stiffness  $K'$  and damping coefficient  $C'$  of the RF-GD model are obtained, which is given by Eq. (3a, b)<sup>[1]</sup>.

$$K' = K_f + K'_a(\omega_n) \quad (3a)$$

$$C' = 2M\omega_n \left[ \frac{C_f}{2M\omega'_n(\omega_n)} + \frac{\eta(\omega_n)}{2} \right] \quad (3b)$$

## 4.2. Zero-crossing-rate based GD (ZR-GD) model

The equivalent stiffness  $K'$  and damping coefficient  $C'$  of the ZR-GD model are defined with the zero crossing rate  $\omega_{ZR}$ , given by Eq. (4a, b).

$$K' = K_f + K'_a(\omega_{ZR}) \quad (4a)$$

$$C' = 2M\omega_{ZR} \left[ \frac{C_f}{2M\omega'_n(\omega_{ZR})} + \frac{\eta(\omega_{ZR})}{2} \right] \quad (4b)$$

The zero crossing rate  $\omega_{ZR}$  can be obtained by the standard derivations ( $\sigma_D$ ,  $\sigma_V$ ,  $\sigma_A$ , and  $\sigma_J$ )<sup>[1]</sup>, given by Eq. (5). There are six kinds of  $\omega_{ZR}$  for wind-induced responses. When considering the along-wind responses, the standard deviation used along-wind responses (including displacement, velocity, and acceleration); when considering the across-wind responses, the standard deviation used across-wind responses, respectively.

$$\omega_{ZR} = \begin{cases} \sigma_{V,AL}/\sigma_{D,AL}, & \text{Disp.in along - wind direction.} \\ \sigma_{A,AL}/\sigma_{V,AL}, & \text{Velo.in along - wind direction.} \\ \sigma_{J,AL}/\sigma_{A,AL}, & \text{Acc.in along - wind direction.} \\ \sigma_{V,AC}/\sigma_{D,AC}, & \text{Disp.in across - wind direction.} \\ \sigma_{A,AC}/\sigma_{V,AC}, & \text{Velo.in across - wind direction.} \\ \sigma_{J,AC}/\sigma_{A,AC}, & \text{Acc.in across - wind direction.} \end{cases} \quad (5)$$

Where  $\sigma_D$ ,  $\sigma_V$ ,  $\sigma_A$ , and  $\sigma_J$  can be obtained by Eq. (6a-d).

$$\sigma_D = \sqrt{\int_0^\infty |H_D(i\omega)|^2 S_F(i\omega) d\omega}, \quad (6a)$$

$$\sigma_V = \sqrt{\int_0^\infty |i\omega H_D(i\omega)|^2 S_F(i\omega) d\omega}, \quad (6b)$$

$$\sigma_A = \sqrt{\int_0^\infty |-\omega^2 H_D(i\omega)|^2 S_F(i\omega) d\omega}, \quad (6c)$$

$$\sigma_J = \sqrt{\int_0^\infty |-i\omega^3 H_D(i\omega)|^2 S_F(i\omega) d\omega}, \quad (6d)$$

Here,  $H_D(i\omega)$  is the displacement transfer functions of the system<sup>[1]</sup>;  $S_F(i\omega)$  is the PSD of wind force.

### 5. Comparison of wind-induced responses

Fig. (5) shows the FD, RF-GD, and ZR-GD models' displacement responses in the along- and across-wind direction, respectively. Fig. (5a-i) and Fig. (5b-i) express that the maximum displacement of the RF-GD of the 2H-HH-00 model (an added component has both the hard stiffness of the brace and damper with no frame damping) has a massive difference from that of the FD model; but, the maximum displacement of the ZR-GD of the 2H-HH-00 model matches the FD model well. In contrast, Fig. (5a-ii) and Fig. (5b-ii) express the RF-GD and ZR-GD of the 2H-SS-00 model has the same trend of displacement response as the FD model.

Fig. (6) show the comparison of the accuracy of the

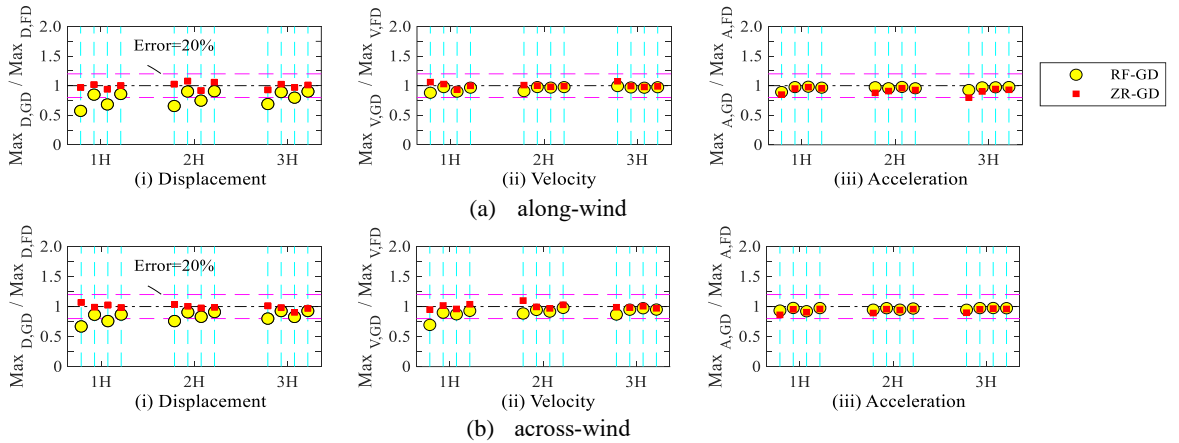


Fig. 6. Comparison of maximum responses: (HH, SH, HS, SS from left to right of each frame)

maximum of along- and across-wind responses respectively of RF-GD model and ZR-GD model with no frame damping. The ZR-GD models that match the maximum of the FD models well have better agreements than the RF-GD models.

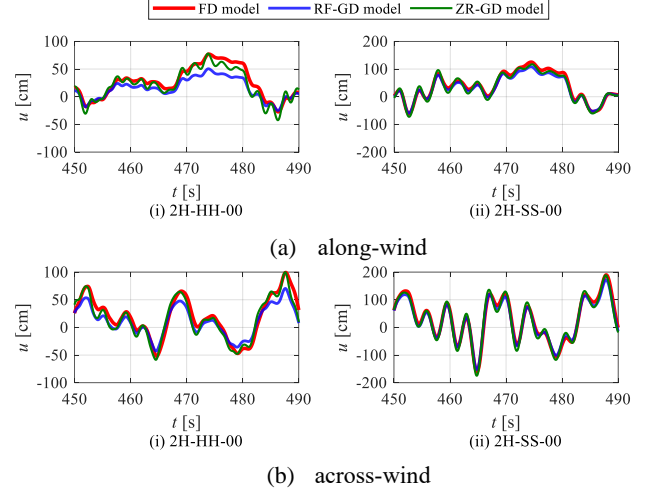


Fig. 5. Displacement of the FD, RF-GD, and ZR-GD models

### 6. Conclusions

This paper proposed the ZR-GD models for tall VE-damped buildings subjected to along- and across-wind forces, respectively. The behavior of the ZR-GD model of the VE-damped structure is described by a SDOF model, which considers the characteristics of both the frequency-sensitive fractional derivative model and wind excitation. Compared with the conventional RF-GD model, the ZR-GD model is verified with high accuracy by the fractional derivative model of the VE-damped structure.

### References

- [1] D. Sato, T.-W. Chang, Prediction on wind-induced responses for tall buildings considering frequency dependency of viscoelastic damped structures, *The Structural Design of Tall and Special Buildings* (2024) e2094
- [2] Sato, D., Chang, T. W., & Chen, Y. (2022). Effects of Different Frequency Sensitivity Models of a Viscoelastic Damper on Wind-Induced Response of High-Rise Buildings. *Buildings*, 12(12), 2182.
- [3] K. Kasai, K. Okuma, Evaluation rule and its accuracy for equivalent period and damping of frequency-dependent passive control systems [in Japanese], *Journal of Structural and Construction Engineering* 580 (2004) 51–59.
- [4] Hirai, H.; Yoshie, K.; Sato, D.; Suzuki, Y.; Kitamura, H. Characteristic of higher mode response of high-rise building under fluctuating wind force [in Japanese]. *AIJ Journal of Technology and Design* 2012, 18, 79–84.

\*東京工業大学環境・社会理工学院 大学院生

\*\*東京工業大学科学技術創成研究院 准教授・博士 (工学)

\* Doctoral Student, School of Environment and Society, Tokyo Institute of Technology

\*\* Associate Prof., IIR, Tokyo Institute of Technology, Dr. Eng.