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Learning from Demonstration and Adaptation of Biped Locomotion

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In this paper, we introduce a framework for learning biped locomotion using dynamical movement primitives based on nonlinear oscillators. Our ultimate goal is to establish a design principle of a controller in order to achieve natural human-like locomotion. We suggest dynamical movement primitives as a central pattern generator (CPG) of a biped robot, an approach we have previously proposed for learning and encoding complex human movements. Demonstrated trajectories are learned through movement primitives by locally weighted regression, and the frequency of the learned trajectories is adjusted automatically by a novel frequency adaptation algorithm based on phase resetting and entrainment of coupled oscillators. Numerical simulations and experimental implementation on a physical robot demonstrate the effectiveness of the proposed locomotion controller.

1. Introduction

There has been a growing interest in biped locomotion with the recent development of advanced humanoid robots. Many of existing successful walking algorithms use the zero moment point (ZMP) criterion [1] for off-line motion planning [2,3] and on-line balance compensation [4–6]. These ZMP based methods have been shown to be effective to achieve biped locomotion in legged robots with flat feet. However, they require precise modelling of the robot dynamics and high-gain trajectory tracking control, and the generated patterns result in a typical "bent-knee" posture to avoid singularities of inverse kinematics. From the viewpoint of energy efficiency, such walking patterns are not desirable since torque must be continuously applied to the knee joint to maintain a bent-knee posture. These previous ZMP approaches have primarily focused on the ability of executing planned movements at

any instance by ensuring surface contact between the sole and the ground [7] rather than natural human-like motion which exploits passive dynamics of the body [8].

In contrast to off-line trajectory planning, biologically-inspired control approaches based on central pattern generators (CPGs) with neural oscillators have been drawing much attention for rhythmic motion generation. As a CPG, a neural oscillator proposed by Matsuoka [9] is widely used, which models the firing rate of two mutually inhibiting neurons described in a set of differential equations. This model is used in robotic applications to achieve designated tasks involving rhythmic motion which requires interactions between the system and the environment. Examples include biped locomotion [10–13], quadruped locomotion [14], juggling [15], drumming [16], and playing with a slinky toy [17]. Neural oscillators have desirable properties such as adaptation to the environment through entrainment. However, it is difficult to design interconnection and feed-

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back pathways of neural oscillators, and to manually tune all open parameters in order to achieve the desired behavior.

Other approaches include [18] in an effort to design a simple controller based on physical intuition. The control strategy proposed in [18] is quite simple and easy to implement. However, it requires manual tuning of the control parameters and accurate torque controlled actuators.

In this paper, we suggest an approach to learning biped locomotion from demonstration and its adaptation through coupling between the pattern generator and the mechanical system. Motivated by human's capability of learning and imitating demonstrated movements of a teacher, imitation learning has been explored as an efficient method for motor learning in robots to accomplish desired movements [19–21]. In our previous work, we proposed dynamical movement primitives to encode complex discrete and rhythmic multi-joint movements through imitation learning [22]. Dynamical movement primitives are formulated as a set of autonomous nonlinear differential equations with well-defined attractor dynamics. Demonstrated trajectories are learned using locally weighted regression, and the output of dynamical movement primitives serves as kinematic movement plans, e.g., desired trajectories, for a robot.

This paper presents the idea of using the rhythmic movement primitives based on phase oscillators [22] as a CPG to learn biped locomotion from demonstration. Compared with neural oscillators, one of the appealing properties of phase oscillators is that the desired phase relationship among oscillators can be specified in a straightforward manner. In [23], a comprehensive formulation of phase coordination of coupled phase oscillators is proposed. Applications of coupled phase oscillators have been explored in the gait control of multi-legged robots [24,25] and the control of a biped robot [26]. In addition to using phase oscillators, our movement primitive has various desirable properties which are beneficial for biped locomotion. For example, it can learn a demonstrated trajectory rapidly, and it is easy to re-scale the learned rhythmic movement in terms of amplitude, frequency and offset of the patterns [22]. In the application of rhythmic move-
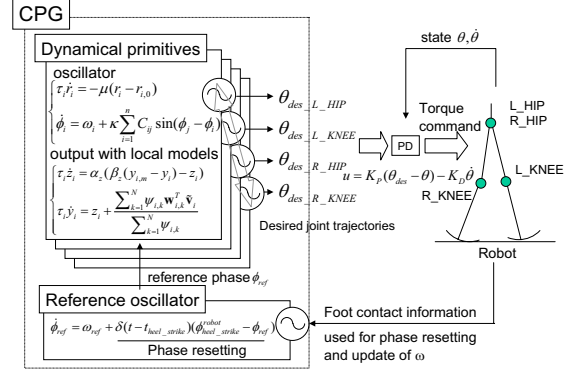

Figure 1. Proposed control architecture for biped locomotion with dynamical movement primitives.

ment primitives to biped locomotion, we introduce coupling terms to the movement primitives to achieve the desired phase relationship among limbs following the formulation proposed in [23]. We also propose an adaptation algorithm for the frequency of walking based on phase resetting [27] and entrainment between the phase oscillator and mechanical system using feedback from the environment. Frequency adaptation of a CPG is beneficial when the desired frequency of the coupled system is not exactly known in advance.

In [26], a similar idea of using coupled phase oscillators as a pattern generator for biped locomotion was proposed. In their method, desired joint trajectories of the legs are generated from a nominal trajectory at the tip of each leg defined by a combination of simple prescribed functions of phase through inverse kinematics [26]. In comparison to [26], we believe that our method has the advantage of flexibility in encoding complex movements by imitation learning and the potential capability of improving learned movements through reinforcement learning [28]. We demonstrate the effectiveness of the proposed control strategy by numerical simulations and experimental implementation.

2. Biped Robot

We use a planar 5-link biped robot developed in [29]. The height of the robot is 0.4 m and the weight is about 2 kg. The length of each link of the leg is 0.2 m. The mass of the body is 1.0 kg, the thigh is 0.43 kg and the shank is 0.05 kg. The motion of the robot is constrained within the sagittal plane by a tether boom. The hip joints are directly actuated by direct drive motors, and the knee joints are driven by direct drive motors through a wire transmission mechanism with the reduction ratio of 2.0. These transmission mechanisms with low reduction ratio provide high back drivability at the joints. Foot contact with the ground is detected by foot switches. The robot is an underactuated system having rounded soles with no ankles. Thus, it is challenging to design a controller to achieve biped locomotion with this robot since no actuation can be applied between the stance leg and the ground compared to many of the existing biped robots which have flat feet with ankle joint actuation.

3. Dynamical Movement Primitives

In this section, we outline the rhythmic dynamical movement primitives originally proposed in [22], which we will use as a CPG for biped locomotion in this paper.

3.1. Rhythmic Dynamical Movement Primitives

Rhythmic dynamical movement primitives encode periodic behavioral patterns as an output of a set of nonlinear dynamical systems composed of a *canonical* dynamical system with a phase oscillator and a *transformation* dynamical system with a nonlinear function approximator.

Consider the following limit cycle oscillator characterized in terms of an amplitude r and a phase ϕ as a canonical dynamical system which generates basic rhythmic patterns:

$$\tau\dot{\phi} = 1 \tag{1}$$
$$\tau\dot{r} = -\mu(r - r_0) \tag{2}$$

where τ is a temporal scaling factor, r_0 determines the desired (relative) amplitude, and μ is a positive constant. Note that the phase dynamics (1) can be written as:

$$\dot{\phi} = \omega \tag{3}$$

where $\omega \overset{\text{def}}{=} 1/\tau$ is the natural frequency. When there are multiple oscillators, we will introduce coupling terms among the oscillators (see Section 4.1). This rhythmic canonical system is designed to provide an amplitude signal $\tilde{\mathbf{v}} = [r\cos\phi, r\sin\phi]^T$ and phase variable $\text{mod}(\phi, 2\pi)$ to the following second order transformation dynamical system (z, y), where the output y is used as the desired trajectory for the robot:

$$\tau\dot{z} = \alpha_z(\beta_z(y_m - y) - z) \tag{4}$$
$$\tau\dot{y} = z + f(\tilde{\mathbf{v}}, \phi) \tag{5}$$

where α and β are time constants, y_m is an offset of the output trajectory. f is a nonlinear function approximator using local linear models [30] of the form:

$$f(\tilde{\mathbf{v}}, \phi) = \frac{\sum_{k=1}^{N} \Psi_k \mathbf{w}_k^T \tilde{\mathbf{v}}}{\sum_{k=1}^{N} \Psi_k} \tag{6}$$

where $\mathbf{w}_k$ is the parameter vector of the k-th local model which will be determined by locally weighted learning [30] from a demonstrated trajectory y_{demo} (see Section 3.2). Each local model is weighted by a Gaussian kernel function

$$\Psi_k = \exp(-h_k(\text{mod}(\phi, 2\pi) - c_k)^2) \tag{7}$$

where c_k is the center of the k-th linear model, and h_k characterizes its width. A final prediction is calculated by the weighted average of the predictions of the individual models. As demonstrated in [22], the amplitude, frequency and offset of the learned rhythmic patterns can be easily modified by scaling the parameters r_0, $\omega(= 1/\tau)$ and y_m individually.

3.2. Imitation Learning with Dynamical Movement Primitives

An important issue is how to learn the parameters $\mathbf{w}_k$ in the nonlinear function (6) to characterize the output of a dynamical movement primitive for a given demonstrated trajectory y_{demo}. Given a sampled data point $(f_{target}, \tilde{\mathbf{v}})$ at t where

$$f_{target} = \tau\dot{y}_{demo} - z_{demo} \tag{8}$$

and

$$\tau \dot{z}_{demo} = \alpha_z(\beta_z(y_m - y_{demo}) - z_{demo}),$$

the learning problem is formulated to find the parameters $\mathbf{w}_k$ in (6) using incremental locally weighted regression technique [30] in which $\mathbf{w}_i$ is updated by

$$\mathbf{w}_k^{t+1} = \mathbf{w}_k^t + \Psi_k \mathbf{P}_k^{t+1} \tilde{\mathbf{v}} e_k \qquad (9)$$

where

$$\mathbf{P}_k^{t+1} = \frac{1}{\lambda}\left(\mathbf{P}_k^t - \frac{\mathbf{P}_k^t \tilde{\mathbf{v}} \tilde{\mathbf{v}}^T \mathbf{P}_k^t}{\frac{\lambda}{\Psi_k} + \tilde{\mathbf{v}}^T \mathbf{P}_k^t \tilde{\mathbf{v}}}\right)$$

$$e_k = f_{target} - \mathbf{w}_k^T \tilde{\mathbf{v}}$$

and $\lambda \in [0,1]$ is a forgetting factor. We chose this locally weighted regression framework as it can automatically find the correct number of necessary basis function, and can tune the h_k parameters of each Gaussian kernel function (7) to achieve higher function approximation accuracy. Moreover, it learns the parameters $\mathbf{w}_k$ of every local model k totally independent of all other local models, which minimizes interference between local models and provides a means to robustly classify a rhythmic pettern with the help of the parameters $\mathbf{w}_k$ [22].

4. Rhythmic Dynamical Movement Primitives as a CPG

We use the rhythmic dynamical movement primitives introduced in Section 3.1 as a CPG for biped locomotion. Figure 1 illustrates the proposed control architecture in this paper. Each joint is equipped with a movement primitive which generates the desired joint trajectory θ_{des}. We define the index and the corresponding name of the joint as Left hip ($i = 1$, L_HIP), and Left knee ($i = 2$, L_KNEE), Right hip ($i = 3$, R_HIP), and Right knee ($i = 4$, R_KNEE). An additional oscillator (ϕ_{ref}) is allocated to provide a reference phase signal to the limb oscillators, which is adjusted by the ground contact information at the instance of heel strike. Section 4.1 introduces coupling to the oscillators of the movement primitives to achieve the desired phase relationship

between the limbs. Section 4.2 proposes a frequency adaptation algorithm of the learned periodic movements through the interaction among the coupled oscillators, robot and environment.

4.1. Inter- and Intra-limb Phase Coordination

We introduce coupling among the oscillators to regulate the desired phase relationship between the limbs of the robot. This kind of coupling is motivated from a biological point of view where it has been hypothesized that coupling among neural oscillators plays an important role in coordinating the desired phase relationship of limb movements in locomotion and gait transition [31].

Consider the following coupling terms for the oscillator i:

$$\dot{\phi}_i = \omega_i + \kappa \sum_{i=1}^{N} C_{ij} \sin(\phi_j - \phi_i) \qquad (10)$$

where κ is a positive constant gain, and C_{ij} is an element of the $n \times n$ matrix $\mathbf{C}$ which characterizes the coupling with other oscillators. This form of coupling appears in various studies of coupled oscillators and their application, e.g., [23–26,32,33]. In this paper, we employ the formulation in [23] to specify the desired phase relationship. In [23], $\mathbf{C}$ is defined to be a symmetric matrix where the diagonal elements are $C_{ii} = 0$ for all i, and off-diagonal elements C_{ij} are chosen as follows:

- $C_{ij} = 1$: oscillators i and j are designed to be in phase such that $\phi_i - \phi_j = 0 \pmod{2\pi}$.

- $C_{ij} = -1$: oscillators i and j are designed to be out of phase such that $\phi_i - \phi_j = \pi \pmod{2\pi}$.

As noted in [23], an arbitrary phase difference other than 0 or π can be specified by introducing a change of coordinates, or equivalent to having an offset in the coupling terms.

In this paper, we design the desired phase difference among the canonical oscillators such that the links of each leg move in phase (with zero phase difference), and the left and right legs move out of phase (with π phase difference) by defining the phase of the oscillator as $\phi_i = 0$ at the instance of heel strike of the corresponding

leg. More specifically, we require $\phi_1 - \phi_2 = 0$, $\phi_3 - \phi_4 = 0$, $\phi_1 - \phi_3 = \pi$, and $\phi_2 - \phi_4 = \pi$. Thus, the connection matrix $\mathbf{C}$ is chosen to be:

$$\mathbf{C} = \begin{bmatrix} 0 & 1 & -1 & -1 \\ 1 & 0 & -1 & -1 \\ -1 & -1 & 0 & 1 \\ -1 & -1 & 1 & 0 \end{bmatrix} \qquad (11)$$

4.2. Frequency Adaptation of Locomotion

Section 4.1 introduced internal coupling of the oscillators to coordinate the phase difference among the limbs of the robot. This section considers interaction between the environment and the CPG to achieve self-tuning of the natural frequency of the oscillators and synchronization of the CPG with the periodic behavior of the robot.

4.2.1. Synchronization of Coupled Oscillators with Frequency Adaptation

Before introducing the proposed frequency adaptation law for the biped robot CPG, let us consider the behavior of the following dynamics of two coupled oscillators:

$$\dot{\phi}_1 = \omega_1 + K_1(\phi_2 - \phi_1) \qquad (12)$$
$$\dot{\phi}_2 = \omega_2 + K_2(\phi_1 - \phi_2) \qquad (13)$$

where $\omega_1, \omega_2 > 0$ are natural frequencies of the oscillators, and K_1, K_2 are positive coupling constants. Then, the oscillators run with the phase difference $\psi^* = \phi_2 - \phi_1 = \frac{\omega_2 - \omega_1}{K_1 + K_2}$ at the coupled frequency $\omega^* = \frac{K_2\omega_1 + K_1\omega_2}{K_1 + K_2}$ when they are entrained. When $\omega_1 \neq \omega_2$, the phase difference $\psi = \phi_2 - \phi_1$ remains non-zero. However, if $\omega_1 = \omega_2$, then the phase difference of these oscillators will be zero. Thus, we introduce an update law of the natural frequency ω_1 to achieve synchronization of these oscillators with zero phase difference:

$$\dot{\phi}_1(t) = \omega_1(t) + K_1(\phi_2(t) - \phi_1(t)) \qquad (14)$$
$$\dot{\omega}_1(t) = K(\omega_2 - \omega_1(t)) \qquad (15)$$
$$\dot{\phi}_2(t) = \omega_2 + K_2(\phi_1(t) - \phi_2(t)) \qquad (16)$$

where K is a positive constant. It is straightforward to see that $\omega_1 \to \omega_2$ as $t \to \infty$. Thus, the phase difference will be zero such that $\psi = \phi_2 - \phi_1 \to 0$.

4.2.2. Frequency Update Law and Phase Resetting of CPG

In this section, we introduce an adaptation algorithm of the CPG in order to adjust the frequency of the learned periodic motions by the robot through the interaction among the CPG, robot and environment. As depicted in Figure 1, the proposed control system can be regarded as a coupling of the CPG and the mechanical oscillator (robot) which is analogous to the coupled oscillator system discussed in Section 4.2.1.

For this purpose, we first introduce a reference oscillator (ϕ_{ref}) which will be synchronized with the locomotion of the robot through the adaptation mechanism described below. This reference oscillator can be considered as a phase estimator of locomotion by the discrete heel strike information detected by foot switches. Then, additional coupling is introduced to the limb oscillators with ϕ_{ref} to achieve the desired relative phase $\phi_1 = \phi_2 = \phi_{ref}$ and $\phi_3 = \phi_4 = \phi_{ref} + \pi$.

Motivated by the synchronization mechanism of the coupled oscillators in Section 4.2.1, we propose the following phase resetting and frequency update law. They can be interpreted as a discretized version of phase coupling (14) and frequency update (15) at the instance of heel strike:

$$\dot{\phi}_{ref} = \hat{\omega}_{ref}^n + \delta(t - t_{heel\ strike})(\phi_{heel\ strike}^{robot} - \phi_{ref}) \quad (17)$$

$$\hat{\omega}_{ref}^{n+1} = \hat{\omega}_{ref}^n + K(\omega_{measured}^n - \hat{\omega}_{ref}^n) \qquad (18)$$

where δ is the Dirac's delta function, n is the number of steps, and $\phi_{heel\ strike}^{robot}$ is the phase of the mechanical oscillator (robot) at heel strike defined as $\phi_{heel\ strike}^{robot} = 0$ at the heel strike of the left leg, and $\phi_{heel\ strike}^{robot} = \pi$ at the heel strike of the right leg. $\omega_{measured}^n$ is the measured frequency of locomotion defined by

$$\omega_{measured}^n = \frac{\pi}{T_{measured}^n} \qquad (19)$$

where $T_{measured}^n$ is the stepping period of locomotion (half period with respect to the oscillator). At the same time, natural frequencies of all the limb oscillators ω_i are updated at the instance of heel contact such that $\omega_i = \hat{\omega}_{ref}^{n+1}$. Note that it is possible to directly introduce phase resetting to the limb oscillators as seen in [26]. However, introduction of a reference oscillator allows
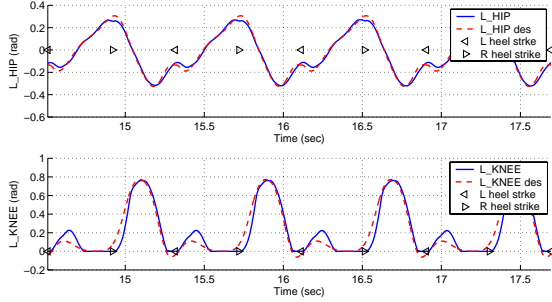
Figure 2. Joint trajectories for the left leg and heel strike timing for four periods (8 steps) of walking (simulation).

Figure 3. Torque command to the left hip and knee joints for four periods (8 steps) of walking (simulation).

phase estimation depending on multiple events and multi-modal information. Moreover, continuous phase coupling of the limb oscillators with the reference oscillator having phase resetting alleviates the problem of discontinuity to the desired joint trajectories.

The phase resetting algorithm (17) is motivated from a biological perspective as well as a mathematical point of view. Phenomena of phase resetting or phase shift are observed in many biological oscillators resulting from external perturbations, e.g., circadian pacemakers, biochemical oscillators and human finger tapping neural networks [27]. Phase resetting is related to the stability properties of neural rhythms, which can be analyzed by examining the phase dependent responses against perturbations. A recent study [34] investigated the role of phase resetting in biped locomotion. Numerical studies in [34] suggest possible contribution of phase resetting during walking to gait stability against external perturbations.

5. Numerical Simulations

As a demonstrated trajectory, we use the motion capture data of human walking in [35] (29-year-old male, 173cm, 83.5kg, right hip and knee). We identified the period and frequency of this pattern by the power spectrum estimation with
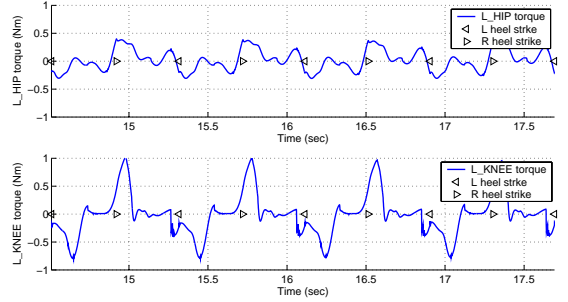
FFT and autocorrelation as $T = 1.17$ sec and $f = 1/T = 0.855$ Hz respectively. The dynamics of the robot are derived using SD/FAST[2] and integrated using the Runge-Kutta algorithm at 1ms step size. The ground contact force is calculated using a linear spring-damper model. A low-gain PD controller is used at each joint to track the desired trajectory which is the output of the movement primitive.

A walking pattern from the demonstrated trajectory is learned with the dynamical primitives. We manually designed the desired trajectory for the initial step of locomotion from a standing position at rest, and the proposed CPG controller is activated at heel contact of the first step. The amplitude parameter of the dynamical primitives is set to $r_0 = 0.7$, and the offset $y_m = 0.375$ is introduced to the knee joints. For the scaling of the natural frequency of the oscillator, the adaptation law proposed in Section 4.2.2 is used with the initial frequency of $\omega = 4.83$ rad/s (period of oscillation is 1.3 sec). These parameters are determined empirically from trial and error.

Figure 2 illustrates the desired and actual joint trajectories for the left leg, and the timing of heel strike after a stable pattern was learned by the phase resetting algorithm. Figure 3 shows the torque command for the left leg, which indicates
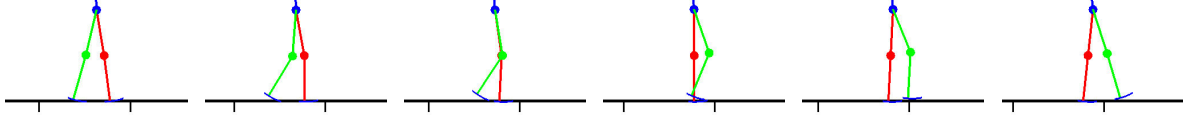
Figure 4. Snapshots of walking simulation for one step at 15 frames/sec (1 frame ≈ 66 msec)
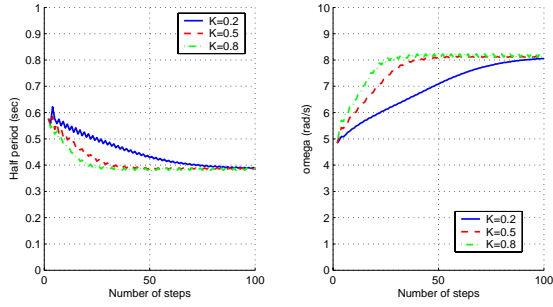

Figure 5. Frequency adaptation of walking via entrainment (simulation). Left: adaptation of period. Right: learning curve of the frequency of the CPG.
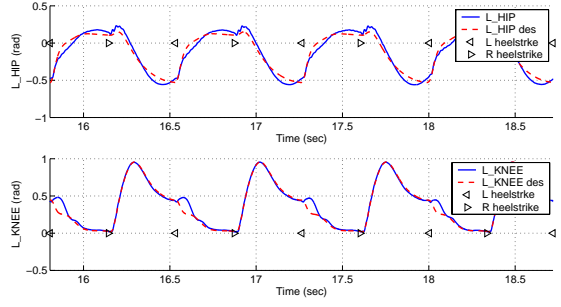

Figure 6. Joint trajectories for the left leg and heel strike timing for four periods (8 steps) of walking (experiment).

that the knee joint swings passively since it requires almost no torque (see $t = 15.1 \sim 15.3$ sec). Figure 4 depicts one step of walking. Figure 5 (left) shows the adaptation of the period of locomotion and Figure 5 (right) shows the learning curve of the frequency of the CPG with different coupling constants $K = 0.2, 0.5$ and 0.8 in (18). The stepping period approached 0.387 sec, and the resultant CPG frequency was $\omega = 8.12$ rad/s, which roughly corresponds to the natural frequency of the swing leg modelled as a simplified linear pendulum, using the proposed adaptation law.

Robustness against external perturbations is evaluated by pushing the robot forward and backward with external forces. Forces are applied for a duration of 0.1 sec at different timing during a single step (at an interval of 0.1 rad from 0 to 2π of the phase of the reference oscillator). When a forward perturbing force is applied, the robot could cope with up to 9.3 N (max) at $\phi = 0.5, 0.7 \sim 0.9$ rad, and 1.2 N (min) at $\phi = 2.8$ rad of the perturbing forces. When a backward perturbing force is applied, the robot could cope with up to -3.2 N (max) at $\phi = 4.9$ rad and -0.8 N (min) at $\phi = 0.3$ rad of the perturbing forces. In contrast, without phase resetting, the robot only could cope with much smaller disturbances, for example, the robot only tolerated up to 2.6 N of the forward perturbing force applied at $\phi = 0.5$.

The simulation results demonstrate self-adaptation of the frequency of locomotion and robustness of walking against disturbance by the proposed algorithm.
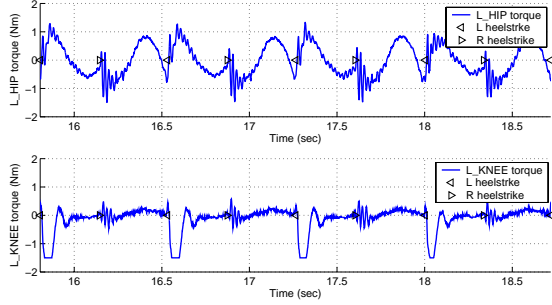
Figure 7. Torque command to the left hip and knee joints for four periods (8 steps) of walking (experiment).
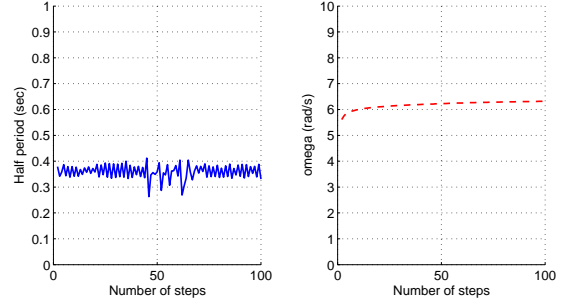

Figure 8. Frequency adaptation of walking via entrainment (experiment). Left: adaptation of period. Right: learning curve of the frequency of the CPG.

6. Experimental Implementation

We implemented the proposed control framework on our biped robot. In the experimental implementation, our initial attempt to achieve biped locomotion using the human demonstrated trajectory was not successful largely due to mechanical limitation of the experimental system and discrepancy in the ground contact condition between simulations and experiments. Thus, we used another target trajectory which was experimentally obtained from an actual trajectory of successful robot locomotion using a state machine controller. The state machine controller is designed to coordinate the leg movements with the physical state of the legged system based on the idea presented in [36].

To initiate locomotion in the experiments, we first suspended the robot with the legs swinging in the air, and then placed the robot on the ground manually. Thus, the initial condition of each run was not consistent, and occasinally the robot could not start walking or fell over after a couple of steps when the timing was not appropriate. Figure 6 illustrates the desired and actual joint trajectories for the left leg, and the timing of heel strike. Figure 7 shows the torque command for the left leg. Some oscillation in the torque command for the hip joint can be seen. This is due to noisy joint velocity signals obtained from numerically differentiated joint angles measured by optical encoders. We are currently planning to use gyros to obtain smoother joint velocities to improve the performance of the tracking controller. Note that a limit on the torque command is imposed at ± 1.5 Nm. Figure 8 (left) shows the period adaptation and Figure 8 (right) shows the learning curve of the frequency of the CPG. Stepping period for a typical walking experiment was around 0.37 sec. In this experiment, the initial frequency of the oscillator was set to $\omega = 5.71$ rad/s (period of oscillation is 1.1 sec), and the adaptation gain in (18) was decreased according to an annealing procedure $K = \frac{K_0}{n}$, where $K_0 = 0.05$ and n is the number of steps, as is needed in most gradient descent procedure. We introduced an offset α for phase resetting

$$\dot{\phi}_{ref} = \hat{\omega}^n + \delta(t - t_{heel\ strike})(\phi_{heel\ strike}^{robot} - \phi_{ref} + \alpha) \quad (20)$$

to adjust the timing of foot contact, where α is chosen to be $\alpha = 0.8$ rad. These parameters are determined empirically. Note that phase resetting with an offset effectively changes the period of oscillation.

Robustness of the proposed algorithm is evaluated by testing walking over surfaces with different friction properties such as carpet, cork sheet (3 mm thick) and a seesaw-like metal plate (2
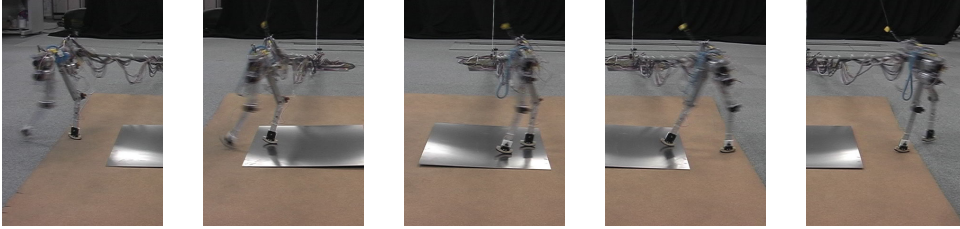
Figure 9. Walking over surfaces with different friction properties and a seesaw-like metal sheet with a slight change in the slope.

mm thick). The metal plate was placed so that the inclination of the slope slightly changes like a seesaw when the robot walks over it (the height of the center is 7 mm). The robot could deal with the change in the environment as depicted in Figure 9.

Note that even if we use the learned trajectory from the actual robot walking pattern, the robot could not walk by just replaying it as a desired trajectory. Phase resetting using foot contact information was necessary. This implies that appropriate on-line adjustment of the phase of the CPG by sensory feedback from the environment is essential to achieve successful locomotion. In addition, empirically we found that the proposed controller achieved much more robust walking compared to the state machine based controller which we originally designed.

7. Conclusion

In this paper, we proposed a method for learning biped locomotion from demonstration and its frequency adaptation using dynamical movement primitives. In the dynamical movement primitives, kinematic movement plans are described in a set of nonlinear differential equations with well-defined attractor dynamics, and demonstrated trajectories are learned using locally weighted regression. Specifically, we use rhythmic dynamical movement primitives based on coupled phase oscillators as a CPG, and introduced a frequency adaptation algorithm through interactions among the CPG, mechanical system and the environ-

ment motivated by the synchronization of coupled oscillators. Numerical simulations and experimental result demonstrate the effectiveness of the proposed control algorithm to achieve steady state walking roughly at the natural frequency of the coupled system. We also evaluated robustness against disturbance in numerical simulations and experiments.

Future work will address initiation and termination of walking, and on-line balance compensation. We will also consider collection of human's walking data under various behavioral conditions. In our current study, we used a simple phase resetting mechanism in which the phase of the CPG is forced to be reset to a specific value at the instance of heel strike regardless of the current phase of the CPG. In the future, we are interested in the generalization of the idea of phase resetting to determine phase dependent reaction against external perturbations such as recovery from stumbling by designing an appropriate phase resetting curve [27]. Formal mathematical analysis will be required to understand the principle of periodic stability of a limit cycle solution to the dynamics of a combined oscillator and mechanical system. In the long run, we are hopeful that our approach may provide insight into a theoretically sound design principle of biped locomotion control to achieve human-like natural walking.

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