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Design of a Weight-compensated and Coupled Tendon-driven Articulated Long-reach Manipulator

Atsushi Horigome1, Gen Endo2, Koichi Suzumori2 and Hiroyuki Nabae2

Abstract—A weight-compensated and coupled tendon-driven mechanism which is a combination of the existing two mechanisms is proposed and its static control is discussed. This mechanism allows the long-reach manipulator with very small actuators by applying one thick tendon to a coupled tendon-driven mechanism. Static control of tension was investigated and the solution which derives the tension of the joint controlling tendons and the weight-compensating tendon from the arm posture was proposed. Moreover, tendon tension on three types of the proposed mechanism is simulated in six postures. The weight-compensation sometimes requires large tension of the joint controlling tendons, however, it reduces tendons tension under around 2 kN basically.

I. INTRODUCTION

A tendon-driven manipulator which installs actuators in the base unit has many advantages compared with a manipulator which equips actuators in its joints. For instance, it can reduce the total weight of the arm since it does not have heavy actuators in the arm part, consequently make the actuators small and the arm slim. In this paper, taking advantages of the above, we propose a long-reach tendon-driven 3D multi-joint manipulator with a length of over 10 meters as a first step of the manipulator of 15 m length which meets the requirement for a survey of the inside of a primary containment vessel and so forth.

One of the existing methods to construct a tendon-driven slim multi-joint robot arm is to arrange tendons radially and winding and paying out the tendons[1][2][3][4]. Many tendons reach from the base unit to the arm joint and three (or four) tendons which are attached at equal intervals drive one joint. Although such constructions are very simple and can construct the light-weight arm part, there is the large friction between the tendons and structural parts. Each driving tendon goes through many arm segments and generates slide motions. When the arm becomes longer and/or the arm bends sharply, the friction increases ultimately and we have to control by large actuators and thick tendons. Therefore, it might be difficult for such construction to make a long-reach slim manipulator.

Now, we focus on the robot arm which consists of rigid links, pulleys and tendons. Transmitting all tendons via pulleys can greatly reduce friction between the tendons and the structural parts. Moreover, tendons and pulleys can construct a coupled tendon-driven mechanism which generates large torque in the proximal joint by coupling tendons traction force[5]. In our existing work, we proposed a coupled tendon-driven three-dimensional multi-joint manipulator and carried out experiments with a preliminary prototype model whose arm is 2.4 m length and consisted of 6 joints (4 pitches and 2 yaws) as shown in Fig. 1[6]. This manipulator moved in the space freely and showed the possibility to develop a long-reach manipulator by using a coupled tendon-driven mechanism. However, some tendons which drive proximal joints still need generating large tension and it shows that some large actuators and thick tendons are required.

Therefore, we focused on a weight-compensation mechanism[7]. This mechanism consists of one thick tendon which generates large torque in all joints to support the arm weight and the other small actuators which control the position of each joint. In this paper, we propose introducing a weight-compensation mechanism into a coupled tendon-driven mechanism to reduce tendon tension considerably. By introducing a weight-compensation mechanism, we develop a coupled tendon-driven manipulator with only one large actuator and some small actuators.

The organization of this paper is as follows. In section II, we discuss required tendon tension for long-reach multi-joint manipulator with/without a coupled tendon-driven mechanism. Moreover, we propose a weight-compensated and coupled tendon-driven mechanism which is a combination of the existing two mechanisms to reduce required tendon tension. In section III, we investigated the control system based on static balance by describing the relation between the tendon tension and the joint torque. In section IV, we simulate required tendon tension on three types of the weight-compensated and coupled tendon-driven manipulators in the case of six postures. In section V, we discuss a realistic

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Fig. 1: The preliminary prototype model of a coupled tendon-driven three-dimensional multi-joint manipulator
design of actuators from the result of section IV. In section VI, a summary is given.

II. MECHANICAL DESIGN OF A WEIGHT-COMPENSATED AND COUPLED TENDON-DRIVEN MANIPULATOR

A. A coupled tendon-driven mechanism

Fig. 2 shows the basic principle of a large torque generation on the proximal joint by a coupled tendon-driven mechanism. Three tendons are fixed to the three joints respectively. The tendon passes via free rotating pulleys at each of the joints between the joint which the tendon is fixed to and the acted part in the base. When the tendon has tension, torque is generated in all joints which the tendon passes through. Therefore, when the three tendons have tension $F$ in Fig. 2, torque which is generated in three joints is $3\tau$, $2\tau$ and $\tau$ respectively. This means the proximal joints which are passed by many tendons get larger torque than the distal joints. Using this principle, the manipulator can generate large torque at the proximal joints by small tension.

In order to assess tendon tension of a coupled tendon-driven mechanism, we set an over 10 m length multi-joint manipulator model as shown in Fig. 3. This model is also used in section 4 to assess a weight-compensated and coupled tendon-driven mechanism. The model has 7 links, each of the proximal 4 links has a pitch joint (1 DOF) and each tendon-driven mechanism. The model has 7 links, each of the proximal 4 links has a pitch joint (1 DOF) and each of the distal 3 links has pitch and yaw joints (2 DOF). We decided a link mass $m$, the length of 1 DOF link $l_1$, the length to the center of gravity of 1 DOF link $l_{g1}$ and 2 DOF link $l_{g2}$ and all pulleys diameters $D$ as follows:

$$m = 8 \text{ [kg]}, \quad l_1 = 1.43 \text{ [m]}, \quad l_2 = 0.4 \text{ [m]}, \quad l_{g1} = 0.35 \text{ [m]}, \quad l_{g2} = 0.5125 \text{ [m]} \quad \text{and} \quad D = 150 \text{ [mm]}.$$

A part of these values are based on the long-reach arm that we are currently designing. Actually, tendons cannot be arranged without using pulleys of various diameters, we unified the pulley diameters to solve the problem easily. Fig. 3 also shows tendon arrangement of a coupled tendon-driven mechanism.

Now, we lead required tendon tension with this model. When the required joint torque $\tau = \{\tau_j\} \in \mathbb{R}^{10 \times 1}$ is described as

$$\tau = \tau(\theta) \quad (1)$$

at joint angles $\theta = \{\theta_i\} \in \mathbb{R}^{10 \times 1}$, the following static relation between joint torque and tendon tension $F = \{F_j\} \in \mathbb{R}^{20 \times 1}$ is established:

$$\tau = \frac{D}{2} \delta F \quad (2)$$

where $\delta$ is a coefficient matrix to represent tendons and pulleys arrangement. In the case of a decoupled tendon-driven mechanism, $\delta$ is expressed as follows:

$$\delta = \begin{bmatrix} -1 & 1 & 0 & 0 & \ldots & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 1 & \ldots & 0 & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \ldots & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & \ldots & 0 & 0 & -1 & 1 \end{bmatrix} \in \mathbb{R}^{10 \times 20},$$

and in the case of a coupled tendon-driven mechanism, $\delta$ is expressed as follows:

$$\delta = \begin{bmatrix} -1 & 1 & -1 & 1 & \ldots & -1 & 1 & -1 & -1 \\ 0 & 0 & -1 & 1 & \ldots & -1 & 1 & -1 & -1 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \ldots & -1 & 1 & -1 & -1 \\ 0 & 0 & 0 & 0 & \ldots & 0 & 0 & -1 & 1 \end{bmatrix} \in \mathbb{R}^{10 \times 20}.$$

When the manipulator extends in the horizontal direction as shown in Fig. 3, the tension is simulated as shown in Fig. 4 by using the way to find $F$ from (2) which was already studied[5]. Now, $F_{2j-1}$ and $-F_{2j}$ are plotted at the joint number $j$ by yellow bars as a coupled tendon-driven mechanism and black bars as a decoupled tendon-driven mechanism. This shows a coupled tendon-driven mechanism reduces tendons tension, in particular, around a quarter at the first joint where the required torque is 2585 Nm. However, some tendons which drive proximal joints still need generating large tension compared with the distal joints. Therefore, we propose introducing a weight-compensation mechanism to reduce such tension.
B. Introduction of a weight-compensation mechanism

Fig. 5a shows the three joints model with a coupled tendon-driven mechanism and Fig. 5b shows the same model with a weight-compensation mechanism which we propose. Stretching one thick tendon, weight-compensating tendon, from the proximal joint to the distal joint, the manipulator can get large torque which supports the greater part of the manipulator weight. The other thin tendons support the rest torque and control the manipulator posture. We call the former thick tendon a weight-compensating tendon and the latter thin tendons joint controlling tendons in this paper.

The required torque to support the manipulator weight is different in each joint as shown in Fig. 4. In order to generate such torque by a weight-compensating tendon, the method of using double pulley which has different radii between the inlet side and the outlet side has been proposed[7]. For example, a weight-compensating tendon of the three pitch axes model is described as shown in Fig. 6a. In this model, the generated torque $\tau_{w,j}$ in the $j$th joint is derived as

\[ \tau_{w1} = r_1 F_w, \quad \tau_{w2} = \frac{r_1}{R_1} r_2 F_w \quad \text{and} \quad \tau_{w3} = \frac{r_1}{R_1} \frac{r_2}{R_2} r_3 F_w \]

(5)

respectively when the tendon tension is $F_w$. The relation of $\tau_{w1} \geq \tau_{w2} \geq \tau_{w3}$ is established when $r_1 \leq R_1$, $r_2 \leq R_2$ and $\max\{r_j\} \leq \min\{R_j\}$ are set. In the case of pitch and yaw axes model such as a distal part of the model in Fig. 3, tendon arrangement should be described as shown in Fig. 6b. This model has two weight-compensating tendons in order to cancel the torque at yaw joints. Generated torque values in all joints are

\[ \tau_{w1} = r_1 F_w, \quad \tau_{w2} = 0, \quad \tau_{w3} = \frac{r_1}{R_1} \frac{r_2}{R_2} r_3 F_w \quad \text{and} \quad \tau_{w4} = 0 \]

(6)

respectively. $\tau_{w2}$ and $\tau_{w4}$ are zero because two tendons cancel each torque. $\tau_{w1} \geq \tau_{w3}$ is established when $r_1 \leq R_1$, $r_2 \leq R_2$, $r_3 \leq R_3$ and $\max\{r_j\} \leq \min\{R_j\}$ are set.

The advantages of the weight-compensated and coupled mechanism are follows.

- It makes the force of actuators which control the joint controlling tendons smaller.
- It can unify all joint controlling tendons and all joint controlling actuators.
- Since the maximum tension is in proportion to a square of a pulley radius, the structure of one very thick tendon and some thin tendons has higher volumetric efficiency than the structure of some thick tendons. It contributes to making a slim manipulator.
The point to be noted is that one actuator is required to put out large force for the weight-compensating tendon such as a high torque motor, a pneumatic cylinder or a hydraulic cylinder.

III. Tendon Tension Control Based on Static Balance

In order to apply the weight-compensated and coupled tendon-driven mechanism, first of all, we need to decide the standard weight-compensating tendon tension and the radii \( r_{wj} \) of pulleys which the weight-compensating tendon is wound around. In this paper, we set them according to following procedures.

1) The standard posture \( \theta = \theta_{std} \) is set.
2) The standard tension \( F = F_{std} \) of the joint controlling tendons at the standard posture is set.
3) The required weight-compensating torque at the standard posture is derived as
   \[
   \tau_w = \tau - \frac{D}{2} \delta F
   \]  
   where \( \tau = \theta_{std} \) and \( F = F_{std} \).
4) The standard weight-compensating tendon tension and the radius of pulleys for the weight-compensation which satisfy (7) is derived. In real-time controlling, we have to calculate the tendon tension according to the manipulator posture. Since we are planning to control a long-reach manipulator slowly, the tendon tension is set on the basis of static balance. Procedures to derive tendon tension based on static balance are summarized as follows.

1) Required torque \( \tau \) at the joints is derived from the manipulator posture \( \theta \) by (1).
2) The tension of the joint controlling tendons \( F \) and the weight-compensating tendon \( F_w \) is derived from
   \[
   \tau = \frac{D}{2} \delta F + \tau_w(F_w)
   \]  
   where \( \tau_w = \{\tau_{wj}\} \in \mathbb{R}^{10 \times 1} \) is torque by the weight-compensating tendon tension \( F_w \) and pulleys \( r_{wj} \).

   We can calculate the procedure of 1) simply from the mass and the center of gravity of links. In order to solve the procedure of 2), \( \tau_w \) needs to be defined. In this paper, we adjust \( \tau_w \) to minimize the maximum of the tension of the joint controlling tendons \( F_{max} = \max \{F\} \). Moreover, the tendon tension must be positive at all postures because the tendon cannot generate negative force. Therefore, we set the tendons tension as
   \[
   F_w \geq F_{w\min} \geq 0 [N] \quad (i = 1, 2, \ldots, 20) \]  
   \[
   F_i \geq F_{i\min} \geq 0 [N] \quad (i = 1, 2, \ldots, 20)
   \]
   where \( F_{w\min} \) and \( F_{i\min}(i = 1, 2, \ldots, 20) \) is the minimum tendon tension in order to prevent the tendons slack.

   Since such a long-reach manipulator does not require being controlled quickly, we can search for \( \tau_w \) and \( F \) from simple algorithm to solve the non-linear programming problem under the conditions of (9) and (10). In the section IV, we used steepest descent method as a function \( F_{max} \) of tendon tension \( \{F, F_w\} \) and the longest time expended for a solution was only 23 ms.

IV. Tension Simulation of Three Models

A. Model setting

In order to assess the weight-compensated and coupled tendon-driven mechanism, we simulate the joint controlling tension at various postures with the model which is described in Fig. 3. Since the distal 2 DOF links require smaller tension than the proximal 1 DOF links as shown in Fig. 4, we applied a weight-compensation mechanism to only distal 4 pitch axes like Fig. 6a.

We set the standard posture of the manipulator to the horizontal direction as shown in Fig. 3 because the required torque at the first joint is the largest at that posture. We define the joints angles \( \theta \) as
   \[
   \theta = 0 [\text{rad}]
   \]  
   at the standard posture. In this simulation, we consider the three cases of the standard tension \( F_{std} \) of the joint controlling tendons as follows:

   case (a) \( F_i = 10 [N] \) \( (i = 1, 3, 5, 7, 9) \) \quad (12)
   case (b) \( F_i = 1000 [N] \) \( (i = 1, 3, 5, 7, 9) \) \quad (13)
   case (c) \( F_i = 2000 [N] \) \( (i = 1, 3, 5, 7, 9) \) \quad (14)

   The tension of the proximal joint controlling tendons which competes the above tension \( (F_{2,4,6,8,10}) \) is set to \( F_{min} \). The tension of the distal joint controlling tendons \( f_{11} \) to \( 20 \) is calculated regardless of the weight-compensation. We set \( F_{w\min} = F_{w\min} = 10 [N] \) as the minimum tension.

   Table I shows the radii of the weight-compensation pulleys \( r_{wj} \) of the inlet part and the standard weight-compensating tendon tension which are derived from (7). The radii of the outlet part pulleys are set to 75 mm, same as the joint controlling pulleys. The standard weight-compensating tendon tension \( F_{wstd} \) is 31.1 kN, 26.2 kN and 21.2 kN respectively. These values are possible when we use a \( \phi 8 \) mm stainless steel wire rope[8] driven by a \( \phi 250 \) mm hydraulic cylinder at 0.7 MPa, a \( \phi 10 \) mm hydraulic cylinder at 25 MPa or a large motor reducer[9] with a \( \phi 80 \) mm reel.

   Fig. 7 shows the tension of the joint controlling tendons at the standard posture. \( F_{2j-1} \) and \( -F_{2j} \) are plotted at the joint number \( j \) by yellow bars as a coupled tendon-driven mechanism and red, green and blue bars as the weight-compensated and coupled tendon-driven mechanisms of the cases (a), (b) and (c) respectively. In the distal part, there is no difference

<table>
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<th>CASE</th>
<th>( F_{std} [N] )</th>
<th>( F_{wstd} [kN] )</th>
<th>( F_{w1} [kN] )</th>
<th>( F_{w2} [kN] )</th>
<th>( F_{w3} [mm] )</th>
<th>( F_{w4} [mm] )</th>
<th>( F_{w5} [mm] )</th>
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<tr>
<td>(a)</td>
<td>10</td>
<td>31.1</td>
<td>75</td>
<td>52.5</td>
<td>48.0</td>
<td>40.9</td>
<td>27.1</td>
</tr>
<tr>
<td>(b)</td>
<td>1000</td>
<td>26.2</td>
<td>75</td>
<td>51.1</td>
<td>46.2</td>
<td>38.4</td>
<td>23.5</td>
</tr>
<tr>
<td>(c)</td>
<td>2000</td>
<td>21.2</td>
<td>75</td>
<td>50.0</td>
<td>43.3</td>
<td>34.0</td>
<td>15.7</td>
</tr>
</tbody>
</table>
Fig. 7: Comparison of tendon tension of a coupled tendon-driven model in each joint among a model without a weight-compensation and models with a weight-compensation. Yellow bars show tension without weight-compensation. Red bars, green bars and blue bars show tension with a weight-compensation of 31.1 kN (case (a)), 26.2 kN (case (b)) and 21.2 kN (case (c)) respectively.

B. Simulation in various postures

We simulated the required joint controlling tendons tension in six kinds manipulator postures. For each posture, we optimised the weight-compensating tendon tension $F_w$ under

$$F_{\text{wstd}} \geq F_w \geq F_{\text{wmin}} = 10 \text{ [N]}.$$  \hfill (15)

Since the tension of the distal five joints which do not have a weight-compensation mechanism is the same in all the cases, we show six kinds postures and the tension of the proximal five joints at those postures in Fig. 8.

Fig. 8a shows the non-special posture. In the cases of (a) and (b), the weight-compensating tendon tension $F_w$ is limited under $F_{\text{wstd}}$. This is because both $F_1$ and $F_{10}$ are the largest values in $F$. If $F_w$ becomes larger or smaller, neither $F_1$ or $F_{10}$ becomes larger. This applies to many other cases. In the case of (c), $F_w$ is $F_{\text{wstd}}$.

In Fig. 8b and Fig. 8c, the case (c) shows the largest tension in contrast with that the case (a) shows the largest tension in Fig. 8a, Fig. 8d, Fig. 8e and Fig. 8f. This is because the weight-compensating tendon tension $F_w$ can be set to the large value when the tension magnitude relationship between the joints is similar to the tension in the standard posture.

Fig. 8d shows the largest tension. This is because the required joint torque is very different between the first joint and the fifth joint. In such postures, a weight-compensation mechanism is not very effective.

Fig. 8f and Fig. 8e show the joint controlling tendons tension at the posture that the proximal part is horizontal.
and the distal part turns to the z-axis. The maximum value of $F$ is the same between Fig. 8f and Fig. 8e in all cases, however, the sum total of $F$ is smaller in Fig. 8e than that in Fig. 8f. This is because the shape in Fig. 8e is blunter than that in Fig. 8f.

In summary, the joint controlling tendons tension is under around 2 kN except for Fig. 8d. Although the joint controlling tendons tension is very small in the case (a) of Fig. 8a, the weight-compensation sometimes requires large tension in such as Fig. 8d. This means that the large standard weight-compensating tendon tension does not always reduce the joint controlling tendons tension. Moreover, the joint controlling tendons are required over 2 kN tension, which is the standard tension of the case (c), in some postures. Therefore, the case (c) is the best standard weight-compensating tendon tension in this simulation.

V. DISCUSSION

In this section, we discuss a realistic design of actuators which drive the joint controlling tendons. Since the long-reach manipulator moves slowly, the discussion focuses on static motion.

In the case of a coupled tendon-driven model without a weight-compensation, the maximum tension is 9.4 kN at the first joint as shown in Fig. 7. When a safety factor is 2, around $\phi = 5.3$ mm stainless steel wire rope[8] is required. According to the study on the strength reduction of a tendon[10], the large diameter of a tendon $d$ requires the large diameter of a pulley $D$ in order to prevent the tensile strength from decreasing. A pulley of around 80 mm diameters is required at $D/d = 15$. The driving torque can be calculated as $9.4 \times 2 \times 80/2 = 752$ [Nm]. This torque can be realized by using CSF50[11] and GP52C reducers and RE25 motor[12] at 1.8 rpm. These devices weigh 4.92 kg. In the similar way, five actuators which drive the proximal five joints weigh 15.3 kg.

On the other hand, in the case of a weight-compensated and coupled tendon-driven model, the manipulator can take most postures under 2 kN tension of tendons as shown in Fig. 8. An actuator which generate 2 kN tension with $\phi = 2.4$ mm stainless steel wire rope and $\phi = 36$ mm reel can be realized by using CSF25 and GP32C reducers and RE25 motor. Same ten actuators which are required to drive the proximal five joints weigh 7.1 kg.

In summary, our investigation of the actuators in a realistic design revealed that a weight-compensated and coupled tendon-driven mechanism reduces the total weight of actuators less than half of a non weight-compensated model.

VI. CONCLUSIONS

In this paper, we proposed a weight-compensated and coupled tendon-driven mechanism which is the combination of two existing mechanisms for making joint controlling actuators smaller. This mechanism allows the long-reach manipulator with very small actuators by applying one thick tendon. It can make all joint controlling tendons and all joint controlling actuators uniform.

Moreover, static control of tension was investigated. We discussed the solution to derive the tension of the joint controlling tendons and the weight-compensating tendon from the arm posture.

We also simulated required tendon tension on three types of the weight-compensated and coupled tendon-driven manipulators in six postures. We showed that the weight-compensation sometimes requires large tension, however, it reduce tendons tension under around 2 kN basically.

Finally, we discussed a realistic design of actuators which drive joint controlling tendons and showed that a weight-compensation mechanism reduces the total weight of actuators by half.

In future work, we plan to make coordinated tension control between the weight-compensating tendon and the joint controlling tendon with small joint model. This investigation contributes to develop a very long-reach manipulator.

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